

# CENTER FOR TRANSPORTATION INFRASTRUCTURE AND SAFETY



Design for FRP Systems for Strengthening Concrete Girders in Shear

by

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A National University Transportation Center at Missouri University of Science and Technology

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FRP systems have been used on a project-specific basis for the last two decades. They are now becoming a widely accepted method of strengthening concrete structures. The acceptance and utilization of these new strengthening techniques depend on the availability of clear design guidelines, installation procedures and construction specifications. Standard specifications exist for all commonly used traditional materials in civil engineering structures. At this time, design specifications for FRP use are still under development. The results of several experimental investigations have shown that FRP systems can be effective for increasing ductility and strength to structural members such as columns and girders. As most of the research focused on strengthening of axial members of flexural members, there are less experimental and analytical data on the use of FRP systems for shear strengthening of girders. Shear strengthening with FRP is still under investigation and the results obtained thus far are scarce and sometimes controversial. Even in traditional reinforced concrete members without FRP, the shear design is a complex challenge and uses more empirical methods as compared to axial and flexural design methods. Adding FRP to the equation, with its specific design issues, would bring another level of complication in the design. These FRP-related shear design issues and lack of comprehensive analytical and experimental models are the main motivation for this research project. Thus, a thorough understanding of the shear design problem along with the development of an AASHTO design method for FRP shear strengthening of concrete girders are needed.

As such, the objective of this project is to develop design methods, specifications, and examples for design of FRP systems for strengthening concrete girders in shear. The proposed specifications will be in LRFD format and will be suitable for recommendation to the AASHTO Highway Subcommittee on Bridges and Structures for adoption.

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### FOREWORD

By Amir N. Hanna Staff Officer Transportation Research Board

This report presents design guidelines for concrete girders strengthened in shear using externally bonded Fiber-Reinforced Polymer (FRP) systems. These guidelines address the strengthening schemes and application of the FRP systems and their contribution to shear capacity of reinforced and prestressed concrete girders. The guidelines are supplemented by design examples to illustrate their use for concrete beams strengthened with different FRP systems. The guidelines are presented in AASHTO LRFD format to facilitate use and incorporation into the AASHTO LRFD Bridge Design Specifications. Also, the report presents recommended changes to the AASHTO LRFD Bridge Design Specifications to introduce provisions pertaining to the use of FRP systems for strengthening concrete girders in shear. The material contained in the report should be of immediate interest to state bridge engineers and those involved in the strengthening and repair of concrete structures using FRP systems.

Use of externally bonded FRP systems for the repair and strengthening of reinforced and prestressed concrete bridge structures has become accepted practice by some state highway agencies because of their technical and economic benefits. Such FRP systems are lightweight, exhibit high tensile strength, and are easy to install; these features facilitate handling and help expedite repair or construction. Extensive research has shown that FRP systems improve both short- and long-term flexural behavior of concrete girders. Several analytical studies have dealt with the shear behavior of concrete girders strengthened with FRP systems and a number of models were developed to predict such behavior. However, limited experimental studies have investigated the validity of these models. Nevertheless, some of these studies have shown that FRP systems can provide an effective means for increasing the shear capacity of concrete girders. Currently, there are no widely accepted guidelines for the design of concrete girders strengthened in shear using externally bonded FRP systems. Thus, research was needed to review available information, conduct analytical and experimental investigations to evaluate the contributions of FRP systems to shear capacity, and develop design guidelines for concrete girders strengthened in shear using externally bonded FRP systems. These guidelines will provide highway agencies with the information necessary for considering externally bonded FRP systems for shear strengthening of concrete girders to expedite repair and yield economic and other benefits.

Under NCHRP Project 12-75, "Design of FRP Systems for Strengthening Concrete Girders in Shear," Missouri University of Science and Technology of Rolla, conducted a review of the existing information and practices relevant to the strengthening of concrete girders in shear using FRP systems; identified the factors that influence the design of such girders; evaluated available design methods and the shear design parameters that account for the FRP strengthening; and conducted laboratory tests to evaluate the effect of important factors on

girder response and shear strengthening. Results of this work provided a basis for developing guidelines and proposed changes to the *AASHTO LRFD Bridge Design Specifications*. The guidelines and proposed changes are accompanied by commentaries that are necessary for explaining the background, applicability, and limitations of the respective provisions. In addition, design examples are provided to illustrate use of the guidelines for designing FRP systems for strengthening reinforced and prestressed concrete beams.

The guidelines presented in this report will be particularly useful to highway agencies because they facilitate consideration of FRP systems among the options available for the shear strengthening of concrete girders and help select options that are expected to yield economic and other benefits. The incorporation of the recommended design guidelines into the AASHTO LRFD Bridge Design Specifications will provide easy access to the information needed for the design of externally bonded FRP systems for the strengthening of concrete girders in shear.

The appendix contained in the research agency's final report provides further elaboration on the work performed in this project. This appendix titled "Research Description and Findings" is not published herein; but it is available on the *NCHRP Report 678* summary webpage at http://www.trb.org/Main/Blurbs/164622.aspx.

### CONTENTS

1	Summary													
4	Chapter 1 Introduction													
4	1.1 Background													
4	1.2 Research Objectives													
4	1.3 Research Plan and Methodology													
4	1.4 Organization of the Report													
7	Chapter 2 Summary of Major Findings													
7	2.1 Use of FRP for Shear Strengthening of Concrete Girders													
7	2.2 Field Applications													
8	2.3 Existing Analytical Models													
8	2.4 Experimental Investigations Reported in the Literature													
21	2.5 Current Codes/Guidelines/Specifications													
22	2.6 Factors Affecting the Design of FRP Shear Strengthening													
32	2.7 Performance Evaluation of Existing Design Methods													
33	2.8 Suggestions for Improved Design Methods													
35	2.9 Reliability Assessment													
37	Chapter 3 Application and Implementation													
37	3.1 Approaches for Relevant Changes to AASHTO LRFD													
	Bridge Design Specifications													
38	3.2 Design Guidelines													
38	3.3 Design Examples													
39	<b>Chapter 4</b> Summary of Findings and Recommendations for Future Research													
39	4.1 Summary of Findings													
40	4.2 Suggestions for Future Research													
41	Notations													
47	References													
51	<b>Attachment A</b> Recommended Changes to AASHTO LRFD Bridge Design Specifications													
59	<b>Attachment B</b> Recommended Design Guidelines for Concrete Girders Strengthened in Shear with RFP													

Note: Many of the photographs, figures, and tables in this report have been converted from color to grayscale for printing. The electronic version of the report (posted on the Web at www.trb.org) retains the color versions.

### SUMMARY

# Design of FRP Systems for Strengthening Concrete Girders in Shear

### **Background**

Fiber-reinforced polymer (FRP) systems have been used for more than 20 years and are becoming a widely accepted method of strengthening concrete structures. The use of FRP composites in rehabilitating structures has grown in popularity due to its advantages over conventional materials and wide range of structural applications. FRP systems for strengthening reinforced or prestressed concrete girders consist of externally bonded laminates or near-surface mounted bars. These systems may contain either carbon or glass fibers. Because of their light-weight and exceptional formability, FRP reinforcements can be quickly and easily bonded to even the most curved and irregular surfaces. The high strength-to-weight ratio of FRP composites makes them more structurally efficient than traditional strengthening materials. In addition, FRP composites are noncorrosive, nonmagnetic, nonconductive, and generally resistant to chemicals.

Externally bonded FRP systems composites are generally used for flexural strengthening, confinement and improvement of ductility in columns, or shear strengthening. Although flexure is typically the limiting mode of failure in bridge girder design, shear failure may dominate in cases where the transverse reinforcement has severely corroded or the flexural strength has been increased due to flexural strengthening. In such cases, the shear capacity should be enhanced to avoid catastrophic failures. A significant amount of research has been conducted on flexural and axial strengthening but limited investigations have been conducted on the use of externally bonded FRP for shear strengthening. Nevertheless, several models have been proposed for predicting the shear contribution of externally bonded FRP. These models are diverse in their approach and in many cases contradictory in their estimates of strength increase. FRP reinforcement configurations include the selection of surfaces to be bonded (side bonding, U-wrap, complete wrap), continuous reinforcement or a series of discrete strips, and orientation of the primary direction of fibers. The bond characteristics between the FRP and concrete substrate add to the complexity in understanding the FRP shear contribution. The effectiveness of the strengthening method has been found to depend on the mode of failure.

The use of FRPs for external strengthening of concrete structures has been hindered by the lack of comprehensive design provisions. Design of FRP strengthening systems has been based on system- or project-specific research. The AASHTO LRFD Bridge Design Specifications (AASHTO, 2008) include no provisions for the design of externally bonded FRP systems. NCHRP Project 12-75 was initiated to develop a recommended design method for shear strengthening of concrete girders using FRP systems.

### **Project Objectives and Scope**

The objective of this project was to develop design methods, specifications, and examples for the design of FRP systems for strengthening concrete girders in shear. The proposed specifications are intended for incorporation into the AASHTO LRFD Bridge Design Specifications (AASHTO, 2008). Such specifications will provide design engineers with the information needed for considering externally bonded FRP systems for shear strengthening of existing structures. To accomplish this objective, the research involved the following tasks:

- Study and review relevant practices, existing models and specifications, and research findings from both foreign and domestic sources regarding the use of externally bonded FRP for shear strengthening of concrete girders.
- Identify and evaluate criteria that influence the performance of FRP shear strengthening systems based on review of the literature (including the development of a database of tests related to FRP shear strengthening).
- Evaluate the performance of existing design methods.
- Investigate in full-scale tests, the key parameters affecting the shear performance of externally bonded FRP for both reinforced concrete (RC) and prestressed concrete (PC) girders.
- Recommended provisions and specifications for incorporation into the AASHTO LRFD Bridge Design Specifications.

### **Overview**

To develop design provisions for shear strengthening with externally bonded FRP systems, the parameters affecting the behavior of such systems were identified first through review of the existing literature. Also, a database of the reported test results on the use of externally bonded FRP for shear strengthening was compiled. An experimental program was then developed to further study parameters that were considered to have not been sufficiently investigated in earlier tests, including the effects of pre-cracking, continuity (negative moment), long-term conditioning (such as fatigue loading and corrosion of internal steel reinforcement), and prestressing. The experimental program included full-scale tests on RC T-beams and AASHTO type PC I-girders because most current design equations used in design specifications are based on small-scale test results. An assessment of the existing design methods found significant differences in the magnitude of the FRP shear contribution calculated by various design methods. This assessment revealed the deficiencies of the existing design methods in predicting the shear resistance of a wide range of girder and FRP reinforcement characteristics. Therefore, new design equations for predicting the shear contribution of externally bonded FRP systems were developed and calibrated.

### **Research Findings**

The major findings of this research effort are summarized as follows:

- Externally bonded FRP can be used to enhance the shear resistance of concrete girders.
- The effectiveness of externally bonded FRP for shear strengthening depends on the failure mode (i.e., FRP rupture or debonding).
- The effectiveness of FRP shear strengthening is significantly affected by the cross-sectional shape of the girder.
- The use of a properly designed mechanical anchorage system delays and in some cases prevents debonding of the FRP, resulting in a more effective strengthening scheme.

- An interaction exists between the transverse steel reinforcement and externally bonded FRP; the effectiveness of externally bonded FRP for shear decreases as the transverse steel reinforcement ratio increases.
- The shear span-to-depth ratio (a/d) has a significant influence on the effectiveness of externally bonded FRP for shear.
- The size-effect has little influence on the effectiveness of externally bonded FRP and thus empirical design expressions calibrated from small-scale test results should provide reasonable accuracy.
- The presence of pre-existing cracks and slight damage due to corrosion of the internal transverse steel reinforcement prior to strengthening does not seem to impair the effectiveness of the external FRP shear reinforcement.
- Beam continuity does not seem to influence the effectiveness of the FRP strengthening system.
- The effective FRP strain used in evaluating the FRP shear contribution can be expressed by two separate design expressions to consider the two predominant failure modes (i.e., debonding and FRP rupture).
- Under severe fatigue loading conditions (e.g., stirrups yielding), externally bonded FRP shear reinforcement may experience debonding if proper anchorage is not provided. If stress in the stirrups can be maintained below the yield strength, the externally bonded FRP shear strengthening can help delay fatigue yielding of the stirrups and extend the fatigue life of the girder. If stirrups have already yielded prior to FRP application, the FRP may still help contain the stresses and prevent catastrophic failure but not necessarily extending the service life of the girder.

### CHAPTER 1

### Introduction

### 1.1 Background

Fiber-Reinforced Polymer (FRP) systems have shown potential for use in rehabilitating and retrofitting existing structures. They can be used to provide increased ductility as well as shear and flexural strength to structural elements such as columns, beams/girders, slabs/decks, and walls. Typical applications include compensation for increased traffic volumes on bridges, dampening of vibration, corrosion rehabilitation, correction of deficient design, etc. (Busel and Barno, 1995 and ACI 440.2R-08, 2008).

FRP systems have been used on a project-specific basis for the last two decades. They are now becoming a widely accepted method of strengthening concrete structures. FRP systems used for strengthening reinforced or prestressed concrete girders consist of externally bonded laminates or near-surface mounted bars. These systems may contain either carbon or glass fibers and thus carbon fiber reinforced polymer (CFRP) or glass fiber reinforced polymer (GFRP). The acceptance and use of these strengthening techniques depend on the availability of clear design guidelines, installation procedures, and construction specifications. Standard specifications exist for all materials commonly used in civil engineering structures. However, design specifications for FRP use are not readily available. Most research has focused on strengthening of axially loaded or flexural members with limited experimental and analytical data on the use of FRP systems for shear strengthening of girders. This research, performed under NCHRP Project 12-75, was initiated to address FRPrelated shear design issues and related specifications and design methods.

### 1.2 Research Objectives

The objective of this project was to develop design methods, specifications, and examples for design of FRP systems for strengthening concrete girders in shear.

### 1.3 Research Plan and Methodology

The following tasks were performed to achieve the following project objectives:

- Review of relevant practice, data, specifications, and research findings from both foreign and domestic sources on the strengthening of concrete girders in shear using FRP systems containing carbon or glass fibers and identification of FRP systems available for shear strengthening.
- 2. Identification of criteria that influence design of FRP shear strengthening systems.
- Evaluation of existing design methods and the identification of appropriate shear design provisions that account for FRP and preparation of a work plan for further development of potential design methods.
- 4. Execution of the work plan and development of the design methods.
- Preparation of recommended specifications and commentary for shear design of FRP-strengthened concrete girders together with design examples to illustrate the application of the recommended design methods and specifications.
- 6. Preparation of a report that documents the entire research.

Figure 1.1 shows the process used to determine the critical issues that were addressed in the project. Figure 1.2 illustrates the process used to develop the design methods and specifications.

### 1.4 Organization of the Report

This chapter presents the background, objectives, methodology, and scope of the project. Chapter 2 summarizes the findings of the research, including the literature review as well as experimental and analytical investigations. Chapter 3

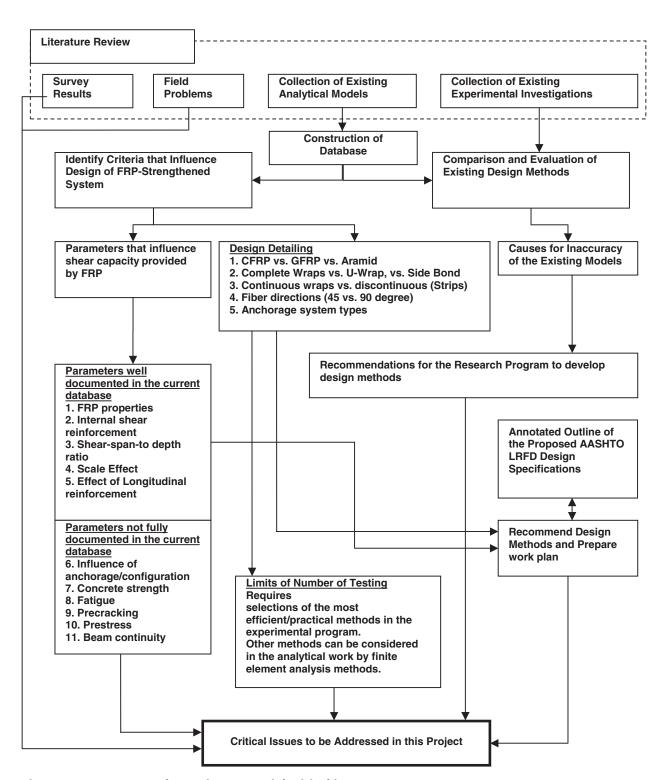


Figure 1.1. Process to determine potential critical issues.

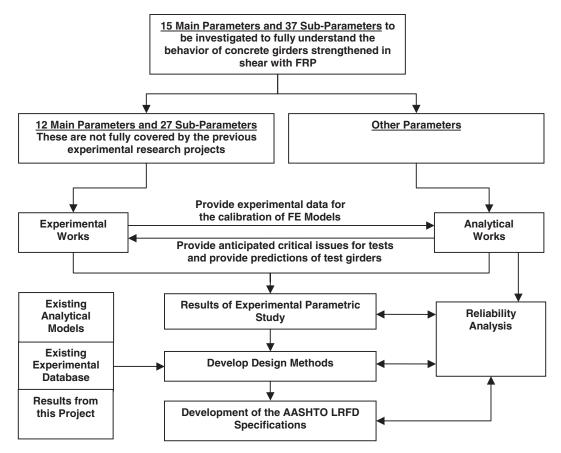


Figure 1.2. Process for developing design methods and specifications.

discusses the application and implementation of the recommended design method and specifications. Chapter 4 presents the conclusions and suggestions for future research. Attachments A and B present suggested changes to AASHTO LRFD Bridge Design Specifications (AASHTO, 2008) and recommended design guidelines, respectively.

Appendix A provides more details on all aspects of the research including, the literature review, survey of state DOTs, existing analytical models, experimental investigations, and data analysis. Appendix A is not published herein but can be found on the *NCHRP Report 678* summary webpage at http://www.trb.org/Main/Blurbs/164622.aspx.

### CHAPTER 2

# **Summary of Major Findings**

### 2.1 Use of FRP for Shear Strengthening of Concrete Girders

A survey of state departments of transportation (DOTs), Washington, DC, and Puerto Rico, was conducted to determine the extent of using FRP for shear strengthening. This survey included a written questionnaire (followed by either a telephone briefing or a written response) aimed at determining the practices for designing concrete girders strengthened in shear using FRP and their perceived deficiencies.

The responses received from 39 agencies revealed that only 7 state DOTs used FRP for shear strengthening of concrete girders and 32 DOTs have never used FRP for shear strengthening of concrete girders. Fourteen DOTs indicated no need for shear strengthening of concrete girders, and 12 DOTs expressed a concern about the lack of proper design specifications or provisions for FRP shear strengthening. Some DOTs considered the use of FRPs less efficient when compared to other strengthening techniques.

The DOTs using FRP for shear strengthening follow the design methods contained in ACI 440.2R-02 (ACI 440, 2002) because it was the only design guidelines document available in the United States. Some DOTs (e.g., New York, Oregon, and Pennsylvania) have made slight modifications to ACI 440.2R-02 (ACI 440, 2002). Design guidelines and specifications provided by FRP manufacturers and course notes from a workshop provided by several organizations were used by some state DOTs. Most state DOTs identified provisions regarding properties of FRP composite materials and control of failure modes as the most important issues to be addressed in future design specifications. An in-depth explanation on FRP strengthening schemes and fatigue and durability issues were also noted as major issues to be addressed.

### 2.2 Field Applications

Although there are several field projects related to FRP strengthening systems, detailed information on these projects is not available and most of these projects were strengthened for flexural rehabilitation. The following six projects were identified as directly related to FRP shear strengthening of concrete bridge girders:

A single span, reinforced concrete T-beam bridge in New York State was strengthened in flexure and shear with externally bonded FRP laminates in November 1999 (Hag-Elsafi et al., 2001b).

The Gröndals Bridge in Sweden is a prestressed concrete box bridge approximately 1,300 feet in length and a free span of 394 feet. CFRP laminate strips were applied to the inside walls with steel plate anchorage system to increase the shear strength (Taljsten et al., 2007).

The Langevin Bridge in Calgary, Canada, is a six-span, four-cell, continuous box-girder bridge constructed in 1972. The internal webs were found to be deficient at the right end of span 2 where the internal prestressing tendons are horizontal and thus contribute nothing to the shear resistance. To correct these deficiencies, CFRP sheets were bonded to the inside face of the external webs and to both faces of the interior webs

The John Hart Bridge in Prince George, British Columbia and the Maryland Bridge in Winnipeg, Manitoba, are two bridges in western Canada that have been strengthened in shear with externally bonded CFRP. The John Hart Bridge consists of seven simply supported spans with six I-shaped prestressed concrete AASHTO girders per span, and the Maryland Bridge consists of two sets of five continuous spans with seven I-shaped prestressed concrete AASHTO girders per span (Hutchinson et al., 2003).

The Willamette River Bridge located near Newberg, Oregon, was found to have significant diagonal cracking during an inspection conducted by the Oregon Department of Transportation (ODOT) in late summer of 2001. CFRP strips of 12 inch width were applied vertically in a U-shape wrapping scheme (Williams and Higgins, 2008).

The Ebay Island Viaduct Bridge is a 21/4 mile long section of westbound Washington State Route 2 that crosses over environmentally sensitive wetlands near the outflow of the Snohomish River into Puget Sound near Everett, Washington. The bridge was built during the late 1960s. In 1996, bridge condition inspectors noted that the bottoms of the existing precast concrete webs exhibited considerable concrete spalling accompanied with primary steel reinforcement corrosion. In 1999, carbon fiber sheets were bonded to the deteriorated elements for flexural strengthening and to compensate for steel reinforcement loss due to corrosion. In addition, carbon fiber sheets were applied with a U-wrap configuration to compensate for the shear capacity loss due to the cross-sectional loss of stirrups caused by corrosion. The carbon fiber repairs were inspected annually after the completion of the repair project with no debonding or deterioration of the carbon fiber plies being reported through spring 2007 (Dornsife, 2007).

### 2.3 Existing Analytical Models

This section summarizes the analytical models previously developed for determining the shear resistance of reinforced concrete members strengthened with externally bonded FRP. Seventeen models were found in the literature. These models have been divided into four groups based on their approaches and are presented in the same units as the original papers.

The first group of models is those relying on an empirically determined value of strain/stress associated with failure of the member for which the shear contribution of the FRP is determined; the principal equations of the analytical models in this group are listed in Table 2.1. The second group of models is those based on the determination of an effective FRP strain; the corresponding principal equations are listed in Table 2.2. The third group of models focuses on the non-uniformity of the strain distribution in externally bonded FRP reinforcements; the corresponding principal equations are listed in Table 2.3. The fourth group of models is mechanics-based theoretical approaches that do not rely on experimental results for regression or calibration; the principal equations of these models are listed in Table 2.4.

# 2.4 Experimental Investigations Reported in the Literature

A review was conducted of experimental investigations which included studies on (1) the behavior of concrete girders strengthened in shear with externally bonded FRP, (2) bond behavior of FRP-concrete interface, and (3) anchorage systems to enhance the effectiveness of FRP strengthening systems.

# 2.4.1 Studies on the Behavior of Concrete Girders Strengthened in Shear with Externally Bonded FRP

The review included 49 experimental studies, encompassing more than 500 test specimens. The review provides information on the objectives, the methodology, the experimental program, the test method, the FRP used and its orientation, as well as the strengthening scheme used (configuration).

Table 2.1. Models based on experimentally determined limiting value	е
of FRP shear strain/stress.	

Reference Author (Year)	Equations
	$V_{p} = \frac{2\left[\tau_{ave} \frac{t_{s} h_{s}}{2}\right] d}{S_{p}} $ (for shear strips)
Al-Sulaimani et al. (1994)	$V_P = 2\left[\tau_{ave}\left(\frac{dh_w}{2}\right)\right]  \text{(for shear wings)}$
	$V_P = 2\left[\tau_{ult}\left(\frac{dh_j}{2}\right)\right]  \text{(for U-jackets)}$
Chajes et al. (1995)	$\begin{split} V_f &= A_f E_f \mathcal{E} v_{cu} d \qquad \text{(for FRP oriented at 0/90 degree)} \\ V_f &= A_f E_f \mathcal{E} v_{cu} d \sqrt{2} \qquad \text{(for FRP oriented at 45/135 degree)} \end{split}$

<sup>\*</sup> Terms are defined in notations section.

Table 2.2. Models based on an effective FRP strain.

Reference Author (Year)	Equations
Triantafillou (1998)	$\begin{split} V_{frp,d} &= \frac{0.9}{\gamma_{frp}} \rho_{frp} E_{frp} \varepsilon_{frp,e} b_w d \left(1 + \cot \beta\right) \sin \beta \\ \varepsilon_{frp,e} &= 0.0119 - 0.0205 \left(\rho_{frp} E_{frp}\right) + 0.0104 \left(\rho_{frp} E_{frp}\right)^2 \text{ when } 0 \le \rho_{frp} E_{frp} \le 1 \text{ GPa} \\ \varepsilon_{frp,e} &= -0.00065 \left(\rho_{frp} E_{frp}\right) + 0.00245 \text{ when } \rho_{frp} E_{frp} > 1 \text{ GPa} \end{split}$
Khalifa et al. (1998)	$V_{f} = 0.9 \rho_{frp} E_{frp} \varepsilon_{fe} b_{w} d \left(1 + \cot \beta\right) \sin \beta  \text{(Eurocode format)}$ $V_{f} = \frac{A_{f} f_{fe} \left(\sin \beta + \cos \beta\right) d_{f}}{s_{f}}  \text{(ACI format)}$ $\varepsilon_{fe} = R \varepsilon_{fu}  f_{fe} = R f_{fu}$ Based on the effective FRP stress: $R = 0.5622 \left(\rho_{frp} E_{frp}\right)^{2} - 1.2188 \left(\rho_{frp} E_{frp}\right) + 0.778 \le 0.5 \text{ when } \rho_{frp} E_{frp} < 1.1 \text{ GPa}$ Based on bond mechanism: $R = \frac{0.0042 \left(f_{c}^{'}\right)^{2/3} w_{fe}}{\left(E_{frp} t_{f}\right)^{0.58} \varepsilon_{fu} d_{f}}$ Effective width: $w_{fe} = d_{f}  \text{(complete wrapping)}$ $w_{fe} = d_{f} - L_{e}  \text{(U-wrap)}$ $w_{fe} = d_{f} - 2L_{e}  \text{(side bonded)}$ $s_{f,\max} = w_{f} + \frac{d}{4} \qquad V_{s} + V_{f} \le \frac{2\sqrt{f_{c}^{'}} b_{w} d}{3}$
Hutchinson and Rizkalla (1999)	$\begin{split} V_n &= V_c + V_{se} + V_{f,\text{max}} \\ V_{f,\text{max}} &= \varepsilon_{f,ave} E_f  2nt_f  w_f  \frac{d_f \left(\cot \theta + \cot \alpha_f \right) \sin \alpha_f}{s_f} \\ \varepsilon_{f,ave} &= \varepsilon_{f\text{max}}  \frac{\left[d/2 + 0.5 \left(d_f - d/2\right)\right]}{d_f} \\ \varepsilon_{f\text{max}} &= L_{fe} C \\ L_{fe} &= e^{6.134 - 0.580 \ln \left(t_f E_f\right)}  \text{and}  C = constant \ strain \ rate \ of \ 110 \times 10^{-6}  mm^{-1} \\ V_{se} &= \varepsilon_{se} E_s A_v  \frac{d \cot \theta}{s}  \text{where}  \varepsilon_{se} = \varepsilon_{f,ave} \sin \alpha_f \big/ \gamma_{fs} \leq \varepsilon_{sy} \end{split}$

(continued on next page)

Table 2.2. (Continued).

	$V_f = 0.9 \rho_{frp} E_{frp} \varepsilon_{fe} b_w d (1 + \cot \beta) \sin \beta$ (Eurocode format)
Khalifa and Nanni (2000)	$V_{f} = \frac{A_{f} f_{fe} \left( \sin \beta + \cos \beta \right) d_{f}}{s_{f}} \qquad \text{(ACI format)}$ $\varepsilon_{fe} = R \varepsilon_{fu} \qquad f_{fe} = R f_{fu}$ $R \text{ is the least of :}$ $R = 0.5622 \left( \rho_{frp} E_{frp} \right)^{2} - 1.2188 \left( \rho_{frp} E_{frp} \right) + 0.778 \le 0.5$ $R = \frac{\left( f_{c}^{'} \right)^{2/3} w_{fe}}{\varepsilon_{fu} d_{f}} \left[ 738.93 - 4.06 (t_{f} E_{frp}) \right] \times 10^{-6}$ $R = \frac{0.006}{\varepsilon_{fu}}$
Triantafillou and Antonopoulos (2000)	$\begin{split} V_{fd} &= 0.9 \frac{\mathcal{E}_{fk,e}}{\gamma_f} E_f \rho_f b_w d \left(1 + \cot \beta\right) \sin \beta  \text{(Eurocode format)} \\ \mathcal{E}_{fk,e} &= \alpha \mathcal{E}_{f,e} \leq \mathcal{E}_{\text{max}} = 0.005 \qquad \alpha = 0.8  \text{(recommended)} \\ \\ \phi_f V_f &= \phi_f \mathcal{E}_{f,e,A} E_f \rho_f \left( \sin \beta + \cos \beta \right) b d  \text{(ACI format)} \\ \mathcal{E}_{f,e,A} &= 0.9 \mathcal{E}_{f,e} \leq \mathcal{E}_{\text{max},A} = 0.006 \\ \\ \mathcal{E}_{f,e} &= 0.65 \left( \frac{f_c^{2/3}}{E_f \rho_f} \right)^{0.56} \times 10^{-3}  \text{(CFRP debonding failure mode)} \\ \\ \mathcal{E}_{f,e} &= 0.17 \left( \frac{f_c^{2/3}}{E_f \rho_f} \right)^{0.30} \mathcal{E}_{f,u}  \text{(shear failure combined with or followed by CFRP fracture)} \\ \\ \mathcal{E}_{f,e} &= 0.048 \left( \frac{f_c^{2/3}}{E_f \rho_f} \right)^{0.47} \mathcal{E}_{f,u}  \text{(shear failure combined with or followed by AFRP fracture)} \\ \\ \left( E_f \rho_f \right)_{\text{lim}} &= \left( \frac{0.65 \times 10^{-3} \alpha}{\mathcal{E}_{\text{max}}} \right)^{1/0.56} f_c^{2/3} = 0.018 f_c^{2/3} \end{split}$
<b>Chaallal et al.</b> (2002)	$\begin{split} V_f &= f\left(\frac{a}{d}, \rho_{tot}\right) \!\! \left(\frac{A_f}{s_f}\right) \!\! E_f \boldsymbol{\varepsilon}_{e\!f\!f} d_f \\ \boldsymbol{\varepsilon}_{e\!f\!f} &= 3 \!\times\! 10^{-5} \!\times\! \rho_{tot}^{-0.6522},  \rho_{tot} = n \rho_f + \rho_s \\ \text{New deep beam coefficient: } f\left(\frac{a}{d}, \rho_{tot}\right) &= \frac{1 + 2a/d}{12} + \left(1000 \rho_{tot} - 0.6\right) \! \leq \! 1 \\ \text{but greater than } \frac{1 + 2a/d}{12} \end{split}$

Table 2.2. (Continued).

$$V_{f} = 0.9 \rho_{pp} E_{pp} E_{pp} E_{pb} k_{o} d (1 + \cot \beta) \sin \beta \quad \text{(Eurocode format)}$$

$$V_{f} = \frac{A_{f} f_{fe} (\sin \beta + \cos \beta) d_{f}}{s_{f}} \quad \text{(ACI format)}$$

$$E_{fe} = R E_{fu} \quad f_{fe} = R f_{fu}$$

$$R \quad \text{is the least of :}$$

$$R = 0.5622 \left( \rho_{fip} E_{fip} \right)^{2} - 1.2188 \left( \rho_{fip} E_{fip} \right) + 0.778 \le 0.5$$

$$R = \frac{0.006}{\varepsilon_{fu}}$$

$$R = R^{4} \left\{ 0.0042 \left( f_{cm} \right)^{2/3} w_{fe} / \left[ \left( E_{fip} t_{f} \right)^{0.58} \varepsilon_{fu} d \right] \right\}$$

$$0 \le R^{8} = -0.53 \ln \rho_{s,f} + 0.29 \le 1$$

$$\rho_{s,f} = E_{s} A_{to} / E_{f} A_{f}$$
for continuous fiber sheet:
$$V_{f} = w_{f} f_{fe} \sin \beta + \cos \beta \right) d_{f}$$

$$f_{fe} = R f_{fu}, \quad \varepsilon_{fe} = R \varepsilon_{fu}$$
Based on model calibration:
$$R = 1.4871 \left( \rho_{f} E_{f} / f_{e}^{-1} \right)^{0.7488}$$
Based on model calibration:
$$R = \frac{\tau_{max} L_{e}}{2 f_{fu} f_{f}} \le 1$$

$$\tau_{max} = \left( 5 \times 10^{-6} \times f_{e}^{-2} \right) - \left( 2.73 \times 10^{-2} \times f_{e}^{-1} \right) + 925.3 \quad \left( English \right)$$

$$\tau_{max} = \left( 7.64 \times 10^{-4} \times f_{e}^{-2} \right) - \left( 2.73 \times 10^{-2} \times f_{e}^{-1} \right) + 925.3 \quad \left( Metric \right)$$

Whenever necessary, the review provides comments or comparisons with other studies. The numerical data extracted from the experimental studies were assembled in a database.

The test parameters considered in these studies are listed in Table 2.5. The major test parameters are (a) the geometry of the beam used in the experiments, (b) beam type, (c) properties of concrete and steel reinforcement, (d) types of FRP, and (e) strengthening schemes. As seen from Table 2.5, most of these studies have focused on rectangular beams, although most RC bridge girders have a T-section with integrated deck slabs. The shape of the cross section is related also to the strengthening scheme. For example, rectangular beams are commonly strengthened by fully wrapping the member, an impractical solution for T-beams due to the presence of the flange. Therefore, more focus should be placed on T-beams

with U-wrap and side-bonding configurations as well as on the use of mechanical anchorage systems to address the issue of debonding. Also, few tests have been conducted on members with spans comparable to those used for bridges, and fewer tests have investigated the influence of scale (i.e., model-scale versus large-scale) on the shear behavior of members strengthened with FRPs. Furthermore, because FRP is generally used to strengthen damaged structures, attention needs to be given to the effects of existing cracks on the behavior of the strengthened member.

The previously developed analytical models were based on the studies listed in Table 2.5, the majority of which considered only small-scale testing. Therefore, this research aimed at expanding the experimental database with results from tests on full-scale T-beams, which are more representative

<sup>\*</sup> Terms are defined in notations section.

Table 2.3. Models that account for non-uniform strain distribution in FRP.

Reference	Equations
Author (Year)	_
Chen and Teng (2003a and 2003b)	$V_{frp} = 2 \frac{f_{frp,ed}}{\gamma_{frp}} t_{frp} w_{frp} \frac{h_{frp,e} \left( \sin \beta + \cos \beta \right)}{s_{frp}}$ $f_{frp,ed} = D_{frp} \sigma_{frp,max}$ Debonding model: $D_{frp} = \frac{\int_{\omega}^{b} \sigma_{frp,e} dz}{h_{frp,e}} \sigma_{frp,max} dz = \begin{cases} \frac{2}{\pi \lambda} \frac{1 - \cos \frac{\pi}{2} \lambda}{\sin \frac{\pi}{2} \lambda} & \text{if } \lambda \leq 1 \\ 1 - \frac{\pi - 2}{\pi \lambda} & \text{if } \lambda > 1 \end{cases}$ $\sigma_{frp,max,d} = 0.315 \beta_{w} \beta_{L} \sqrt{\frac{E_{frp}}{t_{frp}}} \sqrt{f_{e}^{-}} \leq f_{frp}$ Rupture model: $D_{frp} = \frac{\int_{\zeta_{e}}^{\infty} \bar{E}_{z} dz}{h_{frp,e} \bar{E}_{z,max}} = \frac{1 + \zeta'}{2}$ $\sigma_{frp,max} = \begin{cases} 0.8 f_{frp} & \text{if } \frac{f_{frp}}{E_{frp}} \leq \varepsilon_{max} \\ 0.8 \varepsilon_{max} E_{frp} & \text{if } \frac{f_{frp}}{E_{frp}} > \varepsilon_{max} \end{cases}$ Strip spacing limitation: $s_{frp} - \frac{w_{frp}}{\sin \beta} \leq \min \begin{cases} h_{frp,e} (1 + \cot \beta) \\ 2 \\ 300 \ mm \end{cases}$
Carolin and Taljsten (2005b)	for complete wrap: $V_{f} = \eta \varepsilon_{cr} E_{f} t_{f} z \frac{\cos \theta}{\sin \alpha}$ for composite strips: $V_{f} = \eta \varepsilon_{cr} E_{f} t_{f} z \frac{b_{f}}{s_{f} \sin \beta} \frac{\cos \theta}{\sin \alpha}$ $\int_{h/2}^{h/2} \varepsilon_{f}(y) dy$ $\eta = \frac{\int_{-h/2}^{h/2} \varepsilon_{f}(y) dy}{\varepsilon_{max} h}$ $\varepsilon_{cr} = \min \begin{cases} \varepsilon_{fu} \\ \varepsilon_{bond} \cos^{2} \theta \\ \varepsilon_{c \max} \cos^{2} \theta \end{cases}$

Table 2.3. (Continued).

$$V_{frp} = 2D_{f\theta}t_{frp}W_{frp}E_{frp}\varepsilon_{f,\max}\frac{h_{frp}}{s_{frp}}$$

$$D_{f\theta} = \left(1 - \frac{\pi - 2}{\lambda_{frp}\pi}\right) \times \begin{cases} 1 & for \ \lambda \le 1.4\\ \frac{1}{1 - 0.2(\lambda - 1.4)^2} & for \ 1.4 < \lambda < 3\\ 2.05 & for \ \lambda \ge 3 \end{cases}$$

$$\varepsilon_{f,\max} = \frac{0.427\beta_{w}\sqrt[4]{f_{c}}}{\sqrt{E_{frp}}t_{frp}}$$

Table 2.4. Models derived from mechanics-based approaches.

Reference Author (Year)	Equations
Malek and Saadatmanesh (1998)	$V_{f} = ht_{p} \left[ \overline{Q_{13}} \varepsilon_{2} + \overline{Q_{23}} \varepsilon_{1} + \frac{\left( \overline{Q_{12}} \varepsilon_{2} + \overline{Q_{22}} \varepsilon_{1} \right)}{\tan(\theta_{c})} \right]$ $V_{s} = E_{s} \varepsilon_{y} A_{v} \frac{h_{v}}{\tan(\theta_{c}) s}  for  \varepsilon_{y} < \frac{F_{y}}{E_{s}}$ $V_{s} = F_{y} A_{v} \frac{h_{v}}{\tan(\theta_{c}) s}  for  \varepsilon_{y} \ge \frac{F_{y}}{E_{s}}$
Deniaud and Cheng (2001, 2004)	Discrete formulation: $V_{r} = 0.25k^{2}f_{c}\left(A_{cf} \tan \theta_{f} + A_{cw} \tan \theta_{w}\right) + T_{v}n_{s} + T_{FRP}$ Continuous formulation: $V_{r} = k\sqrt{f_{c}A_{c}\left(T_{v} + T_{FRP}\right)\frac{d_{s}}{s}} - T_{v}$ $k = 2.1\left(f_{c}^{'}\right)^{-0.4}$ $T_{v} = A_{v}f_{vy}$ $T_{FRP} = d_{FRP}tE_{frp}\varepsilon_{max}R_{L}\left(\frac{w_{frp}}{s_{fp}}\right)^{2}\left(\frac{\sin\alpha}{\tan\theta_{w}} + (n_{s} + 1)\cos\alpha\right)\sin\alpha$ $T_{FRP} = d_{FRP}tE_{frp}\varepsilon_{max}R_{L}\left(\frac{w_{frp}}{s_{fp}}\right)^{2}\left(\frac{s}{d_{s}}\sin\alpha + \cos\alpha\right)\sin\alpha$ Maximum allowable strain in FRP: $\varepsilon_{max} = \frac{3\sqrt{f_{c}}d_{FRP}^{0.16}}{\left(tE_{frp}\right)^{0.67}\left(k_{a}\sin\alpha\right)^{0.1}}(\%) \le \varepsilon_{ultFRP}$ Remaining bonded width over initial width ratio: $R_{L} = 1 - 1.2\exp\left[-\left(\frac{d_{FRP}}{k_{e}L_{eff}}\sin\alpha\right)^{0.4}\right]$

(continued on next page)

<sup>\*</sup> Terms are defined in notations section.

### Table 2.4. (Continued).

	City has disco
Monti and Liotta (2005)	Side bonding: $V_{Rd,f} = \frac{1}{\gamma_{Rd}} \cdot \min\left\{0.9d, h_w\right\} \cdot f_{fed} \cdot 2t_f \cdot \frac{\sin\beta}{\sin\theta} \cdot \frac{w_f}{p_f}$ design effective stress for side bonding: $f_{fed} = f_{fidd} \cdot \frac{z_{rid,eq}}{\min\{0.9d, h_w\}} \cdot \left[1 - 0.6\sqrt{\frac{l_{eq}}{z_{rid,eq}}}\right]^2$ $z_{rid,eq} = \min\left\{0.9d, h_w\right\} - \left(l_e - \frac{s_f}{f_{fidd}/E_f}\right) \sin\beta$ U-wrap or complete wrapping: $V_{Rd,f} = \frac{1}{\gamma_{Rd}} \cdot 0.9d \cdot f_{fed} \cdot 2t_f \cdot (\cot\theta + \cot\beta) \cdot \frac{w_f}{p_f}$ design effective stress for U-wrapping: $f_{fed} = f_{fidd} \cdot \left[1 - \frac{1}{3} \frac{l_e \sin\beta}{\min\{0.9d, h_w\}}\right]$ design effective stress for complete wrapping: $f_{fed} = f_{fidd} \cdot \left[1 - \frac{1}{6} \frac{l_e \sin\beta}{\min\{0.9d, h_w\}}\right] + \frac{1}{2} \left(\phi_R f_{fid} - f_{fidd}\right) \cdot \left[1 - \frac{l_e \sin\beta}{\min\{0.9d, h_w\}}\right]$ $l_e = \sqrt{\frac{E_f t_f}{2f_{cm}}}  \text{where:}  f_{cm} = 0.27R_{ck}^{2/3}$ $f_{fidd} = \frac{0.80}{\gamma_{f,d}} \sqrt{\frac{2E_f \Gamma_{fk}}{t_f}}$ where: $\Gamma_{Fk} = 0.03k_b \sqrt{f_{ck} f_{cm}} \qquad k_b = \sqrt{\frac{2 - w_f/p_f}{1 + w_f/400}} \ge 1$ $w_f \le \min(0.9d, h_w) \sin(\theta + \beta)/\sin\theta$ $f_{fidd}(l_b) = f_{fidd} \frac{l_b}{l_e} \left(2 - \frac{l_b}{l_e}\right)  \text{(for } l_b < l_e)}$ $\phi_R = 0.2 + 1.6 \frac{r_e}{b_w}  \text{where:}  0 \le \frac{r_e}{b_w} \le 0.5$
Sim et al. (2005)	$\frac{\tau}{v\sigma_{cu}} = \frac{\sqrt{a^2 + d^2} - (1 - 2\phi)a}{2d}  \text{if}  \phi < \frac{\sqrt{(a^2 + d^2)} - a}{2\sqrt{(a^2 + d^2)}}$ $\frac{\tau}{v\sigma_{cu}} = \sqrt{\phi(1 - \phi)}  \text{if}  \frac{\sqrt{(a^2 + d^2)} - a}{2\sqrt{(a^2 + d^2)}} \le \phi \le \frac{1}{2}$ $\frac{\tau}{v\sigma_{cu}} = \frac{1}{2}  \text{if}  \phi > \frac{1}{2}$ $\tau = \frac{V}{b \cdot h}  \text{and}  \phi = \frac{A_v \cdot f_{sy}}{b \cdot e \cdot v\sigma_{cu}} + \alpha \left(\frac{A_p \cdot f_{py}}{b \cdot t \cdot v\sigma_{cu}} (\sin \beta + \cos \beta)\right)$

<sup>\*</sup> Terms are defined in notations section.

Table 2.5. Summary of experimental studies.

											Pro	pertie	es and	Parar	neters									
				Properties and Parameters  Concrete Type of																				
		ests		Geometry					Type of Beam				and Steel			FRP	-	Strengthening Scheme						
		of Te	lon				50											gu						
		Number of Tests	Rectangular Section	on	Beam Spanning L<7 ft	Beam Spanning 7 ft <l<13 ft<="" td=""><td>Beam Spanning L&gt;13 ft</td><td>Regular Beams (a/d&gt;2.5)</td><td>ams</td><td>fect</td><td>ing</td><td>Concrete Strength</td><td>Longitudinal Reinforcement</td><td>Transverse Reinforcement</td><td>п</td><td>p</td><td></td><td>Two-Side Bonding</td><td>dı</td><td>Complete Wrap</td><td>sno</td><td></td><td>ong.</td><td>Angle to Long. Axis≠90 º</td></l<13>	Beam Spanning L>13 ft	Regular Beams (a/d>2.5)	ams	fect	ing	Concrete Strength	Longitudinal Reinforcement	Transverse Reinforcement	п	p		Two-Side Bonding	dı	Complete Wrap	sno		ong.	Angle to Long. Axis≠90 º
		Nun	ular	T-Section	am Spann L<7 ft	Spa <l<< td=""><td>am Spann L&gt;13 ft</td><td>gular Bea (a/d&gt;2.5)</td><td>Deep Beams</td><td>Scale Effect</td><td>Precracking</td><td>te Sı</td><td>gitud</td><td>Transverse einforcemer</td><td>Carbon</td><td>Aramid</td><td>Glass</td><td>de B</td><td>U-Wrap</td><td>lete</td><td>Continuous</td><td>Strips</td><td>to I is=9</td><td>to I e≠si</td></l<<>	am Spann L>13 ft	gular Bea (a/d>2.5)	Deep Beams	Scale Effect	Precracking	te Sı	gitud	Transverse einforcemer	Carbon	Aramid	Glass	de B	U-Wrap	lete	Continuous	Strips	to I is=9	to I e≠si
			tang	Ţ.	eam	eam 7 ft	eam	tegu] (a/	Dee	Scal	Prec	ncre	Longitudinal Reinforcemen	Tra einf	C	A		'o-Si	Ü	omp	Cor	<b>0</b> 1	Ax	Ax
Author	Year		Rec		m m	m B	В	Υ.				ŭ	ŀ	1				Τw					ł .	7
Berset	1992	2																						
Uji	1992	4																						
Al-Sulaimani et al.	1994	4																						
Ohuchi et al.	1994	13																						
Chajes et al.	1995	5																		Щ				
Sato et al.	1996	3																						Щ
Araki et al.	1997	8																						
Funakawa et al.	1997	3																						
Kamiharako et al.	1997	1																						
Miyauchi et al.	1997	4																						
Sato et al.	1997	2																		П				
Taerwe et al.	1997	3																						
Taljsten	1997	3																						
Umezu et al.	1997	15																						
Chaallal et al.	1998	2																						
Mitsui et al.	1998	6																						
Triantafillou	1998	9																		Ш				
Khalifa et al.	1999	6																						Ш
Kachlakev and Barnes	1999	3																						
Khalifa et al.	2000	4																						
Deniaud and Cheng	2001	5																						
Li et al.	2001a																							
Li et al.	2001b	-																						
Park et al.	2001	2																						
Chaallal et al.	2002	10																Ш		Ц				Щ
Khalifa and Nanni	2002	4																						
Li et al.	2002	9																						
Micelli et al.	2002	10																		Ш				
Pellegrino and Modena	2002	9																						
Beber	2003	28																						
Diagana et al.	2003	8																						
Hsu et al.	2003	3																						

(continued on next page)

Table 2.5. (Continued).

			Properties and Parameters																					
												C	oncre	te	Т	ype o	f							
		Tests		Geometry					Type of Beam				and Steel			FRP	Strengthening Scheme							
Author	Year	Number of Tests	Rectangular Section	T-Section	Beam Spanning L<7 ft	Beam Spanning 7 ft <l<13 ft<="" td=""><td>Beam Spanning L&gt;13 ft</td><td>Regular Beams (a/d&gt;2.5)</td><td>Deep Beams</td><td>Scale Effect</td><td>Precracking</td><td>Concrete Strength</td><td>Longitudinal Reinforcement</td><td>Transverse Reinforcement</td><td>Carbon</td><td>Aramid</td><td>Glass</td><td>Two-Side Bonding</td><td>U-Wrap</td><td>Complete Wrap</td><td>Continuous</td><td>Strips</td><td>Angle to Long. Axis=<math>90^{9}</math></td><td>Angle to Long. Axis≠90 º</td></l<13>	Beam Spanning L>13 ft	Regular Beams (a/d>2.5)	Deep Beams	Scale Effect	Precracking	Concrete Strength	Longitudinal Reinforcement	Transverse Reinforcement	Carbon	Aramid	Glass	Two-Side Bonding	U-Wrap	Complete Wrap	Continuous	Strips	Angle to Long. Axis= $90^{9}$	Angle to Long. Axis≠90 º
Taljsten	2003	6																						
Adhikary et al.	2004	8																						
Xue Song et al.	2004	12																						
Cao et al.	2005	10																						
Carolin and Taljsten	2005a	18																						
Miyajima et al.	2005	4																						
Monti and Liotta	2005	16																						
Sim et al.	2005	9																						
Zhang and Hsu	2005	10																						
Barros and Dias	2006	5																						
Bousselham and Chaallal	2006a	20																						
Pellegrino and Modena	2006	8																						
Lees and Kesse	2007	8																						
Leung et al.	2007	12																						
Alrousan et al.	2009	4																						
Arteaga et al.	2009	15																						
Gamino et al.	2009	7																		Щ				
Rizzo and De Lorenzis	2009	1																						

Note: (1) Shaded cells denote considered parameters.

(2) Control specimens without FRP strengthening are not included in the table.

of bridge girders and consider the effects of other parameters such as pre-cracking and the amount of transverse reinforcement.

# 2.4.2 Bond Behavior of FRP-Concrete Interface

The performance of shear strengthening of concrete girders by using externally bonded FRP sheets depends on the interface bond behavior between the FRP sheets and the concrete substrates. Many analytical models attempted to con-

sider the bond characteristics at the interface between FRP and concrete substrate to predict the shear contribution of FRP when the expected failure is caused by debonding of FRP. Consideration of the bond mechanism, the intermediate crack (IC) debonding, the bond stress-slip relationship, the effective bond length, and the bond strength is required for the development of improved shear design equations.

The most important role of the interface bond between the FRP sheets and concrete is to transfer shear stresses from existing concrete structures to externally bonded FRP sheets for both shear and flexural strengthening. The bond properties

of FRP sheet-concrete interfaces have been widely studied. Various test methods have been developed to evaluate the average interfacial bond strength. These methods include single-lap-type, double-lap-type, bending-type, and inserted-type tests, as shown in Figure 2.1. Among the interface parameters evaluated are average shear bond strength, effective bond length, maximum shear bond stress, interfacial fracture energy,

and the local bond stress-slip relationship. Bond behavior is influenced by the mechanical and physical properties of the concrete, FRP composite, and adhesive; the influencing factors are listed in Table 2.6.

In evaluating FRP-concrete interface bond behavior, the bond stress-slip ( $\tau$ -s) relationship is the most important factor. For FRP sheets bonded to concrete, this relationship

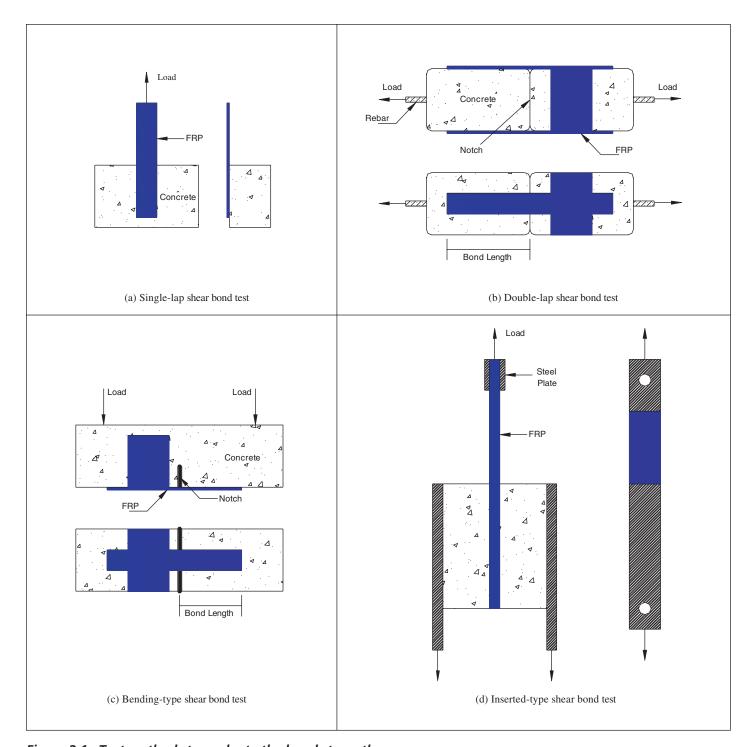


Figure 2.1. Test methods to evaluate the bond strength.

	Elements	Influencing Factor				
Concrete		Modulus of elasticity, thickness, surface condition, strength, drying shrinkage, wate content				
EDD	Continuous Fiber Sheet	Modulus of elasticity, strength, thickness, stiffness, length/width of sheet, weave				
FRP application	Bonding Resin	Modulus of elasticity, strength, glass				
аррисаціон	Primer	transition temperature, spread				
	Putty	ī · ī				
Loading condition		Bending, shearing, punching, cyclic				
Environmental actions		Ambient temperature, moisture, sun light				

Table 2.6. Factors influencing the bond behavior at FRP-concrete interface.

is determined by the strain distributions in the FRP, and the local bond stresses measured in the FRP sheets. Several empirical  $\tau$ -s relationships have been proposed including a elasto-plastic model (Sato et al., 1997 and De Lorenzis et al., 2001); a bilinear model based on interfacial fracture energy (Yoshizawa et al., 2000); a model based on the Popovic's expression (Nakaba et al., 2001); and a shear softening model (Sato et al., 2000).

The experimental studies have shown that the bond shear stress at the FRP-to-concrete interface increases rapidly with increases in the interfacial slip until it reaches the peak stress (bond strength) as illustrated in Figure 2.2. After this point, interfacial softening (or micro-cracking) starts, together with a decrease in the interfacial shear stress and an increase in the interfacial slip.

There is no agreement among researchers on the shape of the model, however, use of fracture mechanics implicitly leads to a very simple generic expression that considers only the FRP stiffness and interfacial fracture energy (defined as the area beneath the bond stress-slip curve) for the determination of bond capacity. Debonding occurs first within the effective bond length (defined as a length over which the majority of the bond stress is maintained, see Figure 2.3) as a result of debonding of a very thin layer of concrete rather than debonding at the FRP/concrete interfaces. When the bonded length of FRP along the FRP-concrete interface

exceeds the effective bond length, no further increase in failure load can be achieved. However, a longer bond length may delay complete debonding and thus improve the ductility.

Several studies have been performed to determine effective bond length. Figure 2.4 shows the effective bond lengths calculated by analytical models and equations stipulated in many current code and design guidelines versus the rigidity of FRP reinforcement ( $E_f \rho_f$ ). As shown in the figure, most studies have reported that effective bond length increases as the stiffness of FRP sheets increases. However, two studies (Maeda et al., 1997 and ACI 440.2R-08) show a different trend, probably because these models were derived using a very limited experimental database.

The analytical models for effective bond length and bond strength were derived based on small-scale tests; the bond behavior of full-size beams may be different than that prescribed by these models. Thus, full-scale tests would provide data to calibrate/improve these models.

### 2.4.3 Anchorage Systems to Enhance the Effectiveness of FRP Strengthening Systems

When a proper anchorage system is not provided, failure of FRP-strengthened reinforced concrete members is commonly manifested by debonding of the FRP. Therefore, vari-

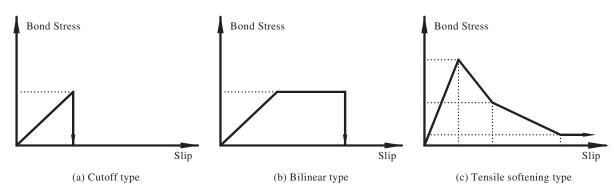


Figure 2.2. Various bond stress-slip models.

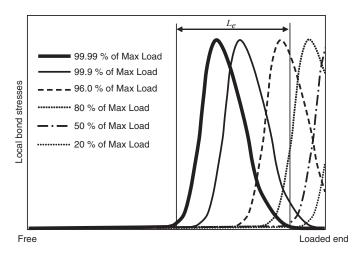


Figure 2.3. Concept of effective bond length based on stress distribution (Ueda and Dai, 2005).

ous types of anchorage systems, including the near surface mounted system (NSM), fiber reinforced polymer anchor spikes, additional horizontal strips, and various mechanical anchorage systems have been studied to evaluate their effect on FRP failure by debonding.

Many experimental studies have demonstrated the effectiveness of the NSM system (Khalifa and Nanni, 2000; De Lorenzis, 2002; Micelli et al., 2002). In this system, a bent portion of the end (or a region near the end) of the FRP reinforcement is embedded into the concrete, as shown in Figure 2.5. For fiber sheets, the bend is created during wet lay-up, and in the case of laminates, it is pre-formed. This

technique requires no surface preparation work but considerable labor for cutting the grooves.

Another system used to prevent debonding of FRP is anchor spikes (Eshwar et al., 2003; Eshwar et al., 2008; Orton, 2007; Niemitz, 2008). Each anchor spike consists of a precured fiber portion and a dry fiber portion (see Figure 2.6). The anchor spikes may be constructed in situ. First, fibers are bundled together, and half of the fiber length is covered with plastic or duct tape. The uncovered bundled fibers are then impregnated and thoroughly saturated with resin. Finally, the saturated fibers are passed through a circular hole in a steel plate, or die, to obtain the desired diameter of the anchor spikes. The dry fibers are used for bonding purposes and trimmed to the appropriate length according to specific requirements. Following surface preparation of the concrete, holes of the desired diameter and depth are drilled and partially filled with saturant. The laminate is then applied, and while it is wet, the precured portion of each spike anchor is inserted into the holes. The dry fibers are spread around the layer in a circular fashion, and a layer of saturant is then applied (see Figure 2.6).

An additional horizontal FRP strip applied on top of the vertical FRP strips has also been used as an anchorage system (Hutchinson and Rizkalla, 1999; Schnerch, 2001). This technique is very easy to install and requires no more labor than other anchorage systems. However, different levels of effectiveness have been reported. Schnerch (2001) reported that the horizontal strip neither delays nor prevents debonding, and it does not increase the contribution of the FRP to the shear strength of the beam at failure. Test results reported by Hutchinson

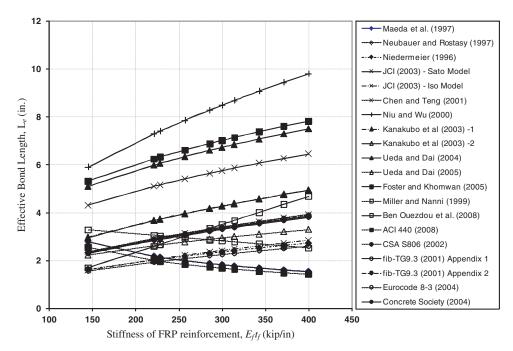


Figure 2.4. Effective bond length versus FRP rigidity.

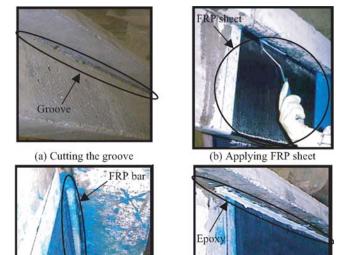


Figure 2.5. Construction of a NSM Anchorage System.

(d) Filling with epoxy

(c) Inserting an FRP bar

and Rizkalla (1999) indicated that using the horizontal strip increased the shear contribution of FRP by 16 percent.

Mechanical anchorage systems have been used widely to prevent premature FRP debonding. Steel angles, steel or FRP composite plates, and anchor bolts are examples of most commonly used mechanical anchorage systems.

Sato et al. (1997) conducted a series of tests using various anchoring methods to develop a shear strengthening technique for beams and a method of estimating their effectiveness. The test results showed that sufficient strength can be achieved only if the CFRP sheets are mechanically anchored.

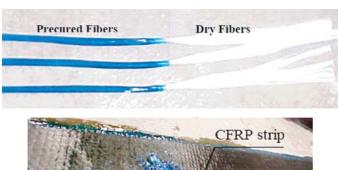




Figure 2.6. Anchor spikes.

in Figure 2.7 are (a) nail type, (b) semi-closed type, (c) subvariation of semi-closed type, and (d) closed type. Sato et al. (1997) concluded that the shear strength of beams can be improved by transverse wrapping of FRP sheets if adequate anchoring is provided by steel plates and bolts and

The four methods used to anchor the FRP sheets as shown

recommended the use of long anchor bolts that penetrate the full web. This anchorage system, however, creates stress concentrations where the anchors are placed, and the bolts lead to discontinuity of the FRP system.

Matthys (2000) conducted a project to strengthen four continuous reinforced concrete beams in shear and flexure, by supporting them with masonry columns. Bond/anchorage tests indicated a 44% increase in anchorage capacity with the use of steel bolted connections. Mechanical anchorage resulted in a less brittle failure mode due to the transition to an external tensioning system after debonding and to increased displacements resulting from CFRP slip.

Schuman (2004) conducted a comprehensive study on anchorage systems for shear strengthening of reinforced concrete (RC) beams. A mechanical anchorage system was applied to increase the shear contribution of CFRP systems by embedding anchor rods into the cross section with various bearing plates, (e.g., GFRP plate). The anchorage systems are possible, the four methods described by Schuman (2004) can be summarized as (1) complete wrapping through the flange (called complete wrap), (2) FRP laminate extended into the flange, (3) bonded steel anchors with bearing plates (called two-side bonding), and (4) GFRP plate anchors.

The two particularly important conclusions from Schuman's (2004) research are (1) the FRP composite alone provides the T-beam with little additional ultimate load and displacement capacity and creates a more brittle failure mode and (2) the use of properly embedded and sized anchors allows the vertical ties to remain intact during failure. These anchors then force a more ductile compression zone and ensure a shear/flexural failure mode.

Schuman (2004) also concluded that short anchors (Figure 2.8) lead to an increase in load carrying and displacement capacity and cause the CFRP reinforcement to be activated before the steel reinforcement yields but deeper anchors (Figure 2.8) allow the CFRP reinforcement to be activated earlier, thus delaying yielding in the steel stirrups.

For all mechanical anchorage systems configurations, the embedment length, diameter of the anchor, and the bearing strength of the plate are primary considerations. Regarding embedment length, longer anchors are more effective, but they increase the amount of labor required and present the risk of damaging the concrete and steel reinforcement. The diameter of the anchor must be chosen based on the failure modes of the connection (e.g., bearing of the plate, spalling of concrete, and yielding or rupture of the anchor).

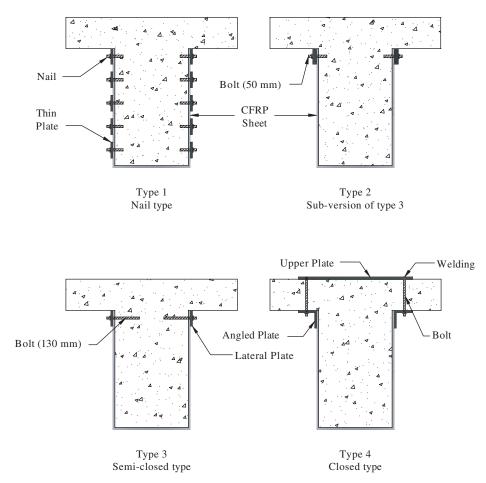


Figure 2.7. Anchoring methods of CFRP sheets.

### 2.5 Current Codes/Guidelines/ Specifications

Design procedures for shear strengthening of concrete structures with externally bonded FRP are available in various forms (e.g., codes, guidelines, and specifications).

The Guide for the Design and Construction of Externally Bonded FRP Systems for Strengthening Concrete Structures (ACI 440, 2008) was developed based on ACI 318-08 (ACI 318, 2008). This guide determines the shear contribution of exter-

nally bonded FRP based on failure modes. FRP rupture is the likely mode of failure for complete wrapping applications and the ultimate strain of the FRP can be used for calculation of the shear contribution of FRP, with the use of a strength reduction factor of 0.75. However, the ultimate strain is limited to 0.004 in order to maintain aggregate interlock. For U-wrap and side bonding applications, both FRP debonding and rupture are potential failure modes, and the shear contribution of the FRP should be investigated for each failure mode with the lesser value used for design. The analytical

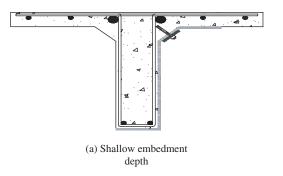
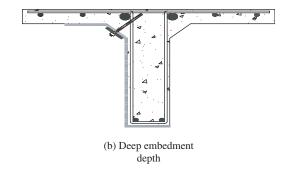


Figure 2.8. Specimen details (Schuman 2004).



model proposed by Khalifa et al. (1998) is adopted to predict the shear contribution of FRP for debonding of FRP.

The Canadian Design and Construction of Building Composites with Fiber Reinforced Polymers (CAN/CSA S806, 2002) is a design code that addresses externally bonded FRP reinforcement for concrete. The equations in this code are based on the simplified method for shear design used in the concrete design code (CAN/CSA A23.3, 1994), which is limited to the usual cases of shear reinforcement (including FRP) perpendicular to the longitudinal axis of beams. The shear contribution of the FRP is determined based on failure modes. The ultimate strain is limited to 0.004 for failure due to FRP rupture and 0.002 for bond critical applications.

The Canadian Highway Bridge Design Code (CAN/CSA S6-06, 2006) deals with the shear strengthening of concrete with externally-bonded FRPs. This code specifies that the FRP shear strengthening system should consist of U-wraps anchored in the compression zone or complete wrapping of the cross-section. This code specifies the same equations contained in ACI 440 (2002).

European fib bulletin 14 Design and Use of Externally Bonded Fiber Polymer Reinforcements (FRP EBR) for Reinforced Concrete Structures, (fib-TG9.3 2001) is a combination of guidelines and state-of-the-art reports and calculates the FRP contribution to shear capacity ( $V_{fd}$ ) according to a model proposed by Triantafillou and Antonopoulos (2000), and the bulletin recognizes the difference in expected performance between FRP material types as well as between preformed and wet lay-up FRP systems, which is expressed in the form of various material safety factors. Delamination and debonding are addressed using a simplified bilinear bond model and by considering the effects of the loss of composite action between the FRP and concrete substrate. Durability is discussed but no design guidelines are provided.

Japan Society of Civil Engineering Recommendations for Upgrading of Concrete Structures with Use of Continuous Fiber Sheets (JSCE, 2001) employs a performance-based approach to the design of externally bonded FRP materials. In addition to verifying flexural and shear capacity, flexural crack width and protection of the concrete substrate from chloride ion penetration are also considered.

The Manual for Strengthening Reinforced Concrete Structures with Externally-Bonded Fiber Reinforced Polymers, prepared by the Canadian Intelligent Society of Innovative Structures (ISIS, 2001), provides guidance and design examples for the use of externally bonded FRP based on Canadian Codes (CAN/CSA S6-06, 2006 and CAN/CSA S806-02, 2002).

The British Concrete Society Technical Report 55, Design Guidelines on Strengthening Concrete Structures Using Fiber Composite Materials (Concrete Society, 2004) is similar to fib-Bulletin 14 (fib-TG9.3, 2001) in approach and scope; how-

ever, it addresses construction issues associated with the use of externally bonded FRP materials. Externally bonded FRP strips are treated using a 45-degree truss analogy. The strain in the FRP is limited to one half of the ultimate design strain for FRP rupture failure. For debonding failure, this report adopts an equation proposed by Neubauer and Rostasy (1997); the strain is limited to 0.004 for all cases.

# 2.6 Factors Affecting the Design of FRP Shear Strengthening

The factors affecting the design of FRP shear strengthening systems was investigated by (1) reviewing existing experimental databases, (2) conducting an experimental program to investigate the factors that had not been considered in prior research, and (3) performing an analysis using finite element method (FEM) to verify the experimental results.

# 2.6.1 Investigation on the Existing Experimental Database

A total of 49 published experimental studies containing more than 500 test results were reviewed. These studies covered all relevant, detailed and specific data from tests related to FRP shear strengthening (see Table 2.5). These data were examined for appropriateness and validity by reviewing the test set-up, failure modes reported, and material properties. The data was then compiled into a tabular format to facilitate identification of the parameters that influence design of externally bonded FRP systems. These data were also used to (1) develop an experimental program to be carried out as part of this project and (2) develop and calibrate shear design provisions for concrete girders retrofitted with externally bonded FRP. The following parameters and criteria were successively subjected to qualitative and quantitative analysis: (a) mechanical and geometric properties of the FRP, (b) transverse steel ratio, (c) longitudinal steel ratio, (d) shear span-to-depth ratio or type of beams (slender versus deep), and (e) scale factor or size effect of the specimens. Other parameters and criteria that were also qualitatively examined included the effects of (a) concrete strength, (b) fatigue, (c) anchorage details, (d) pre-cracking, and (e) prestress.

The effects of failure modes were also considered because the analysis was performed by discretization of the various failure modes. The failure modes considered were (a) shear failure due to debonding, including delamination and (b) shear failure due to rupture of the FRP. Other shear failure modes (due to diagonal concrete crushing or concrete splitting) were not considered in the analyses. Results of tests in which test beams failed in flexure were disregarded.

### 2.6.1.1 Influence of FRP Properties

Table 2.5 indicates that CFRP sheets have been used in almost all studies addressing performance of RC beams strengthened in shear with FRP. The effective strain concept was used to evaluate the effectiveness of FRP shear strengthening systems. Figure 2.9 shows the variation of the effective FRP strain ( $\varepsilon_{fe}$ ) versus ( $E_f \rho_f / f_c^{'2/3}$ ) a function of FRP rigidity ( $E_f \rho_f$ ) and the compressive strength of concrete ( $f_c$ ). The effective FRP strain ( $\varepsilon_{fe}$ ) was determined based on the traditional truss analogy using the following expression:

$$\varepsilon_{fe} = V_f / (b_w d_f E_f \rho_f (1 + \cot \beta))$$
 (Eq. 2.1)

where:  $b_w$  = the width of the web

 $d_f$  = the effective depth of FRP reinforcement

 $\beta$  = the angle of inclination of the FRP with respect to the longitudinal axis of the beam.

The term  $(E_f \rho_f / f_c^{'2/3})$  was used because it includes the effects of (1) the amount of FRP expressed in terms of the FRP ratio  $(\rho_f = A_f / (b_w s_f))$ , (2) the fiber type expressed in terms of the modulus of elasticity of FRP  $(E_f)$ , and (3) the compressive strength of concrete  $(f_c)$  which is a major factor influencing the bond performance of FRP strengthening. The term  $(E_f \rho_f / f_c^{'2/3})$  is particularly important for evaluating the contribution of FRP to shear resistance, as it was established in the European design guidelines (fib-TG 9.3, 2001). It includes all the factors affecting the behavior of the materials at the FRP-concrete interface. This term is also used in many design methods to calculate the contribution of FRP to shear resistance (ACI 440.2R-08, 2008; Chen and Teng, 2001; Khalifa and Nanni, 2000; and Deniaud and Cheng, 2004).

Figure 2.9 shows that the effective FRP strain decreases as FRP stiffness increases. It also shows that beams failing by

FRP debonding are likely to exhibit smaller effective strains than beams failing by FRP rupture or other failure modes. Similar results were reported by other researchers (Bousselham and Chaallal, 2004; Khalifa and Nanni, 2000; and Triantafillou and Antonopoulos, 2000).

Figure 2.10 shows the variation in the ratio of the effective FRP strain to the ultimate FRP strain ( $R = \varepsilon_{fe}/\varepsilon_{fu}$ ) an indicator of the effectiveness of the FRP strengthening system versus  $E_f \rho_f / f_c^{\prime 2/3}$ . Figure 2.10 shows similar trends to those shown in Figure 2.9. In all cases, the effective strains are a modest fraction of the ultimate FRP strain. However, there is a high degree of scatter indicating an effect of other parameters on the shear resistance mechanism of FRP shear strengthening systems.

### 2.6.1.2 Effect of Internal Transverse Steel Reinforcement

Recent studies have shown that the contribution of externally bonded FRP to shear resistance is less for beams containing internal transverse steel than for beams without such reinforcement (Li et al., 2002; Pellegrino and Modena, 2002; Chaallal et al., 2002; Bousselham and Chaallal, 2004; and Czaderski, 2002). This interaction was observed in terms of resistance and strains (Bousselham and Chaallal, 2006a, b). This study also showed that for a given load, the stresses in transverse steel reinforcement of FRP-retrofitted beams were less than in beams that were not retrofitted.

### 2.6.1.3 Scale Effect

Although a T-section is generally used in practice, the majority of the experimental data were obtained for rectangular beams, and most tests were performed on small-scale specimens. Also, studies on the influence of the depth of an

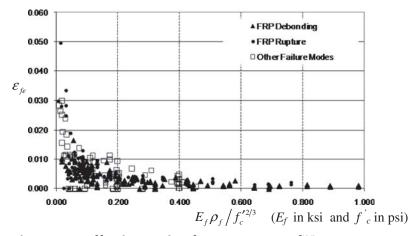


Figure 2.9. Effective strain of FRP versus  $E_f \rho_f / f_c^{-2/3}$ .

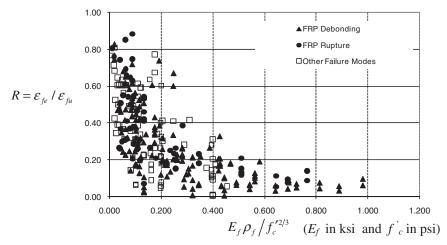


Figure 2.10.  $\varepsilon_{fe}/\varepsilon_{fu}$  versus  $E_f \rho_f / f_c^{'2/3}$ .

RC beam on its shear behavior have shown that for beams without shear reinforcement the shear resistance decreases as the beam size increases (ACI-ASCE, 1998). This scale effect is considered one of the major factors affecting shear data. For this reason, most concrete standards (except those in North America) have introduced correction factors for size to adjust for the contribution of the concrete to shear resistance. It is also desirable to determine if there is a scale effect on the results of tests on RC beams strengthened in shear with externally bonded FRP as shown in a preliminary investigation (Bousselham and Chaallal, 2004). Analysis of the test results reported in the literature on shear strengthening showed a tendency for a decrease in the gain of shear resistance due to FRP as the height of the specimen increased (Bousselham and Chaallal, 2004; Leung et al., 2007). The predictive models for the contribution of FRP to shear strength proposed in the literature are largely based on test results from small-scale testing and, therefore, may yield higher than actual strength values.

# 2.6.1.4 Effect of Shear Span-to-Depth Ratio (Slender versus Deep Beam)

The majority of the available experimental data were derived from tests on slender beams. However, the shear behavior of RC beams depends largely on the shear span-to-depth ratio [defined as the shear length (a) divided by the effective beam depth (d)]. This ratio (a/d) is used to distinguish between slender and deep beams. It is important to determine whether slender and deep beams strengthened in sheer with externally applied FRP exhibits the same shear behavior. Bousselham and Chaallal (2006b) studied the influence of the a/d ratio by considering both slender beams (a/d=3.0) and deep beams (a/d=1.5). The results of this study indicated a larger gain in shear resistance due to FRP for slender beams than for deep

beams, probably because of the arch action exhibited by deep beams. Thus, the shear contribution of externally bonded FRP is less for deep beams than for slender beams.

# 2.6.1.5 Influence of FRP Configuration and Anchorage

The frequency of each mode of failure occurrence for different FRP configurations (side bonding, U-wrap, or complete wrap), as determined from examination of the database information, is illustrated in Figure 2.11. The figure indicates that (a) debonding is the dominant mode of failure for beams strengthened with FRP and bonded on the sides only, (b) FRP debonding almost never occurs in beams retrofitted with complete FRP wrap and U-wraps with anchorage systems, and (c) failure of beams retrofitted with U-wraps occurs by debonding (65%) or by other failure modes (35%), such as diagonal tension failure in the web, shear compression failure in the compression zone, and flexural failure.

### 2.6.1.6 Influence of Concrete Strength

Concrete strength influences the performance of shear strengthening with FRP because it influences the bonding performance at the FRP-concrete interface and the failure mode. A higher concrete strength will delay, or even inhibit, failure by debonding. A low concrete strength will inhibit early crushing of concrete in the compression zone or in the diagonal struts (Bousselham and Chaallal, 2006a) but it will decrease the bond strength at the FRP-concrete interface. The guidelines for the design of RC structures strengthened with externally applied FRP take into account the concrete strength when calculating the contribution of FRP to shear resistance (ACI 440.2R, 2008; and *fib*-TG 9.3, 2001), either for the determination of the effective FRP strain or to prevent premature

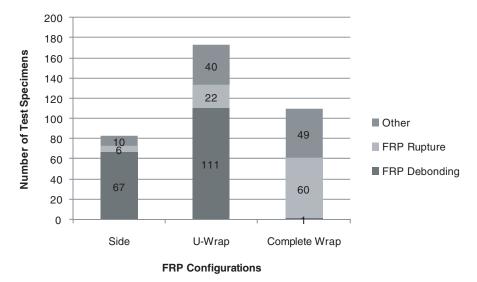


Figure 2.11. Modes of failure related to strengthening scheme.

crushing of concrete. Therefore, the range in concrete strengths used in tests should be representative of the strength prevailing in practice for existing bridge structures.

### 2.6.1.7 Influence of Fatigue

Limited research has dealt with fatigue behavior of concrete structures strengthened with externally bonded FRP laminates; most of the research have focused on flexural strengthening (Muszynski and Sierakowski, 1996; Papakonstantinou et al., 2001; Senthilnath et al., 2001; Lopez-Anido et al., 2003; Breña and Gussenhoven, 2005; Ekenel and Myers, 2005).

Williams and Higgins (2008) reported on repeated load tests conducted on three full-size girder specimens repaired with bonded carbon fiber laminate for shear strengthening and static tests conducted on two similar specimens. The specimens were 1,219 mm high with a 356 mm wide stem and a deck portion 914 mm wide by 152 mm thick. The fatigue loading resulted in localized debonding along the FRP termination locations at the stem-deck interface but did not significantly alter the ultimate shear capacity of the specimens.

Chaallal et al., (2009) tested six specimens under fatigue loading that varied between 35% and 65% of the respective static capacity of the specimen. Three of the beams had no internal shear reinforcement, and the other three had internal transverse steel reinforcement. The specimens of each group were tested with none, one, and two layers of continuously wrapped CFRP for up to 5 million cycles at a frequency of 2 Hz. However, the predicted capacities differed by as much as 50% from the measured values.

### 2.6.1.8 Influence of Pre-Cracking

Almost all reported experimental investigations that dealt with the shear performance of strengthened RC beams were

performed on beams that had not been loaded (or cracked) prior to their retrofit. However, external strengthening with FRP is often performed on pre-cracked, or slightly-damaged, structures. The few investigations carried out on RC beams that were pre-cracked prior to strengthening indicated that pre-cracking does not affect the shear performance of retrofitted beams (Czaderski, 2002; Carolin and Taljsten, 2005a, and Hassan Dirar et al., 2006).

### 2.6.1.9 Influence of Prestress

According to a *fib* report (*fib*-T.G 9.3, 2001), less than 10% of the bridges that have been strengthened with FRP are prestressed. The literature review revealed only one study dealing with PC beams strengthened in shear with FRP (Hutchinson and Rizkalla, 1999). In this study, the authors proposed shear equations based on ACI 318 (ACI 318, 1999) and reported predictions in good agreement with the test results of seven prestressed concrete beams strengthened with CFRP strips.

### 2.6.1.10 Influence of Structural Continuity

The ACI 440 Committee (ACI 440, 2008) reported that the methodology for determining the bond reduction coefficient  $\kappa_{\nu}$  described in this guide has been validated for members in regions of high shear and low moment, such as monotonically-loaded, simply supported beams. However, no reference was made to the shear response for areas subjected to a combination of high flexural and shear stresses. The literature reports on very few tests performed on continuous beams (Khalifa et al., 1999; Mitsui et al., 1998; and Miyauchi et al., 1997) but provides no information on the behavior of the web under this condition.

## 2.6.1.11 Factors Recommended for Further Investigation

Based on the review of the factors affecting the design of FRP shear strengthening, the effects of (a) internal transverse steel reinforcement, (b) scale, (c) FRP configuration and anchorage, (d) fatigue (e) pre-cracking (f) prestressing, and (g) structural continuity were selected for further investigation.

### 2.6.2 Results of Experimental Investigation

An experimental investigation was designed to address the factors and designs that affect the shear behavior of FRP strengthened girders but have not been fully investigated in earlier studies. These factors include the effects of: (1) precracking, (2) negative moments, (3) long-term conditions such as fatigue loading and corrosion of internal steel reinforcement, and (4) prestressing. The experimental program included full-scale RC T-beams and AASHTO type prestressed I-girders. The results of this experimental program, together with the existing experimental database were used to develop design equations for predicting the contribution of externally bonded FRP to shear strength.

### 2.6.2.1 RC T-Beams

The experimental program was conducted to investigate the shear performance of full-scale RC T-beams strengthened with externally bonded FRP sheets. Tests were performed on eight full-scale RC beams, seven of which were designed to provide two distinct test regions and one beam was designated for fatigue testing. Thus a total of 15 tests were performed to investigate the effects of (1) transverse steel reinforcement, (2) pre-cracking, (3) mechanical anchorage systems, (4) fiber orientations (45 and 90 relative to the longitudinal axis of the beam), (5) negative moment, (6) environmental conditioning (corrosion damage), and (7) fatigue loading.

The test beams were designed to mimic the geometry of beams used in a bridge located in Troy, New York (Hag-Elsafi et al., 2001a), that were strengthened with externally bonded FRP in 1999. This bridge is a 42-feet long by 120-feet wide RC structure consisting of 26 simply-supported T-beams spaced at 4.5 feet on center with an integral concrete deck. The bridge was built in 1932 and exhibited severe corrosion damage. The RC T-beams of the bridge have been strengthened in shear and flexure with externally bonded CFRP laminates. The cross section of the test beams is shown in Figure 2.12. The transverse reinforcement was designed to ensure shear failure prior to flexural failure and thus required the use of #3 stirrups at moderate (8 in.) and large (12 in.) spacing. Grade 40 steel (similar to that used in the Troy Bridge) was used for the transverse reinforcement. The test set-up, shown

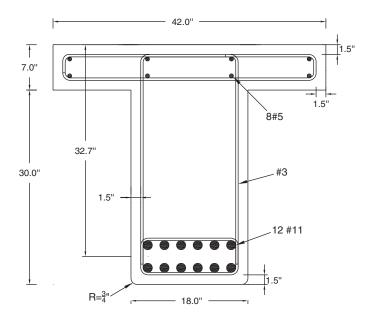


Figure 2.12. Cross-section of test beams.

in Figure 2.13, was designed to provide a shear-span-to-depth ratio of 3.3.

Table 2.3 summarizes the test results. The specimen designations indicate the stirrup spacing in inches (8 or 12), the strengthening configuration (S90 = strips at 90 to the longitudinal axis, and S45 = strips at 45 ), the presence and type of mechanical anchorage (NA = no anchorage, DMA = discontinuous mechanical anchorage, SDMA = sandwich discontinuous mechanical anchorage, and HA = additional horizontal strips), the presence of pre-existing cracks (PC), testing under negative moment conditions (HM), and fatigue loading conditions (Ftg).

The shear contributions of stirrups  $(V_s)$  and FRP  $(V_f)$  listed in Table 2.7, were determined from the measured strains in the stirrups and FRP sheets bridging the critical cracks. The shear contribution of the concrete was calculated by subtracting the contributions of the stirrups and FRP from the total shear resistance  $(V_{n,test})$ . A direct comparison of the shear strengths of the test beams could not be made because of the differences in concrete strength. Thus, the concrete strength and shear strength were normalized and listed in the table.

The test results showed that the differences in the amount of internal transverse steel reinforcement (stirrups) used in the RC-8 and RC-12-Series beams did not significantly influence the shear strength gain. However, a shear component analysis revealed an interaction between the contribution of FRP and the contribution of stirrups. Of the different anchorage systems, the sandwich discontinuous mechanical anchorage (SDMA) systems provided the best performance leading to rupture of FRP sheets. The specimens with discontinuous mechanical anchorage (DMA) systems and horizontal additional (HA) FRP strips provided higher shear strength than

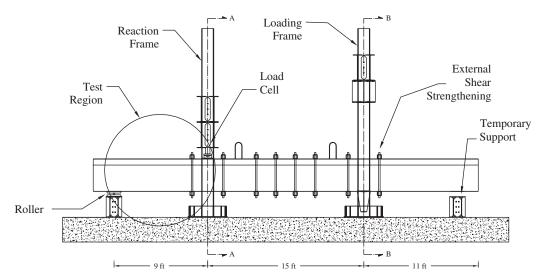


Figure 2.13. Details of test set-up.

those with no anchorage systems. The fibers oriented at 45 with respect to the longitudinal axis of the beams appeared to be more effective than those oriented at 90 . However, such orientation is less practical because of the difficulty of installation. Specimens tested under negative moment condition exhibited similar behavior to that of the specimens tested under positive moment conditions. Test results showed that beams with slight corrosion damage can be effectively repaired in shear by externally bonded FRP sheets since cracks due to corrosion do not influence the effectiveness of FRP shear strengthening. The stirrups in the beams with pre-existing

cracks yielded at a lower shear force than those in the beams without pre-existing cracks. However, the presence of pre-existing cracks did not influence the ultimate failure modes of the beams. Thus, pre-existing cracks do not seem to have a negative impact on the effectiveness of FRP shear strengthening.

The fatigue test performed in this study and other tests reported in the literature indicate that (a) if stresses in the shear stirrups are below the yield strength, the FRP strengthening can help delay the yielding and prevent fatigue failure of the girder in shear; and (b) if the stirrups have already yielded under existing service loads, it is unlikely that adding

Table 2.7. Nominal shear strength and shear gain calculations based on normalized concrete strength.

Specimen Designation	f' <sub>c</sub> (psi)	V <sub>n,test</sub> (kips)	V <sub>c</sub> (kips)	V <sub>s</sub> (kips)	V <sub>f</sub> (kips)	V <sub>n,norm</sub> (kips)	Actual Shear Gain (kips)	Shear Gain (%)
RC-8-Control	2,800	153	72	81	-	153	-	-
RC-12-Control	2,880	124	65	59	-	124	-	-
RC-8-S90-NA	3,000	191	87	64	41	189	36	23.2
RC-8-S90-DMA	3,450	212	133	56	24	199	47	30.9
RC-12-S90-NA	4,190	172	92	41	40	156	33	26.3
RC-12-S90-DMA	4,420	205	112	38	55	183	60	48.1
RC-12-S90-SDMA-PC	2,780	214	118	37	59	216	92	74.6
RC-12-S90-HA-PC	2,650	188	88	38	61	191	67	54.5
RC-12-S90-SDMA-Cor	6,180	268	98	64	106	237	113	91.1
RC-12-S45-NA	6,050	217	79	44	95	191	67	54.0
RC-12-S45-HA	3,850	181	53	41	86	174	50	40.2
RC-12-S45-SDMA	4,230	203	37	42	124	196	73	58.6
RC-12-S90-NA-HM	3,710	186	28	103	55	182	59	47.3
RC-12-S90-SDMA-HM	4,060	229	44	87	84	222	99	80.4
RC-12-S90-NA-Ftg	4,730	-	-	-	-	-	-	-

f'<sub>c</sub>: Concrete strength at the time of testing

 $V_{n,test}$  : Measured Shear Strength

V<sub>c</sub>: Shear contribution of concrete

V<sub>s</sub>: Shear contribution of stirrups

V<sub>f</sub>: Shear contribution of FRP

 $V_{n,norm}$ : Normalized Shear Strength

an FRP strengthening system will reduce stresses considerably, but it would help contain the stresses and prevent catastrophic failure of the girder.

Therefore, it is important to consider shear strengthening of a concrete girder using FRP within an overall strengthening plan that also considers the flexural capacity. Strengthening a girder that is deficient in shear may be required to raise the shear resistance to an acceptable level without the need to increase flexural capacity. In addition, limiting the stress in the

stirrups to the yield strength will eliminate that fatigue failure of the girder in shear.

### 2.6.2.2 PC Girders

Tests were conducted on full-scale AASHTO type PC girders to investigate the effects of FRP shear strengthening. Table 2.8 lists the test parameters for the PC girders. The parameters investigated included (a) size of test girders (Type 4 and

Table 2.8. PC girder test parameters.

	Girder	Test I.D.	Test Parameters							
MoDOT Standard			Cross-Section Type	Pre-Existing Cracks	Strengthening Scheme	Anchorage Type	Steel Shear Reinforcement	FRP Shear Reinforcement	Shear Span (ft)	Shear Span- to-Depth Ratio (a/d)
Type 4	1	T4-12-Control	I	No	None	None	#3 @ 12" (ρ <sub>v</sub> = 0.0031)	$\rho_f = 0$	9	2.9
		T4-18-Control	I	No	None	None	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_f = 0$	9	2.9
	2	T4-18-S90-NA	I	No	Strips/90	None	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_{f} = 0.0014$	9	2.9
		T4-18-S90-CMA	П	No	Strips/90	Continuous CFRP Plates	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_{f} = 0.0014$	12	2.9
	3	T4-18-S90-DMA	П	No	Strips/90	Discontinuous CFRP Plates	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_{f} = 0.0014$	12	2.9
		T4-18-S45-DMA	II	No	Strips/45	Discontinuous CFRP Plates	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_{f} = 0.0010$	12	2.9
	4	T4-12-Control-Deck	II	No	None	None	#3 @ 12" (ρ <sub>v</sub> = 0.0031)	$\rho_f = 0$	12	2.9
		T4-12-S90-SDMA	II	No	Strips/90	Discontinuous Sandwich CFRP Plates	#3 @ 12" (p <sub>v</sub> = 0.0031)	$\rho_{f} = 0.0014$	12	2.9
Туре 3	5	T3-12-Control	III	No	None	None	#3 @ 12" (ρ <sub>v</sub> = 0.0031)	$\rho_f = 0$	12	3.4
		T3-12-S90-NA	III	No	Strips/90	None	#3 @ 12" (ρ <sub>v</sub> = 0.0031)	$\rho_{f} = 0.0014$	12	3.4
	6	T3-12-S90-NA-PC	III	Yes	Strips/90	None	#3 @ 12" (p <sub>v</sub> = 0.0031)	$\rho_{f} = 0.0014$	12	3.4
		T3-12-S90-DMA	III	No	Strips/90	Discontinuous CFRP Plates	#3 @ 12" (ρ <sub>v</sub> = 0.0031)	$\rho_{f} = 0.0014$	12	3.4
	7	T3-18-Control	IV	No	None	None	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_f = 0$	12	3.4
		T3-18-S90-NA	IV	No	Strips/90	None	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_{f} = 0.0014$	12	3.4
	8	T3-18-S90-HS	IV	No	Strips/90	Horizontal FRP Strips	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_{f} = 0.0014$	12	3.4
		T3-18-S90-SDMA	IV	No	Strips/90	Discontinuous Sandwich CFRP Plates	#3 @ 18" (ρ <sub>v</sub> = 0.0020)	$\rho_{f} = 0.0014$	12	3.4

Type 3), (b) stiffness of top and bottom flanges (cross-sectional type), (c) effects of pre-existing damage (pre-cracking), (f) FRP strengthening scheme (fibers oriented at 90 versus 45 ), (g) types of mechanical anchorage, and (h) transverse steel reinforcement (stirrups) ratio.

All PC girders were designed with consideration for the AASHTO LRFD design guidelines (AASHTO, 2008). Girder geometry and strand patterns were based on standard I-girders used by the Missouri Department of Transportation (MoDOT). The girders were designed to fail in shear, with moderate and low levels of shear reinforcement, to investigate the influence of the transverse reinforcement on the shear behavior. Girders with the four cross-sectional designs shown in Figure 2.14 were constructed and tested.

The PC girders were tested in a three point loading configuration with each girder being designed to have two test regions: one on each end of the girder. Electric resistance strain gages, confinement bars, and longitudinal reinforcement to monitor local strains were installed on the stirrups within the test regions. Strain gages were also installed on the mechanical anchorage systems and at various locations along the FRP strips to monitor strain variation along the width and height of the FRP strips. These gages were also used to monitor the progression of delamination/debonding of the FRP. A strain rosette consisting of 21 LVDTs was anchored to the web of each test girder to measure shear strains within the test region for the purpose of determining the principal strains and their orientation. A similar system consisting of Demec gages glued to the opposite side of the web was used as a secondary measure for evaluating the principal strains and their orientations. Additional string transducers and LVDTs were also used to monitor deformations at critical points along the test girders.

The results of the PC girder testing were inconclusive as to the effectiveness of the FRP shear strengthening because of the variety of failure modes observed during the testing. In many cases, no shear gain was observed for the FRP strengthened specimens. Failure modes included (1) horizontal failure along the top flange, (2) debonding of FRP, (3) localized rupture of FRP, (4) diagonal shear tension, (5) web crushing, (6) mechanical anchorage failure, and (7) failure due to high stress concentrations localized at the reaction point. Some test specimens exhibited multiple failure modes either at the same time or in a sequential manner.

For the MoDOT Type 4 girders [Figures 2.14 (a) and (b)], shear cracks in the web propagated toward the top flange at which point they turned and ran horizontally along the longitudinal compression reinforcement located at the interface between the web and top flange. The maximum shear force carried by all MoDOT Type 4 girders was ultimately governed by a failure plane created by the horizontal cracks along the top flange (failure mode—TF). For the MoDOT Type 4 girders strengthened in shear with FRP, the horizontal top flange

failure was generally preceded by debonding of the FRP (failure mode—D). In two extreme cases, ultimate failure was accompanied by failure of the mechanical anchorage (T4-18-S90-CMA) (failure mode—MA) and localized rupture of the FRP (T4-18-S90-DMA) (failure mode—LR). For the MoDOT Type 3 girders, failure due to web crushing (failure mode— WC) or high stress concentrations near the reaction point (failure mode—SC) were observed when a moderate level of transverse steel reinforcement was provided (stirrups spaced at 12 inches). For the MoDOT Type 3 girders with low transverse steel reinforcement conditions (stirrups spaced at 18 inches), ultimate failure was always characterized by diagonal sheartension failure (failure mode—DT) preceded by some level of debonding (failure mode—D) when FRP reinforcement was present. The diminished effectiveness of the FRP shear strengthening is probably related to the thin web and stiff flange geometry of the PC girders and the adverse effect of FRP debonding when it is accompanied by peeling off of the concrete cover. In extreme cases, web crushing failure can occur, which is a failure mode that cannot benefit from FRP strengthening. The use of properly anchored FRP systems (e.g., with mechanical anchorage) will minimize the extent of debonding and improve performance.

To better understand the shear resistance mechanisms and quantify the FRP contribution to the ultimate shear capacity, it is necessary to examine the effects of the individual components contributing to the total shear resistance. The primary components contributing to the shear resistance are those provided by the concrete  $(V_c)$ , steel stirrups  $(V_s)$ , and externally bonded FRP  $(V_f)$ . A shear component analysis was conducted on the experimental data to identify the contribution of each component throughout the loading history of the test girders. The three individual components  $(V_c, V_s, \text{ and } V_f)$  were evaluated from crack-based free-body diagrams of a portion of the test girders along the critical shear cracks.  $V_s$  and  $V_f$  were determined from strain gage measurements along the stirrups and FRP strips within the test regions. Only strain measurements closest to the critical shear crack were used for such analysis.  $V_c$ was estimated as the difference between the applied shear force  $(V_n)$  and the contributions of the stirrups and FRP (i.e.,  $V_s + V_f$ ). A shear component analysis showed that externally bonded FRP provides a significant contribution to the total shear resistance of a PC girder. The results of this analysis are summarized in Table 2.9 at the stages corresponding to yielding of the steel stirrups and ultimate load.

# 2.6.3 Results of Finite Element Method (FEM) Analysis

Nonlinear finite element analyses were carried out using the commercial FE program DIANA (DIsplacement ANAlyzer) to (1) predict the behavior of the test girders prior to testing, (2) investigate the effects of additional parameters not

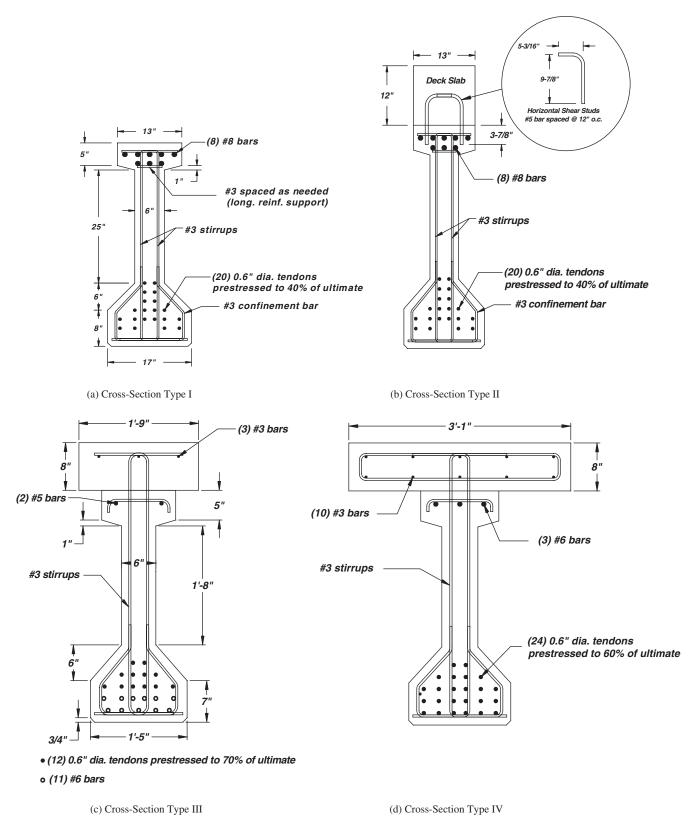


Figure 2.14. Specimen cross sections.

Table 2.9. Summary of shear contributions.

		Cross	Shear		At Yield	ing of Steel	Stirrups	At U	At Ultimate Load		
Test I.D.	f' <sub>c</sub> (psi)	Section Type	Crack Angle (deg.)	Failure Mode	V <sub>cy</sub> (kips)	V <sub>sy</sub> (kips)	V <sub>fy</sub> (kips)	V <sub>cu</sub> (kips)	V <sub>su</sub> (kips)	V <sub>fu</sub> (kips)	
T4-12-Control	9,970	I	32.0	TF	N/A	N/A	N/A	131	71	N/A	
T4-18-Control	9,930	I	26.0	TF	127	57	N/A	149	57	N/A	
T4-18-S90-NA	10,020	I	21.0	D + TF	83	43	67	83	43	67	
T4-18-S90-CMA	10,120	П	25.0	D + MA + TF	N/A	N/A	N/A	95	47	87	
T4-18-S90-DMA	10,160	П	24.0	D + LR + TF	N/A	N/A	N/A	161	39	44	
T4-18-S45-DMA	10,190	П	32.0	D + TF	N/A	N/A	N/A	144	34	77	
T4-12-Control-Deck	10,660	П	26.0	TF	142	86	N/A	159	86	N/A	
T4-12-S90-SDMA	10,330	П	30.0	TF	113	57	35	134	57	67	
T3-12-Control	8,890	III	23.0	SC	133	100	N/A	153	100	N/A	
T3-12-S90-NA	8,910	III	22.0	D + WC	120	86	23	143	90	38	
T3-12-S90-NA-PC	9,470	III	21.0	D + WC	110	86	41	115	86	39	
T3-12-S90-DMA	10,380	III	25.0	SC	N/A	N/A	N/A	158	60	31	
T3-18-Control	9,590	IV	21.0	DT	108	59	N/A	192	60	N/A	
T3-18-S90-NA	10,120	IV	15.0	D + DT	52	86	26	112	86	18	
T3-18-S90-HS	10,190	IV	26.0	D + DT	82	43	38	140	51	31	
T3-18-S90-SDMA	10,430	IV	33.0	D + DT	48	77	110	48	77	110	

considered in the experimental test program, and (3) identify the global and local behaviors of girders that were not monitored in the tests such as the interface behavior between concrete and FRP sheets. DIANA is a program with its own library of structural elements and constitutive material models and includes a user-defined option for adding specific elements and constitutive models to provide flexibility for FE modeling. Subsequently, an FE model capable of simulating the global and local behavior of the RC and PC girders strengthened with FRP in shear was developed. The progression of the FE model development was as follows: (i) Preliminary analyses, focused on the modeling aspects of the FE model, were carried out at the initial state of the FE analysis using two- and three-dimensional FE models. Another finite element program, FEAP, was used to confirm the results of DIANA; (ii) The results of the twodimensional FE analysis were used to refine the input parameters of the three-dimensional model and improve accuracy; (iii) Other modeling techniques (e.g., phase analysis, modeling of the interface region between concrete and FRP, use of different elements, and refinement of mesh size) were introduced in the developed FE models to better reflect the processes observed in the experimental girders; (iv) Because results of FE models are strongly dependent on the material models chosen for each material, several material models for concrete, steel, FRP, and interface were examined, and optimized material models were incorporated in the FE model (special consideration was given to concrete and interface models because of their inherent complex properties and effects on the shear behavior).

The results obtained from the FE models were compared to the experimental results with respect to global behavior (i.e., shear force-displacement relationships and final failure modes) and local behavior (i.e., stress and strain variations for each component). The shear force-displacement relationships obtained from the FE model showed somewhat stiffer behavior than that obtained from the tests on RC and PC girders regardless of FRP strengthening (see Figure 2.15). This phenomenon is attributed to the configuration considered in the FE model that differed from the test. For example, the FE simulation did not consider external configurations such as strengthening of the specimens with the Dywidag bars. Also, the smeared crack model used for concrete in the FE simulation does not precisely replicate the behavior of the test specimens that were mostly governed by a few primary discrete diagonal cracks. However, accurate prediction of cracking and ultimate loads, similar crack patterns, consistent ductility, and similar strain/stress variations in each component are indications of the developed FE model's efficiency.

In terms of failure strength, the average ratio of experimental shear strength to analytically evaluated shear strength of the PC girders ( $V_{exp}/V_{FE}$ ) was 1.04 with a maximum ratio of 1.22 and a minimum ratio of 0.95. The variance (VAR), standard deviation (STDEV), and coefficient of variance

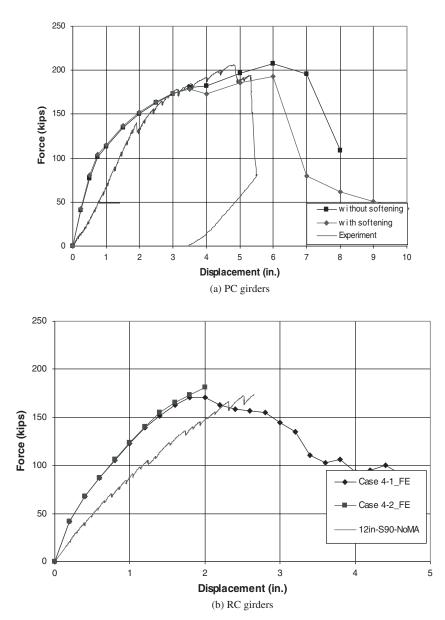


Figure 2.15. Representative shear force-displacement relationship.

(COV) are calculated as 0.01, 0.07, and 0.07, respectively. For RC girders, the average shear strength ratio was 0.98 with a maximum ratio of 1.11 and a minimum ratio of 0.90, and VAR, STDEV, and COV are calculated as 0.00, 0.07, and 0.07, respectively. The FE analyses showed a good agreement with test results for the ultimate strength suggesting that the developed FE models appropriately predict the ultimate strength of both PC and RC girders.

The FE analysis allowed investigation of local behaviors that could not be examined through experiments such as the interface behavior between concrete and FRP sheets. The FE analysis also provides the stress and strain variations for concrete, steel, FRP, and interface regions that were used to investigate each component contribution to the shear transfer mechanism. In particular, strain variations along the principal direction of FRP sheets are valuable inputs for design-

ing FRP strengthening for shear. Figure 2.16 illustrates the strain distribution determined from FE analysis along the principal direction of a critical FRP sheet for a series of increasing load stages. As shown in the figure, when the test beam reached the ultimate state (i.e., a loading state of 250 kips), the maximum strain in the FRP was only 0.0091 which is 54% of the rupture strain (0.017).

## 2.7 Performance Evaluation of Existing Design Methods

This section presents a summary of the performance evaluation conducted for existing models and relationships for Vf. Table 2.10 presents a summary of the performance of 21 different relationships (i.e., 17 models presented in research papers and four models included in code and guideline docu-

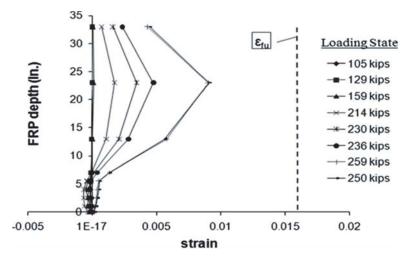


Figure 2.16. Strain variations along principal direction of critical FRP sheet.

ments) for calculating Vf based on the comparisons of the FRP contributions predicted by each model to the experimentally measured FRP contributions as reported in the database. Table 2.10 presents the average ratio of the shear strength provided by FRP reinforcement  $(V_{f,test}/V_f)$ , the COV, and the number of beams used in calculating this average for 13 segments of the experimental dataset.  $V_{f,test}$  is the experimentally measured strength of a test beam with FRP reinforcement minus the experimentally measured strength of the corresponding (control) beam without FRP reinforcement, and  $V_f$  is the strength calculated from each model. The first segment is the entire dataset of "all beams;" the second set contains only those test results considered appropriate for calibrating provisions to be used in codes of practice including the AASHTO LRFD Bridge Design Specifications (AASHTO, 2008). This action reduced the potential number of available test results from 324 to 251. These results were further separated into segments according to the Mode of Failure (MoF), the use of steel shear reinforcement (No Av or With Av), and by combinations of these two. It was apparent that within each segment, there was a large variation in the average strength ratio, and generally, the COVs are large because the models were derived to provide a best fit with a relatively small number of tests, and there is a very wide range in types and effectiveness of FRP including stiffness  $(E_f)$ , ultimate strength  $(f_{fu})$ , means of application, anchorage, orientation, and other factors. Therefore, the individual models would perform better (reasonable strength ratio and lower COV) for some segments of the test data than others. For example, the model by Khalifa et al., (1998) shows COV of 1.47 and 0.48 for members with observed rupture failures without and with steel shear reinforcement, respectively. Relationships for  $V_f$  in codes and guidelines are expected to consider a wide range of test results with a uniform average strength ratio and COV across all segments of the test data. Model (fib-TG9.3, 2001) exhibited the most uniform perform-

ance. Models 3, 9, 13, and 14 also demonstrated similar performance across a broad range in categories.

# 2.8 Suggestions for Improved Design Methods

The statistical assessment of the performance of models for  $V_f$  determined that the following five models provide the lowest COV across a wide range of segments of the database:

Model 3 (Triantafillou and Antonopoulos, 2000) Model 9 (Chen and Teng, 2003a and 2003b) Model 13, (Cao et al., 2005) Model 14, (Zhang and Hsu, 2005) Model 18 (fib-TG 9.3, 2001 and Triantafillou and Antonopoulos, 2000)

Based on the review of these models, a  $V_f$  model that includes the following features would be appropriate for incorporation into the LRFD specifications (AASHTO, 2008):

axial stiffness of FRP reinforcement ( $\rho_f E_f$ ) compressive strength of concrete ( $f_c$ ) mode of failure (debonding or rupture) type of FRP application (full wrap, side bonding, or U-wrap) development length available for FRP ( $L_e$ ) bond strength between FRP and concrete ( $\tau_{max}$ )

For use in design the  $V_f$  model must also consider the following:

1. Complexity of Relationship for Evaluation. The majority of available models for  $V_f$  are much more complex than

Table 2.10. Statistical evaluation of strength ratios  $V_{f,test}/V_{f,model}$  by test beam type.

Model Affiliation	Al-Sulaimani et al.	Chajes et al.	Triantafillou and Antonopoulos	Malek and Saadatmanesh	Khalifa et al.	Chalifa and Nanni	Hutchinson and Rizkalla	Chaallal et al.	Chen and Teng	Pellegrino and Modena	Hsu et al.	Deniaud and Cheng	Cao et al.	Zhang and Hsu	Carolin and Taljsten	Monti and Liotta	Pellegrino and Modena	fib-TG9.3	JSCE	CSA S806	ACI 440
	<u>≺ ਲ</u> 1994	1995	2000	1998	1998	2000	1999	2002	2003a,b	2002	2003	2001	2005	2005	2005b	2005	2006	2001	2001	2002	2008
Model #	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
1.) All Bea	<u> </u>		3	7		0	,	0	3	10	- ' '	12	10	14	10	10	17	10	13	20	21
Mean	0.23	1.10	0.84	0.34	1.46	1.49	1.90	1.16	1.68	3.56	1.30	8.39	0.75	1.19	1.15	1.67	0.41	1.24	0.52	1.46	1.65
COV	0.67	1.05	1.10	0.81	1.05	1.03	1.01	0.77	0.64	2.29	0.89	1.71	0.71	0.59	0.81	0.75	0.73	0.60	0.76	0.99	0.96
Num	324	324	324	324	315	317	324	324	324	244	244	324	324	324	324	324	324	317	324	324	317
2.) All "Va		_								244	244	324	324	324	324	324	324	317	324	324	317
Mean	0.25	1.23	0.98	0.38	1.53	1.57	2.10	1.18	1.83	3.24	1.39	9.30	0.78	1.30	1.25	1.84	0.44	1.35	0.57	1.61	1.78
COV	0.62	0.94		0.36	0.97	0.95	0.91		7.57	1.34		1.71		0.53	0.73			0.50		0.89	0.88
		<b>-</b>	0.56					0.60			0.89	<b>-</b>	0.57			0.66	0.67		0.66	<b>-</b>	-
Num	251	251	251	251	244	244	251	251	251	187	187	251	251	251	251	251	251	244	251	251	244
3.) "Valid"			= Ru		1.05	4.00	4.50	4.07	1 10	0.70	4.05	0.05	0.00	1.00	1.00	1.50	0.00	4 47	0.40	4.40	4.05
Mean	0.24	0.88	0.81	0.32	1.25	1.32	1.53	1.07	1.48	2.73	1.35	8.85	0.62	1.22	1.08	1.58	0.38	1.17	0.48		-
COV	0.69	0.70	0.38	0.69	0.57	0.69	0.68	0.62	0.45	1.16	0.79	1.33	0.52	0.44	0.69	0.51	0.63	0.43	0.59	0.67	
Num	126	126	126	126	125	125	126	126	126	94	94	126	126	126	126	126	126	125	126	126	125
4.) "Valid'				onding		0.07	0.70	4 40	0.00	4.05	4.00	45.70	4.04	4.04	4.05	0.04	0.50	4.50	0.70	0.00	0.00
Mean	0.22	1.60	1.19	0.49	2.14	2.07	2.73	1.43	2.23	4.85	1.92	15.70	1.01	1.64	1.65	2.31	0.56	1.58	0.73	2.09	2.36
COV	0.45	1.00	0.62	0.77	1.18	1.18	0.96	0.67	0.57	1.31	1.03	1.63	0.49	0.56	0.77	0.73	0.73	0.48	0.72	0.94	1.00
Num	61	61	61	61	58	58	61	61	61	40	40	61	61	61	61	61	61	58	61	61	58
5.) "Valid"			= Oth																		
Mean	0.30	1.55	1.12	0.37	1.51	1.62	2.63	1.18	2.12	2.91	1.05	4.08	0.89	1.15	1.23	1.89	0.42	1.52	0.58	2.00	2.10
COV	0.53	0.82	0.53	0.56	0.72	0.66	0.80	0.66	0.54	1.35	0.35	1.29	0.53	0.52	0.56	0.64	0.50	0.50	0.55	0.78	0.73
Num	64	64	64	64	61	61	64	64	64	53	53	64	64	64	64	64	64	61	64	64	61
6.) "Valid'																					
Mean	0.30	1.48	1.14	0.41	1.74	1.92	2.54	1.01	2.06	1.89	1.22	4.31	0.83	1.23	1.36	1.89	0.47	1.49	0.62	1.94	2.15
COV	0.61	1.00	0.59	0.77	1.16	1.04	0.97	0.53	0.58	1.08	0.76	1.21	0.56	0.41	0.77	0.68	0.70	0.44	0.69	0.95	0.96
Num	114	114	114	114	108	108	114	114	114	108	108	114	114	114	114	114	114	108	114	114	108
7.) "Valid'		: With																			
Mean	0.21	1.01	0.85	0.35	1.36	1.30	1.74	1.33	1.63	5.08	1.62	13.45	0.74	1.37	1.16	1.80	0.41	1.25	0.52	1.33	1.48
COV	0.54	0.71	0.44	0.67	0.58	0.62	0.68	0.70	0.51	1.13	0.96	1.49	0.56	0.59	0.67	0.64	0.63	0.53	0.61	0.67	0.62
Num	137	137	137	137	136	136	137	137	137	79	79	137	137	137	137	137	137	136	137	137	136
8.) "Valid'	Beam	s: MoF	= Del	r i	g: No /	٩v															
Mean	0.31	0.82	0.87	0.30	1.38	1.62	1.43	0.91	1.53	1.42	1.18	5.21	0.63	1.22	1.00	1.62	0.39	1.27	0.47	1.10	1.42
COV	0.71	0.77	0.40	0.73	0.65	0.74	0.75	0.47	0.49	0.65	0.52	0.77	0.57	0.40	0.73	0.55	0.71	0.42	0.60	0.75	0.67
Num	47	47	47	47	46	46	47	47	47	46	46	47	47	47	47	47	47	46	47	47	46
9.) "Valid'	Beam	s: MoF	= Ru	oture: N	No Av																
Mean	0.22	1.95	1.36	0.57	2.45	2.55	3.33	1.10	2.37	2.67	1.53	5.62	0.94	1.34	1.90	2.08	0.62	1.61	0.79	2.55	2.88
	-			0.86						1.34								0.54		_	-
Num	29	29	29	29	26	26	29	29	29	26	26	29	29	29	29	29	29	26	29	29	26
10.) "Valid																					
Mean			1.30				3.31	1.05	2.48	1.93		2.20	1.01	1.16	1.40		0.45			_	-
	0.50		0.43		0.69			0.48	0.42			0.48	0.41	0.38		0.51				0.64	0.64
Num		38	38	38	36	36	38	38	38	36	36	38	38	38	38	38	38	36	38	38	36
11.) "Valid																					
	0.19		0.77			1.14		1.16	1.44	3.99	1.52	11.02	0.61	1.22	1.12	1.56	0.38	1.11	0.48	1.22	1.31
COV	0.50	0.65		0.66	0.49	0.55	0.64	0.65	0.42	0.99	0.89	1.28	0.48	0.46		0.48	0.57	0.43	0.58	0.63	0.55
Num		79	79	79	79	79	79	79	79	48	48	79	79	79	79	79	79	79	79	79	79
12.) "Valid	d" Bear				With A	٩v															
Mean	0.22	1.28	1.03	0.43	1.89	1.68	2.19	1.72	2.11	8.91	2.64	24.84	1.07	1.91	1.42	2.51	0.51	1.56	0.66	1.68	1.94
COV	0.50	0.57	0.32	0.53	0.48	0.57	0.54	0.62	0.42	0.92	0.89	1.27	0.39	0.56	0.53	0.59	0.62	0.43	0.48	0.52	0.53
Num		32	32	32	32	32	32	32	32	14	14	32	32	32	32	32	32	32	32	32	32
13.) "Valid	d" Bear	ns: Mo	F = 0	ther: W	ith Av																
Mean	0.27	0.96	0.86	0.29	1.26	1.30	1.63	1.36	1.60	5.00	1.07	6.82	0.72	1.13	0.97	1.63	0.38	1.28	0.47	1.25	1.44
COV	0.56	0.97	0.64	0.89	0.73	0.73	0.93	0.76	0.69	1.24	0.44	1.07	0.69	0.69	0.89	0.83	0.67	0.74	0.80	0.90	0.77
Num	26	26	26	26	25	25	26	26	26	17	17	26	26	26	26	26	26	25	26	26	25

- most formulas in codes of practice and therefore, not suitable for use in practice.
- 2. Availability and Reliability of Model Parameter Data. The models proposed by most researchers require knowledge of the measurable features of the test beam and FRP application, such as the development length of the FRP reinforcement. While such requirements improve accuracy, design provisions must include items that are available or can be appropriately assumed. The parameters proposed in a V<sub>f</sub> relationship for use in the LRFD specifications should recognize that FRP shear reinforcement is most likely to be used for strengthening of an existing old structure for which full design details may not be available.
- 3. Calibration with Full Shear Strength Ratio Considering Specific  $V_c$  and  $V_s$  Relationships. A comparative evaluation of  $V_f$  models, can be conducted using the strength ratios of  $V_{f,test}/V_f$ . However, to include in a code of practice, the relationship for  $V_f$  must be calibrated based on the bias (strength ratio) and COV of the  $V_{n,test}/V_n$  ratio ( $V_n = V_c + V_s + V_f$ ).

### 2.9 Reliability Assessment

A study was conducted to assess the reliability of the proposed design equations using procedures similar to those used in the calibration of AASHTO-LRFD specifications (AASHTO, 2008). The First Order Reliability Method (FORM) was used for calculating the reliability index ( $\beta_r$ ) of 36 bridges that were designed for such purposes. These bridges covered three span lengths, interior and exterior girders, and three shear defi-

ciency levels that were strengthened with FRP shear reinforcement (i.e., a set of  $3 \times 2 \times 3 = 18$  bridges). One set used anchored FRP reinforcement where FRP rupture is the dominating mode of failure, and another set used non-anchored FRP reinforcement where debonding is to be expected. Table 2.11 lists the nominal properties of these bridges, illustrating the wide range in the ratio of FRP contribution ( $V_f$ ) to the nominal strength of the existing structure. The live-to-dead load shear demand ratio for these bridges ranges from 0.83 to 2.32.

The nominal values of the bridge properties were used to obtain random variables for each of the main parameters in the design equation. This step required knowledge of the statistical characteristics of the random variables. Some of the required information was obtained from the literature, and other information specific to this study had to be determined by estimating the random variables' bias (ratio of random variable's mean value to its nominal value) and COV (ratio of random variable's standard deviation to its mean value). For example, the statistical characteristics of the analysis model uncertainty,  $\xi_P$ , were obtained by comparing the predicted shear strength using the proposed equations to the experimentally, measured values as reported in the database. The effect of material and fabrication tolerances on the resistance model was determined using Monte Carlo simulations and some recently published data (Nowak and Szerszen, 2003). The statistical characteristics of load-related random variables were taken from NCHRP Report 368 (Nowak, 1999). Table 2.12 shows the bias and coefficient of variation for the main parameters used in the limit state function (Z) that

Table 2.11. Shear resistance components.

Bridge			$A_{\nu}d_{\nu}/s$	$W_f$	$S_f$	$t_f$	(in)	$V_c$	$V_s$	$V_f$	$V_f$		
Span Length	Girder	Case	Case	Case	$(in^2)$	(in)	,	Rupture	Debond	(kips)	(kips)	(kips)	$\overline{V_c + V_s}$
		L45F1I	L45F1I 0.847		12.0	0.00774	0.01863		50.82	33.88	0.272		
	Interior	L45F2I	0.730		10.0	0.01142	0.02749		43.79	40.91	0.349		
45 ft		L45F3I	0.613		8.0	0.01477	0.03556	73.57	36.76	47.94	0.435		
43 11		L45F1E	0.697	4.0	12.0	0.01461	0.03519	111.24	41.79	41.79	0.362		
	Exterior	L45F2E	0.532		10.0	0.02315	0.05575		31.92	51.66	0.490		
		L45F3E	0.368		8.0	0.03146	0.07576		22.05	61.53	0.643		
	Interior	L60F1I	0.696		14.0	0.00644	0.01023		41.77	41.77	0.273		
		L60F2I	0.580		12.0	0.00644	0.01402		34.78	48.76	0.334		
60 ft		L60F3I	0.463		10.0	0.00728	0.01753		27.79	55.76	0.401		
0011		L60F1E	0.565		14.0	0.01461	0.01855		33.89	50.84	0.350		
	Exterior	L60F2E	0.468		12.0	0.02315	0.02210		28.06	56.67	0.407		
		L60F3E	0.371		10.0	0.03146	0.02477		22.23	62.49	0.468		
		L75F1I	0.501		16.0	0.00596	0.00596		30.06	45.09	0.233		
	Interior	L75F2I	0.319		14.0	0.00648	0.00776		19.12	56.03	0.306		
75 ft		L75F3I	0.136		12.0	0.00664	0.01142	163.81	8.18	66.97	0.389		
		L75F1E	0.394		16.0	0.00730	0.00849	103.81	23.67	55.23	0.295		
	Exterior	L75F2E	0.214		14.0	0.00764	0.01277		12.86	66.04	0.374		
		L75F3E	0.034		12.0	0.00762	0.01734		2.05	76.85	0.463		

Random Variable	Bias	COV		
Material and Fabrication Tolerances, $\alpha_{MR}$	Varies (see Appendix)			
Analysis Model, $\xi_{P}$	FRP Rupture	1.680	0.330	
Analysis Model, $S_P$	Other	1.410	0.269	
Wearing Surface DL, $\zeta_{ws}$	1.000	0.250		
Component DL, $\zeta_{DC}$	1.050	0.100		

L=45 ft

L=60 ft

L=75 ft

Interior

Exterior

1.041

1.046

1.071

1.134

1.307

Table 2.12. Summary of bias and COV values used in calibration study.

Highway LL (including impact),  $\zeta_{\text{LL+IM}}$ 

LRFD Girder Distribution Factor,  $\eta_{GDF}$ 

accounts for variabilities and uncertainties in material and fabrication tolerances ( $\alpha_{MF}$ ), analysis model accuracy ( $\xi_p$ ), and girder distribution factors ( $\eta_{GDF}$ ) as well as the different loading types (wearing surface, dead load, and live load).

The simplified approximate expressions used in previous AASHTO calibration studies were not used because of the high COV for the analysis model, which exceed the limits of the applicability of the simplified approximated expressions. A detailed iterative FORM analysis was performed; the results

were validated using Monte Carlo simulations for one bridge. After several trials, the proposed design expression was adjusted to achieve  $\beta_r$  values close to the level targeted by most AASHTO calibration studies (i.e.,  $\beta_{r,target} = 3.50$ ).

0.180

0.180

0.180

0.157

0.239

The performance of the proposed expression is illustrated in Figure 2.17 for a range of girder span lengths and spacings. The figure shows that the reliability index is nearly the same for all girder spacings and is about 3.50 for shorter span lengths but decreases for longer span lengths.

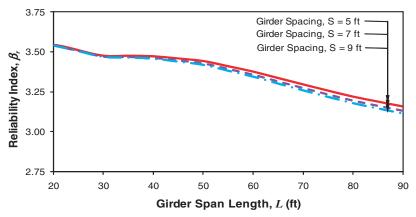


Figure 2.17. Reliability index ( $\beta_r$ ) versus span lengths for different girder spacings.

## CHAPTER 3

# **Application and Implementation**

## 3.1 Approaches for Relevant Changes to AASHTO LRFD Bridge Design Specifications

The models for  $V_f$  were selected to provide best fit empirical expressions incorporating the variables that were found to influence  $V_f$ . These models were formulated and calibrated to achieve a  $\beta_r$  value around 3.5 as characterized by the AASHTO LRFD Bridge Design Specifications (AASHTO, 2008). For the evaluation of the bias and COV of strength ratios  $V_{test}/V_n$ , it was necessary to evaluate  $V_c + V_s$ . The AASHTO LRFD Bridge Design Specifications (AASHTO, 2008) provide six different means of evaluating shear resistance, however, only the simplified procedure was selected to calibrate the model for  $V_f$  to achieve the target reliability of,  $\beta_r$ , 3.5. The simplified procedure for evaluating  $V_c$  and  $V_s$  is given by the following equations:

$$\begin{split} V_c &= 0.0316 \beta \sqrt{f_c'} \, b_\nu d_\nu \\ \text{For: } \beta &= 2 \quad V_c = 0.0632 \sqrt{f_c'} \, b_\nu d_\nu \quad (f_c' \text{in ksi}) \\ \text{or } V_c &= 2 \sqrt{f_c'} \, b_\nu d_\nu \quad (f_c' \text{in psi}) \end{split}$$

While this method is not applicable to members greater than 16 inches in depth that do not contain shear reinforcement, the relationship provided for  $V_c$  is identical to that in the General Procedure (AASHTO, 2008) which is applicable to such members when distributed horizontal reinforcement is placed on 12-in. centers, and the strain in the longitudinal reinforcement ( $\varepsilon_s$ ) is less than 0.00187. For  $\varepsilon_s = 0.00187$ :

$$\beta = \frac{4.8}{(1+750\varepsilon_s)} \frac{51}{(39+s_{xe})} = \frac{4.8}{(1+750(0.00187))} \frac{51}{(39+12)} = 2.00$$

The contribution of the steel reinforcement is given by:

$$V_{s} = \frac{A_{v} f_{y} d_{v} (\cot \theta + \cot \alpha) \sin \alpha}{s}$$
 (5.8.3.3-4)

where:  $\theta$  = the angle of diagonal compression and  $\alpha$  = the angle of the transverse reinforcement relative to the longitudinal axis of the member

If 
$$\theta = 45$$
 and  $\alpha = 90$  then:  $V_s = \frac{A_v f_y d_v}{s}$ 

The contribution of the FRP reinforcement can be evaluated using the truss model used for evaluating the contribution of the steel shear reinforcement. In this case:

$$V_f = \frac{A_f f_{fe} d_f}{s_f} (\cot \theta + \cot \alpha) \sin \alpha$$

If 
$$\theta = 45$$
 and  $\alpha = 90$  then:  $V_f = \frac{A_f f_{fe} d_f}{s_f}$ 

Since  $f_{fe} = E_f \varepsilon_{fe}$ , the contribution of the FRP to shear resistance may be controlled by  $\varepsilon_{fe}$  as done in most existing models for  $V_f$ .

Based on the results of statistical assessments (including the reliability study) and for simplicity, the following expressions are proposed for determining the effective strain ( $\varepsilon_{fe}$ ) and use in the AASHTO LRFD Bridge Design Specifications (AASHTO, 2008).

When "full-anchorage" is provided such that the shear resistance at shear failure is controlled by FRP rupture:

$$\varepsilon_{fe} = R \, \varepsilon_{fu}$$
 where  $\varepsilon_{fu} = f_{fu} / E_f$  and  $R = 4 (\rho_f E_f)^{-.67} \le 1.0$ 

where  $\rho_t E_f$  is in ksi units and limited to 300 ksi.

Comparison of this expression with the test data yields an average strength ratio (bias) of 1.68 and a corresponding COV of 0.33.

When "full-anchorage" is not provided, it is likely that the shear capacity will be controlled by FRP debonding or another mode of failure before FRP rupture can be achieved:

$$\varepsilon_{fe} = R \varepsilon_{fu} \le 0.012$$
 where  $\varepsilon_{fu} = f_{fu} / E_f$  and  $R = 3(\rho_f E_f)^{-.67} \le 1.0$ 

where  $\rho_f E_f$  is in ksi units and limited to 300 ksi.

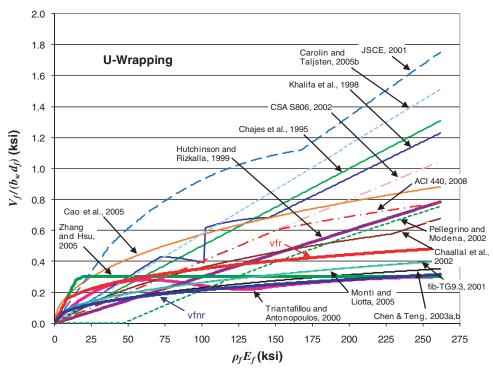


Figure 3.1. Influence of FRP axial rigidity on FRP shear stress resistance.

Comparison of this expression with the test data yields an average strength ratio (bias) of 1.44, and a corresponding COV of 0.25.

These expressions are only applicable for RC and PC members in which  $d_v/b_v < 4.0$ , and the calculated R value should not be taken greater than one (i.e.,  $R \le 1.0$ ).

Figure 3.1 shows the calculated shear stress capacity provided by the FRP reinforcement ( $V_f/b_w d_f$ ) as a function of the axial rigidity of the FRP reinforcement ( $\rho_f E_f$ ) for 15 models and the two relationships identified in this study for a member having a rectangular cross-section and the following properties:

Dimensions: 7.09 inches wide, 19.69 inches high, and a shear span-to-depth ratio of 3.5

FRP reinforcement: CFRP sheets externally bonded with fibers oriented at 90 in a U-wrap configuration over a height of 17.32 inches

Concrete compressive strength: 8,557 psi

Modulus of elasticity of the CFRP sheets: 33,939 ksi Ultimate tensile strength of the CFRP sheet: 653 ksi

The case of full anchorage for which FRP rupture failure is expected is labeled by *vfr*, and the case of less than full anchorage for which debonding or other non-rupture failure modes are expected is labeled *vfnr*. Figure 3.1 shows that the strength when full anchorage is not provided is less than when full anchorage is provided. In addition, the two relationships

(Chen and Teng, 2003a,b; Zhang and Hsu, 2005) provide values similar to those obtained from the models that provide the best estimates of FRP shear contribution (i.e., Triantafillou and Antonopoulos, 2000; and fib-TG9.3, 2001).

## 3.2 Design Guidelines

Recommended design guidelines for concrete girders strengthened in shear with FRP were developed based on the findings of this research. The guidelines, provided as Attachment B, were drafted in LRFD format to facilitate incorporation into the *AASHTO LRFD Bridge Design Specifications* (AASHTO, 2008).

## 3.3 Design Examples

Six design examples were prepared to illustrate the use of the proposed design. Four of the design examples consider RC T-beams (i.e., two with transverse steel reinforcement and two without transverse steel reinforcement) with a U-wrap FRP strengthening scheme with and without anchorage (i.e., two with mechanical anchorage and two without any anchorage). The other two design examples consider PC I-girders with transverse steel reinforcement and U-wrap FRP strengthening scheme with and without anchorage (i.e., one with mechanical anchorage and one without any anchorage).

## CHAPTER 4

# Summary of Findings and Recommendations for Future Research

This section summarizes the findings of this research effort and provides suggestions for future research.

### 4.1 Summary of Findings

This research effort has produced recommended design methods and specifications for strengthening concrete girders in shear using externally bonded FRP systems. The findings of this research regarding use of FRP systems for strengthening concrete girders in shear are as follows:

- Externally bonded FRP can be used to enhance the shear resistance of concrete girders.
- Externally bonded FRP systems can be applied in a variety of configurations and molded to any geometrical shape to provide side bonding, U-wrap, or complete wrapping of the girder web and as continuous sheets or discrete strips. The fibers of the composite may be oriented in any direction. Fibers oriented perpendicular to the longitudinal axis of the girder provide the most practical application, but fibers oriented orthogonal to the shear crack provide the most effective application.
- There is an interaction between transverse steel reinforcement and externally bonded FRP shear reinforcement. The
  effectiveness of externally bonded FRP for shear strengthening decreases as the transverse steel reinforcement ratio
  increases.
- The shear span-to-depth ratio (a/d) influences the effectiveness of externally bonded FRP for shear. Shear span-to-depth ratios (a/d) less than 2.0 develop arch action resistance mechanisms (deep beam behavior) that reduce the effectiveness of FRP shear strengthening.
- Tests on large scale RC T-beams showed that the size-effect has little influence on the effectiveness of externally bonded FRP (effective strains in the FRP of the large-scale specimens were found to be similar to those reported for small-scale tests).

- Tests on beams with pre-existing cracks prior to strengthening showed that stirrups yield at a lower shear force than for beams without cracks. However, the existence of cracks seemed not to change the failure modes of the beams suggesting that the existence of cracks does not adversely influence the effectiveness of FRP shear strengthening.
- Beam continuity (negative moment) did not appear to influence the behavior of the beams strengthened with FRP (similar behavior to beams tested under positive moment conditions).
- The effectiveness of externally bonded FRP for shear strengthening depends on the failure mode (i.e., FRP rupture or debonding). Debonding occurs when girders are strengthened in shear by side bonding and occasionally in cases of U-wrapping due to insufficient bond length. FRP rupture can be reached through use of proper anchorage such as that provided by complete wrapping, adequate bond length, or by some form of mechanical anchorage. Girders strengthened in shear with a U-wrapping configuration fail by either debonding or FRP rupture, depending on the bond characteristics.
- The use of mechanical anchorage delays and, in some cases, prevents debonding of the FRP, resulting in a greater increase of the ultimate shear resistance. Use of horizontal strips of FRP as mechanical anchorage does not provide much additional shear capacity. Continuous CFRP plates with anchorage bolts are not very effective in anchoring the CFRP sheets. Discontinuous CFRP plates attached with concrete wedge anchors or bolts through the web provide the most effective mechanical anchorage. The effectiveness of this method can be further improved by the use of a sandwich application that prevents slippage of the FRP sheet from beneath the anchorage plate. For PC girders with very thin webs, the embedment length of anchor bolts may not be sufficient to avoid premature failure due to the anchor bolts pulling out. In such cases, the use of a thru-bolt systems are more practical and provide better performance.

- The effectiveness of FRP for shear strengthening is significantly affected by the cross-sectional shape of the girder. Debonding of FRP accompanied by peeling of the concrete cover can result in a web crushing failure.
- If the stresses in the stirrups are less than the yield strength, the FRP strengthening can help delay yielding and prevent fatigue failure of the girder in shear. However, if the stirrups have already yielded, the FRP strengthening system would not reduce the stresses but could help restrain steel stress increases and prevent catastrophic failure of the girder.
- In the absence of a proper anchorage system, the externally bonded FRP sheets for shear strengthening could become debonded and result in no shear strengthening.
- Limiting the stress in the stirrups to the yield strength will assure that shear fatigue failure of the girder will not occur.
- The effective FRP strain used in evaluating the FRP shear contribution can be expressed by two separate design expressions to consider the two predominant failure modes (i.e., debonding and FRP rupture). One expression is for members in which sufficient anchorage is provided (FRP rupture failure mode), and the other is for members in which insufficient anchorage is provided (FRP debonding failure mode).

### 4.2 Suggestions for Future Research

Based on the work performed in this research, the following research efforts are needed to enhance understanding of the mechanisms associated with the use of externally bonded FRP for shear.

- An interaction exists between the internal transverse steel reinforcement and externally bonded FRP shear reinforcement, but there are insufficient data to quantify this interaction. Further investigations are needed to better quantify the mechanisms involved in this interaction and incorporate it into an enhanced model for the shear resistance of RC beams strengthened with externally-bonded FRP.
- The use of mechanical anchorage involving discontinuous CFRP plates attached with steel concrete wedge anchors or bolts through the web was found to delay or, in some cases, prevent debonding of FRP. However, because these anchors and bolts are susceptible to corrosion, research is needed to explore alternative mechanical anchorage techniques that are not susceptible to such corrosion.
- The cross-sectional geometry of PC girders influences the
  effectiveness of externally bonded FRP. Also thin web and
  stiff flange geometry reduce the effectiveness of the FRP
  shear strengthening. However, limited results are available
  to fully understand the mechanisms involved in such behavior. Further research is needed to examine the effect of crosssectional geometry of PC girders.
- The effective strain concept was adopted for design guidelines and codes to provide a simple and practical method for estimating the shear contribution of FRP. Research is needed to investigate the non-uniform FRP distribution and develop more reliable design equations.
- Research is needed to investigate the long-term fatigue performance of FRP systems for shear strengthening, particularly the effects of cracks on bond characteristics.

## **Notations**

a Shear span length

a/d Shear span-to-depth ratio

 $A_c$  Concrete area

 $A_{cf}$  Effective flange concrete area  $A_{cw}$  Web concrete area  $= b_w h$  Cross-sectional area of FRP

 $A_p$  Cross-sectional area of strengthening material [Sim et al., 2005]

 $A_{sw}$ ,  $A_{v}$  Area of transverse steel reinforcement

 $b, b_v, b_w$  Minimum width of cross-section over effective depth  $b_f$  Width of FRP strip [Carolin and Taljsten, 2005]

C Constant strain rate =  $110 \times 10^{-6}$  mm<sup>-1</sup> d,  $d_v$  Effective depth of cross-section  $d_f$  Effective depth of FRP reinforcement

 $D_{frp}$  Stress distribution factor for FRP intersected by the shear crack [Chen

and Teng, 2003 a and b]

 $d_{FRP}$  FRP sheet height along side of beam web [Deniaud and Cheng, 2001,

2004

 $D_{f\theta}$  Modified FRP strain distribution factor =  $D_{fip}/\theta$  [Cao et al., 2005]

 $d_{\rm S}$  Stirrup height

e spacing of stirrups [Sim et al., 2005]

 $E_{fr} E_{frp}$  Elastic modulus of FRP

 $(E_f \rho_f)_{lim}$  Limiting value of FRP rigidity separating debonding and FRP rupture

failure modes

*E*<sub>s</sub> Elastic modulus of steel reinforcement

 $f_{o}, f'_{c}$  Concrete compressive strength

 $f_{ck}$  Concrete characteristic cubic strength

 $f_{cm}$  Mean cylindrical compressive strength of concrete

 $f_{ctm}$  Concrete mean tensile strength Design ultimate strength of FRP

 $f_{fdd}$  Debonding FRP strength

Effective tensile stress in FRP sheet/strip in the direction of the prin-

cipal fibers

Design effective strength of the FRP shear strengthening

 $f_{frp}$  Tensile strength of FRP in the main fiber direction [Chen and Teng,

2003 a and b]

 $f_{frp.ed}$  Average/effective design stress of FRP intersected by shear crack at beam

failure

 $f_{fu}$  FRP ultimate tensile strength

 $f_{pv}$  Yield strength of strengthening material [Sim et al., 2005]

 $f_y, f_{yy}, F_y, f_{sy}$  Yield strength of steel reinforcement

h Height of RC/PC member  $h_{frp}$ ,  $h_{frp,e}$  Effective FRP height

*h<sub>i</sub>* Depth of U-jacket strengthening [Al-Sulaimani et al., 1994]

 $h_s$  Depth of each FRP strip [Al-Sulaimani et al., 1994]

 $h_v$  Effective depth of the concrete beam [Malek and Saadatmanesh,

1998]

 $h_w$  Height of web [Monti and Liotta, 2005]

 $h_w$  Height of shear wing strengthening [Al-Sulaimani et al., 1994] k Experimentally determined factor [Deniaud and Cheng, 2001, 2004]  $k_a$  Coefficient describing anchorage considerations [Deniaud and Cheng,

2001, 2004]

 $k_b$  Covering/scale coefficient

 $k_e$  Integer describing number of debonding ends

L Girder span length

 $l_b$  Available bond length of FRP

 $L_e$ ,  $L_{eff}$ ,  $L_{fe}$ ,  $l_e$  Effective bond length

 $l_{eq}$  Bonded length projected vertically that would be necessary if the

fabric strain was uniform

 $L_{\text{max}}$  Maximum bond length n Number of FRP plies

n Ratio of elastic modulus of FRP to elastic modulus of transverse steel

 $(E_f/E_s)$  [Chaallal et al., 2002]

n Number of spaces between stirrups [Deniaud and Cheng, 2001, 2004]

 $n_s$  Total number of stirrups crossing concrete shear plane

 $p_f$  FRP spacing measured orthogonal to the FRP orientation [Monti and

Liotta, 2005

 $\overline{Q}_{12}$ ,  $\overline{Q}_{13}$ ,  $\overline{Q}_{22}$ ,  $\overline{Q}_{23}$  Stiffness elements of FRP

R Ratio of effective stress/strain in the FRP sheet to its ultimate strength/

strain

 $R^*$  Additional reduction factor for debonding failures of beams with

steel web reinforcement [Pellegrino and Modena, 2002]

 $r_c$  Corner rounding radius of concrete section for which FRP is wrapped

 $R_{ck}$  Concrete characteristic cubic strength

 $R_L$  Remaining bonded width over initial width ratio [Deniaud and Cheng,

2001, 2004]

S Girder spacing s Spacing of stirrups  $s_{f}, s_{frp}$  Spacing of FRP strips

 $s_f$  FRP slip at debonding [Monti and Liotta, 2005]  $s_{f,max}$  Maximum spacing limitation for FRP strips

 $s_{xe}$  Crack spacing parameter

t,  $t_f$ ,  $t_{frp}$  FRP thickness

t Spacing of strengthening material [Sim et al., 2005]

 $T_{FRP}$  Tension force in FRP

 $t_p$  Nominal thickness of FRP sheet or bonded plate

 $t_s$  Width of each FRP strip  $T_v$  Tension force in stirrups

V Shear force

 $V_c$  Shear contribution of concrete

 $V_{cy}$  Concrete contribution to shear resistance corresponding with yield-

ing of the stirrups along the primary shear crack

 $V_{cu}$  Concrete contribution to shear resistance corresponding with the

ultimate (maximum) load carried by the girder

 $V_{\text{exp}}$  Experimentally measured ultimate shear strength

 $V_{f}$ ,  $V_{fd}$ ,  $V_{fmax}$ ,  $V_{fmax}$ ,  $V_{frp}$  Shear contribution of FRP

 $V_{\it FE}$  Analytically (Finite Element) predicted ultimate shear strength  $V_{\it f.model}$  FRP contribution to shear resistance predicted by analytical models Relationship developed for the case of less than full anchorage such that debonding or other non-rupture failures are expected

vfr Relationship developed for the case of full anchorage such that FRP

rupture failure is expected

 $V_{frp,d}$  Contribution of external FRP reinforcement (design value)

[Triantafillou, 1998]

 $V_{f,test}$  Experimentally measured shear strength of a test beam with FRP re-

inforcement minus the experimentally measured shear strength of the

corresponding control beam without FRP reinforcement

 $V_{fv}$  FRP contribution to shear resistance corresponding with yielding of

the stirrups along the primary shear crack

 $V_{fu}$  FRP contribution to shear resistance corresponding with the ultimate

(maximum) load carried by the girder

 $V_n$  Total shear capacity

 $V_{n,norm}$  Normalized shear strength

 $V_{n,test}$  Experimentally measured shear strength of a beam

V<sub>P</sub> Fiber glass plate component of shear capacity [Al-Sulaimani et al.,

1994]

 $V_r$  Total shear resistance [Deniaud and Cheng, 2001, 2004]

 $V_{Rd,f}$  Shear carried by FRP [Monti and Liotta, 2005]

 $V_s$ ,  $V_{se}$  Shear contribution of stirrups

 $V_{sy}$  Transverse steel (stirrup) contribution to shear resistance correspon-

ding with yielding of the stirrups along the primary shear crack

$V_{su}$	Transverse steel (stirr	up) contribution	to shear resis	tance correspon-

ding with the ultimate (maximum) load carried by the girder

 $w_f$ ,  $w_{frp}$  Width of FRP strip

 $W_{fe}$  Effective width of FRP strip

Z Limit state function

z Length of a vertical tension tie

 $z_b$  Co-ordinate of lower edge of effective FRP bonded to the sides of a

beam

 $z_{rid,eq}$  Vertically projected length of the FRP strip, minus the effective bond

length where bond is building up, plus a bonded length that would be necessary if the FRP stress was uniform under the debonding slip

 $z_t$  Co-ordinate of upper edge of effective FRP bonded to the sides of a

beam

α Angle of inclination of transverse steel reinforcement to longitudi-

nal axis of beam

α Reduction factor [Triantafillou and Antonopoulos, 2000]
 α Crack inclination angle [Carolin and Taljsten, 2005]

α Angle between principal direction of FRP sheets and the longitudinal

axis of the beam [Deniaud and Cheng, 2001, 2004]

α Strength efficiency factor [Sim et al., 2005]

 $\alpha_f$  Angle between principal direction of FRP sheets and the longitudinal

axis of the beam [Hutchinson and Rizkalla, 1999]

 $\alpha_{MF}$  Random variable for uncertainties in material and fabrication tolerances  $\beta$  Angle of inclination of FRP fibers to longitudinal axis of member  $\beta$  Factor relating effect of longitudinal strain on the shear capacity of

concrete, as indicated by the ability of diagonally cracked concrete to

transmit tension [AASHTO LRFD, 2008]

 $\beta_L$  Bond length coefficient

 $\beta_r$  Reliability index

 $\beta_{r,target}$  Reliability index targeted by most AASHTO calibration studies

 $\beta_w$  FRP strip width coefficient

 $\varepsilon_1, \varepsilon_2$  Strains in the principal 1–2 directions

 $\varepsilon_{bond}$  Maximum allowable strain without achieving anchor failure [Car-

olin and Taljsten, 2005]

 $\varepsilon_{c max}$  Maximum allowable strain to achieve concrete contribution

 $\varepsilon_{cr}$  Critical FRP strain

 $\varepsilon_{f,ave}$  Average strain in FRP at failure [Hutchinson and Rizkalla, 1999]

 $\varepsilon_{fe}$ ,  $\varepsilon_{f,e}$ ,  $\varepsilon_{frp,e}$ ,  $\varepsilon_{eff}$  Effective tensile strain of FRP

 $\epsilon_{fk,e}$  Characteristic effective FRP strain in principal fiber direction

[Triantafillou and Antonopoulos, 2000]

 $\varepsilon_{f,e,A}$  Effective FRP strain in principal fiber direction—ACI code format

[Triantafillou and Antonopoulos, 2000]

 $\varepsilon_{f \text{ max}}, \varepsilon_{f, \text{ max}}$  Maximum strain in FRP sheet  $\varepsilon_{fu}$  Ultimate tensile strain of FRP

 $\varepsilon_f(y)$  Strain in FRP fibers at height y [Carolin and Taljsten, 2005]

Maximum or limiting value of FRP strain  $\epsilon_{max}$ 

 $\epsilon_{\text{max}}$ Maximum FRP strain over remaining bonded width [Deniaud and

Cheng, 2001, 2004]

 $\epsilon_{\text{max,}A}$ Limiting value of effective FRP strain—ACI code format [Triantafillou

and Antonopoulos, 2000]

 $\varepsilon_s$ Tensile strain in cracked concrete in direction of tension tie Effective stirrup strain at failure [Hutchinson and Rizkalla, 1999]  $\epsilon_{se}$ 

Yield strain of steel stirrups  $\varepsilon_{sv}$ ,  $\varepsilon_{v}$ 

Ultimate FRP strain [Deniaud and Cheng, 2001, 2004]  $\epsilon_{ultFRP}$ 

Ultimate vertical tensile strain of the concrete taken as 0.005 [Chajes  $\varepsilon \nu_{cu}$ 

et al., 1995]

 $\overline{\epsilon}_{z}$ Normalized strain in FRP [Chen and Teng, 2003b]

Maximum normalized strain in FRP [Chen and Teng, 2003 b]  $\overline{\epsilon}_{z,\max}$ 

Shear strength reduction factor for FRP  $\phi_f$ 

Coefficient accounting for the effects of sheets wrapped around a  $\phi_R$ 

corner

Partial safety factor for FRP  $\gamma_f, \gamma_{frp}, \gamma_{Rd}$ 

The ratio of the vertical component of average strain in the FRP sheets  $\gamma_{fs}$ 

to the average strain in the steel stirrups

Partial safety factor depending on the FRP application accuracy  $\gamma_{f,d}$  $\Gamma_{Fk}$ Specific fracture energy of the FRP-concrete bond interface

η Average fiber utilization (effectiveness) factor Random variable for girder distribution factor  $\eta_{\text{GDF}}$ 

λ Shear span-to-effective depth ratio

λ Normalized maximum bond length of FRP =  $L_{max}/L_e$  [Chen and Teng,

2003a]

 $\lambda_{frp}$ Normalized FRP bond length =  $L_{max}/L_e$  [Cao et al., 2005]

Constant that represents the contribution of compressive strength of

concrete

 $\theta$ ,  $\theta$ Shear crack angle or angle of diagonal compression

θ Angle between the principal tensile stress and the fiber direction

[Carolin and Talisten, 2005]

 $\theta_f$ Shear plane angle in flange  $\theta_w$ Shear plane angle in web

 $\xi_P$ Random variable for analysis model accuracy

FRP reinforcement ratio =  $\frac{A_f}{b_v s_f} = \frac{2n_f t_f w_f}{b_v s_f}$  ( $w_f = s_f = 1.0$  for continu- $\rho_f$ ,  $\rho_{frp}$ 

ous wraps)

FRP reinforcement ratio =  $(A_f \text{ per unit length}/bd) = 2t_f/bd$  [Chaallal  $\rho_f$ 

et al., 2002]

Shear steel reinforcement ratio =  $(A_v \text{ per unit length}/bd) = A_v/sbd$  $\rho_s$ 

[Chaallal et al., 2002]

Stiffness ratio between the transverse steel shear reinforcement and  $\rho_{s,f}$ 

FRP shear reinforcement [Pellegrino and Modena, 2002]

 $\rho_{tot}$  Total shear reinforcement ratio [Chaallal et al., 2002]

 $\rho_{v}$  Transverse steel reinforcement ratio =  $\frac{A_{v}}{b_{v}s}$ 

 $\sigma_{cu}$  Concrete compressive strength

 $\sigma_{frp,max}$  Maximum stress in FRP intersected by shear crack [Chen and Teng,

2003b]

 $\sigma_{frp,max,d}$  Maximum stress in FRP intersected by shear crack for design [Chen

and Teng, 2003a]

 $\sigma_{frp,z}$  Stress in the FRP at the ultimate limit state at the location where the

intersecting critical shear crack is at a coordinate z [Chen and Teng,

2003a]

τ Shear stress

 $\tau_{ave}$  Average shear stress

 $\tau_{max}$  Ultimate direct bond shear strength between FRP and concrete

 $\tau_{ult}$  Interface shear strength between concrete and fiberglass plates

[Al-Sulaimani et al., 1994]

 $\zeta$  Coordinate ratio of the upper edge to the lower edge of the effective

 $FRP = z_t/z_b$ 

 $\zeta_{DC}$  Random variable for component dead load

 $\zeta_{\it LL+IM}$  Random variable for highway live load including impact loads

 $\zeta_{ws}$  Random variable for wearing surface dead load

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## ATTACHMENT A

# Recommended Changes to AASHTO LRFD Bridge Design Specifications

These proposed changes to AASHTO LRFD Bridge Design Specifications are the recommendations of the NCHRP Project 12-75 Research Team at the Missouri University of Science and Technology. These changes have not been approved by NCHRP or any AASHTO committee nor formally accepted for the AASHTO specifications.

#### 5.2 Definitions – (only additions are shown in this section)

FRP - fiber-reinforced polymer laminate consisting of fibers (carbon, aramid, or glass) and an epoxy matrix.

#### 5.3 Notation – (only additions and particularly relevant notations are shown)

- $d_v$  = effective shear depth as determined in Article 5.8.2.9 (in.)
- $d_f$  = effective depth of FRP shear reinforcement in Article 5.8.3.3 (in.)
- $f_{fe}$  = effective stress of FRP shear reinforcement as determined in Article 5.8.3.3 (ksi)
- s = spacing of stirrups (in.)
- $s_f = \text{center-to-center spacing of FRP shear reinforcement in Article 5.8.3.3 (in.)}$
- $h_f$  = flange thickness in Article 5.8.3.3 (in.)
- $\alpha$  = angle of inclination of transverse steel reinforcement to longitudinal axis (°)
- $\alpha_f$  = angle of inclination of transverse FRP reinforcement to longitudinal axis in Article 5.8.3.3 (°)
- $A_f = \text{sum of area of FRP reinforcement on both faces of the web within a distance } s_f \text{ in Article 5.8.3.3 (in.}^2)$
- $V_f =$  shear resistance provided by externally bonded FRP shear reinforcement in Article 5.8.3.3 (kip)
- $E_f = \text{modulus of elasticity of FRP reinforcement in Article 5.8.3.3 (ksi)}$
- $\varepsilon_{fe}$  = effective strain of FRP reinforcement in Article 5.8.3.3
- $\varepsilon_{fu}$  = failure tensile strain of FRP reinforcement in Article 5.8.3.3
- $R_f$  = strain reduction factor to account for the effectiveness of FRP strengthening in Article 5.8.3.3
- $\rho_f$  = FRP shear reinforcement ratio in Article 5.8.3.3
- $n_f$  = number of plies of FRP reinforcement in Article 5.8.3.3
- $t_{\rm f}$  = thickness of one ply of FRP reinforcement in Article 5.8.3.3 (in.)
- $w_f$  = width of FRP shear reinforcement in Article 5.8.3.3 (in.)

#### COMMENTARY

#### 5.8.2.6 Types of Transverse Reinforcement

Transverse reinforcement may consist of

#### • Steel reinforcement in the form of:

- Stirrups making an angle not less than 45° with the longitudinal tension reinforcement;
- Welded wire fabric reinforcement, with wires located perpendicular to the axis of the member, provided that the transverse wires are certified to undergo a minimum elongation of 4 percent, measured over a gage length of at least 4.0 in. including at least one cross wire;
- Anchored prestressed tendons, detailed and constructed to minimize seating and timedependent losses, which make an angle not less than 45° with the longitudinal tension reinforcement;
- Longitudinal bars bent to provide an inclined portion making an angle of 30° or more with the longitudinal tension reinforcement and inclined to intercept potential diagonal cracks;
- Combinations of stirrups, tendons, and bent longitudinal bars; or
- o Spirals.
- Externally bonded FRP shear reinforcement making an angle not less than 45° with the longitudinal flexural tensile reinforcement in accordance with Article 5.8.3.5 and 5.8.3.6.3 as applicable.

Transverse reinforcement shall be detailed such that the shear force between different elements or zones of a member are effectively transferred.

Torsional reinforcement shall consist of both transverse and longitudinal <u>steel</u> reinforcement. Longitudinal <u>steel</u> reinforcement shall consist of bars and/or tendons. Transverse steel reinforcement shall consist of:

- Closed stirrups perpendicular to the longitudinal axis of the member,
- A closed cage of welded wire fabric with transverse wires perpendicular to the axis of the member, or
- Spirals.

Transverse torsion reinforcement shall be made fully continuous and shall be anchored by 135° standard hooks around longitudinal reinforcement.

# **5.8.2.7** Maximum Spacing of Transverse Reinforcement

The <u>center-to-center</u> spacing of the transverse <u>steel</u> reinforcement <u>and the center-to-center spacing between externally bonded FRP shear reinforcement</u> shall not exceed the maximum permitted spacing,  $s_{\max}$ , determined as:

- If  $v_u < 0.125 f_c$  then  $s_{\text{max}} = 0.8 d_v \le 24.0 \text{ in.}$
- If  $v_u \ge 0.125 f_c$  then  $s_{\text{max}} = 0.4 d_v \le 12.0$  in.

where:

 $v_u$  = the shear stress calculated in accordance with 5.8.2.9 (ksi)

 $d_v$  = effective shear depth as defined in Article 5.8.2.9 (in.)

For segmental post-tensioned concrete box girder bridges, spacing of closed stirrups or closed ties required to resist shear effects due to torsional moments shall not exceed one-half of the shortest dimension of the cross section, or 12.0 in.

#### 5.8.2.8 Design and Detailing Requirements

Transverse <u>steel</u> reinforcement shall be anchored at both ends in accordance with the provisions of Article 5.11.2.6. For composite flexural members, extension of beam shear reinforcement into the deck slab may be considered when determining if the development and anchorage provisions of Article 5.11.2.6 are satisfied.

The design yield strength of nonprestressed transverse steel reinforcement shall be taken equal to the specified yield strength when the latter does not exceed 60.0 ksi. For nonprestressed transverse steel reinforcement with yield strength in excess of 60.0 ksi, the design yield strength shall be taken as the stress corresponding to a strain of 0.0035, but not to exceed 75.0 ksi. The design yield strength of prestressed transverse steel reinforcement shall be taken as the effective stress, after allowance for all prestress losses, plus 60.0 ksi, but not greater than  $f_{py}$ .

When welded wire reinforcement is used as transverse reinforcement, it shall be anchored at both ends in accordance with Article 5.11.2.6.3. No welded joints other than those required for anchorage shall be permitted.

Components of inclined flexural compression and/or flexural tension in variable depth members shall be considered when calculating shear resistance.

Externally bonded FRP shear reinforcement shall be installed to a beam using:

• Side bonding, in which the FRP is only bonded

#### COMMENTARY

# C5.8.2.7 Maximum Spacing of Transverse Reinforcement

Sections that are highly stressed in shear require more closely spaced reinforcement to provide crack control.

#### C5.8.2.8

Figure C5.8.2.8-1 shows different possible configurations of the FRP when applied to a beam.

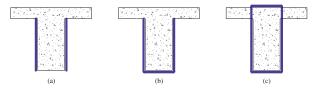


Figure C5.8.2.8-1 - Configuration of FRP Application: (a)
Two-side bonding, (b) U-wrap, and (c) Complete wrap

to the sides of the component;

- U-wrap, in which FRP U-jackets are bonded on both the sides and the soffit of the component; or
- Complete wrapping, in which the FRP is wrapped around the entire cross section.

The fibers in the FRP in its final position on the concrete component shall be oriented to provide the required resistance. The orientation of the fibers shall be shown on the contract documents.

Externally bonded FRP shear reinforcement may be anchored to the concrete. Mechanical anchorage systems consisting of FRP composite plates and concrete anchor bolts shall be proportioned such that the factored bearing resistance of the concrete anchor bolts used to anchor one end of a FRP strip is not less than the tensile force exerted from the FRP strip calculated on the basis of the failure tensile strain of the FRP. The use of additional horizontal strips of FRP as anchorage for FRP shear reinforcement shall not be permitted.

#### 5.8.3.3 Nominal Shear Resistance

The nominal shear resistance,  $V_n$ , shall be determined as the lesser of:

$$\frac{V_n = V_c + V_s + V_f + V_p}{\text{and}}$$

$$V_n = 0.25 f_c' b_v d_v + V_p$$
(5.8.3.3-1)
(5.8.3.3-2)

in which:

$$V_c = 0.0316 \, \beta \, \sqrt{f_c'} \, b_\nu \, d_\nu$$
, if the procedures of Articles 5.8.3.4.1 or 5.8.3.4.2 are used (5.8.3.3-3)

 $V_c$  = the lesser of  $V_{ci}$  and  $V_{cw}$ , if the procedure of Article 5.8.3.4.3 are used

$$V_{s} = \frac{A_{v} f_{y} d_{v} \left(\cot \theta + \cot \alpha\right) \sin \alpha}{s}$$
 (5.8.3.3-4)

$$V_{f} = \frac{A_{f} f_{fe} d_{f}}{s_{f}} (\sin \alpha_{f} + \cos \alpha_{f})$$
 (5.8.3.3-5)

where:

 $\underline{A_f}$  = area of FRP shear reinforcement within a distance  $\underline{s_f}$  (in.<sup>2</sup>)

 $A_v$  = area of steel shear reinforcement (stirrups) within a distance  $s_v$  (in.<sup>2</sup>)

 $b_{\nu}$  = effective web width taken as the minimum web width within the depth dv as determined in Article 5.8.2.9 (in.)

#### COMMENTARY

The direction of the fibers relative to the direction of the stresses the FRP reinforcement is meant to resist will effect the effectiveness of the FRP reinforcement. The fibers should be oriented in the direction that maximizes the effectiveness of the FRP reinforcement.

Anchoring externally bonded FRP shear reinforcement helps reduce the potential for premature failure due to debonding. There are various types of anchorage systems available in the literature [NCHRP Report 12-75].

Examples of mechanical anchorage systems consisting of FRP composite plates and concrete anchor bolts are available in the literature [NCHRP Report 12-75].

#### C5.8.3.3

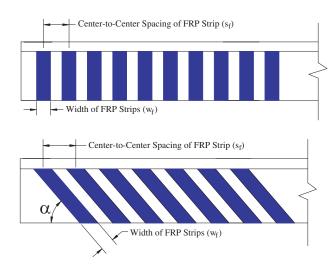


Figure C5.8.3.3-1 Illustration of the Terms  $s_f$  and  $w_f$ 

 $\underline{d_f}$  = effective depth of FRP shear reinforcement equal to  $\underline{d_y}$  for rectangular sections and  $\underline{d}$  -  $\underline{h_f}$  for T-sections(in.)

 $d_v$  = effective shear depth as determined in Article 5.8.2.9 (in.)

 $\underline{f_{fe}}$  = effective stress of FRP shear reinforcement as determined in Article 5.8.3.3 (ksi)

 $h_f$  = flange thickness (in.)

s = spacing of stirrups (in.)

 $\underline{s_f}$  = center-to-center spacing of FRP shear reinforcement (in.)

 $V_f$  = shear resistance provided by FRP shear reinforcement (kip); may only be used in conjunction with the provisions of Articles 5.8.3.4.1 and 5.8.3.4.2 when minimum steel shear reinforcement is provided or when the member depth or maximum spacing of distributed longitudinal reinforcement is less than 12 inches, and with the provisions of Article 5.8.3.4.3.  $V_f$  shall be taken as zero when  $d_V/b_V > 4$ 

 $V_p$  = component in the direction of the applied shear of the effective prestressing force; positive if resisting the applied shear (kip)

 $\underline{\alpha_f}$  = angle of inclination of FRP transverse reinforcement to longitudinal axis (°)

 $\beta$  = factor indicating ability of diagonally cracked concrete to transmit tension as specified in Article 5.8.3.4.

 $\theta$  = angle of inclination of diagonal compressive stresses as determined in Article 5.8.3.4 (°)

The effective stress of FRP shear reinforcement,  $f_{fe}$ , shall be determined as:

$$f_{fe} = E_f \varepsilon_{fe}$$
 (5.8.3.3-6)

in which

$$\overline{\varepsilon_{fe}} = R_f \varepsilon_{fu} \tag{5.8.3.3-7}$$

where:

 $E_f$  = modulus of elasticity of FRP reinforcement (ksi)

 $\underline{R_f} = \text{strain} \quad \text{reduction} \quad \text{factor} \quad \text{to} \quad \text{account} \quad \text{for} \quad \text{the} \quad \text{effectiveness of FRP strengthening}$ 

 $\underline{\varepsilon_{fe}}$  = effective strain of FRP reinforcement. it is limited to 0.012 when Eq. 5.8.3.3-9 is used.

 $\varepsilon_{fu}$  = failure tensile strain of FRP reinforcement

The strain reduction factor ( $R_f$ ) shall be determined as:

 For completely wrapped or properly anchored Uwrap configurations

$$R_f = 0.088 \le 4(\rho_f E_f)^{-.67} \le 1.0$$
 (5.8.3.3-8)

#### COMMENTARY

The application of FRP reinforcements on precast Ishaped sections with "slender webs" did not provide significant or reliable FRP contributions to shear capacity,  $V_{f_2}$ and on occasion resulted in a decrease of strength relative to that of the member that did not have FRP shear reinforcement [NCHRP Project 12-75]. Changes in the experimental setup and girder details made to address this reduction was unsuccessful. It was concluded that the reason that the application of FRP shear reinforcements did not lead to strength gains in I-girders with slender webs was due to degradation of the diagonal compressive resistance of slender webs when stiff and well bonded FRP reinforcements are glued to the surface of these webs. While the members experiencing this web resistance degradation were all prestressed, it has been concluded that this degradation was due to the slenderness of the webs and not the effect of prestressing [NCHRP Project 12-75]. Based on an examination of strength gains as a function of the ratio of depth to web width  $(d/b_v)$ , it was concluded that the shear resistance provided by FRP shear reinforcement,  $V_f$ , should be ignored for members with a web slenderness of  $d/b_w > 4$ [NCHRP Project12-75].

According to the observation on the experimental database, the maximum effective strain that can be achieved in the beams failing due to debonding of FRP was 0.012.

The upper bound for the quantity  $\rho_f E_f$  in Eqs. 5.8.3.3-8 and 5.8.3.3-9 is 300 ksi [NCHRP Project 12-75]. Substituting this value in the two equations results in the lower bound value of  $R_f$  shown in the two equations.

#### **COMMENTARY**

• For Un-anchored U-wrap or Two-side bonding configurations

$$R_f = 0.066 \le 3(\rho_f E_f)^{-.67} \le 1.0$$
 (5.8.3.3-9)

where:

 $\rho_f$  = FRP shear reinforcement ratio

The FRP shear reinforcement ratio,  $\rho_f$ , shall be determined as:

• For discrete strips

$$\rho_f = \frac{2n_f t_f w_f}{b_v s_f}$$
 (5.8.3.3-10)

The factor 2 in Equations 5.8.3.3-10 and 5.8.3.3-11 accounts for the presence of FRP reinforcement on both sides of a component.

• For continuous sheets

$$\rho_f = \frac{2n_f t_f}{b_v}$$
 (5.8.3.3-11)

#### where:

 $b_{\nu}$  = effective web width taken as the minimum web width within the depth  $d_{\nu}$  as determined in Article 5.8.2.9 (in.)

 $n_f$  = number of plies of FRP shear reinforcement

 $\underline{s_f}$  = center-to-center spacing of FRP shear reinforcement strips (in.)

 $t_f$  = thickness of FRP plies (in.)

 $w_f$  = width of FRP shear reinforcement strips (in.)

#### 5.8.3.5 Longitudinal Reinforcement

At each section, the tensile capacity of the longitudinal reinforcement on the flexural tension side of the member shall be proportioned to satisfy:

$$A_{ps} f_{ps} + A_{s} f_{y} \ge \frac{|M_{u}|}{d_{v} \phi_{f}} + 0.5 \frac{N_{u}}{\phi_{c}} + \left( \left| \frac{V_{u}}{\phi_{v}} - V_{p} \right| - 0.5 V_{s} - 0.5 V_{f} \right) \cot \theta$$
(5.8.3.5-1)

in which:

$$V_s + \underline{V_f} \le V_u / \phi \tag{5.8.3.5-2}$$

where:

 $V_s$  = shear resistance provided by the transverse <u>steel</u> reinforcement at the section under investigation as given by Eq. 5.8.3.3-4 (kip)

#### **COMMENTARY**

- $V_f$  = shear resistance provided by the transverse FRP reinforcement at the section under investigation as given by Eq. 5.8.3.3-5 (kip)
- $\theta$  = angle of inclination of diagonal compressive stresses used in determining the nominal shear resistance of the section under investigation as determined by Article 5.8.3.4 (°); if the procedures of Article 5.8.3.4.3 are used, cot  $\theta$  is defined therein
- $\phi_f \phi_v \phi_c$  = resistance factors taken from Article 5.5.4.2 as appropriate for moment, shear and axial resistance

The area of longitudinal reinforcement on the flexural tension side of the member need not exceed the area required to resist the maximum moment acting alone. This provision applies where the reaction force or the load introduces direct compression into the flexural compression face of the member.

Eq. 5.8.3.5-1 shall be evaluated where simply-supported girders are made continuous for live loads. Where longitudinal reinforcement is discontinuous, Eq. 5.8.3.5-1 shall be reevaluated.

At the inside edge of the bearing area of simple end supports to the section of critical shear, the longitudinal reinforcement on the flexural tension side of the member shall satisfy:

$$A_s f_y + A_{ps} f_{ps} \ge \left(\frac{V_u}{\phi_y} - 0.5V_s - 0.5V_f - V_p\right) \cot \theta$$
 (5.8.3.5-3)

Eqs. 5.8.3.5-1 and 5.8.3.5-2 shall be taken to apply to sections not subjected to torsion. Any lack of full development shall be accounted for.

## ATTACHMENT B

# Recommended Design Guidelines for Concrete Girders Strengthened in Shear with FRP

These proposed guidelines are the recommendations of the NCHRP Project 12-75 Research Team at the Missouri University of Science and Technology. These guidelines have not been approved by NCHRP or any AASHTO committee nor formally accepted for the AASHTO specifications.

#### COMMENTARY

#### **B1 GENERAL**

This attachment presents recommended design guidelines for concrete girders strengthened in shear using externally bonded fiber reinforced polymers (FRPs). Design examples developed using these guidelines are presented in the appendix.

#### **B1.1 Design Philosophy**

The proposed design guidelines were based on the traditional reinforced concrete (RC) design principles adopted by the current AASHTO LRFD Bridge Design Specifications and the knowledge on the mechanical behavior of FRP obtained from work performed under the NCHRP Project 12-75. As such, the factored shear resistance,  $\phi V_n$ , of a concrete member should meet or exceed the factored shear force applied to the member,  $V_u$ . The applied factored shear force and the factored shear resistance should be computed based on the load and resistance factors specified in the AASHTO LRFD Bridge Design Specifications. The factored shear resistance shall be determined as:

$$\phi V_n \ge V_u \tag{B1-1}$$

where:

 $V_n$ : Nominal shear resistance  $V_u$ : Required shear strength  $\phi$ : Strength reduction factor (0.9)

Careful consideration for all possible failure modes and subsequent strains and stresses should be considered in determining the nominal shear strength of a member.

#### **B1.2 Scope**

These design guidelines focus on presenting design procedures including design equations. Specific limits of applying the proposed design guidelines are also presented in the relevant sections throughout this document.

# B2 EVALUATION AND REPAIR OF EXISTING RC CB2 BEAMS

FRP strengthening is usually performed on structurally deficient or damaged RC beams. Before a strengthening procedure is implemented, the extent of deficiency and suitability of FRP strengthening should be evaluated. The necessary evaluation criteria for repair of existing concrete structures and post repair evaluation criteria are well established in the following documents.

Information, such as evaluation and repair of existing RC beams as well as proper application of FRP, is available; an attempt was made to provide references to other publications where additional details can be found.

- ACI 201.1R: Guide for Making a Condition Survey of Concrete in Service
- ACI 224.1R: Causes, Evaluation, and Repair of Cracks in Concrete
- ACI 364.1R-94: Guide for Evaluation of Concrete Structures Prior to Rehabilitation
- ACI 440.2R-08: Guide for the Design and Construction of Externally Bonded FRP Systems for Strengthening Concrete Structures
- ACI 503R: Use of Epoxy Compounds with Concrete
- ACI 546R: Concrete Repair Guide
- International Concrete Repair Institute (ICRI) ICRI 03730: Guide for Surface Preparation for the Repair of Deteriorated Concrete Resulting from Reinforcing Steel Corrosion
- International Concrete Repair Institute (ICRI) ICRI 03733: Guide for Selecting and Specifying Materials for Repairs of Concrete Surfaces
- NCHRP Report 609: Recommended Construction Specifications Process Control Manual for Repair and Retrofit of Concrete Structures Using Bonded FRP Composites

Relevant specifications and guidelines provided by FRP manufacturers should also be carefully reviewed prior to the design of any strengthening system.

#### **B3 STRENGTHENING SCHEMES**

FRP shear reinforcement is commonly attached to a beam, as shown in Figure B3.1 with (a) side bonding, in which the FRP is only bonded to the sides, (b) U-wrap, in which FRP U-jackets are bonded to both the sides and soffit, and (c) complete wrapping, in which the FRP is wrapped around the entire cross section.

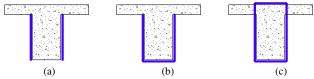


Figure B3.1 Strengthening Scheme: Cross-Sectional View (a) Side bonding, (b) U-wrap, and (c) Complete wrap

For all wrapping schemes, the FRP can be applied continuously along the portion of the member length to be strengthened or as discrete strips. The fibers of the FRP may also be oriented at various angles to meet a range of strengthening requirements as shown in Figure B3.2

#### CB3

Complete wrapping of the cross section is the most effective scheme and is commonly used in strengthening columns where there is sufficient access for such application. Beams are typically limited to U-wrap and side bonding applications since the integral slab makes it impractical to completely wrap such members. U-wrapping has been experimentally shown to be more effective in improving the shear resistance of a member than side bonding.

#### COMMENTARY

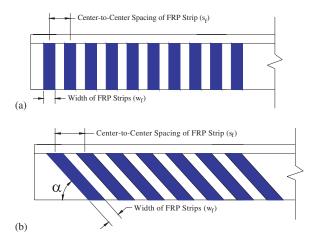


Figure B3.2 Strengthening Scheme: Side View — (a) Fibers at 90° Direction, and (b) Fibers at Inclined Direction

#### **B4 APPLICATION OF FRP**

#### **B4.1 General**

In general, procedures for the installation of FRP systems are developed by the manufacturer and can vary between different systems. Procedures may also vary depending on the type and condition of the structure to be strengthened. The application of FRP systems will not stop the ongoing corrosion of existing steel reinforcements. The cause of corrosion to internal steel reinforcements should be addressed and corrosion-related deterioration should be repaired prior to application of any FRP system.

#### **B4.2 Surface Preparation**

The concrete surface should be prepared to a minimum concrete surface profile (CSP) 3 as defined by the ICRI-surface-profile chips (ICRI 03732, NCHRP Report 609). Localized out-of-plane variations, including form lines, should not exceed 1/32 inch or the tolerances recommended by the FRP system manufacturer, whichever is smaller. Bug holes and voids should be filled with epoxy putty. It is recommended that surface preparation be accomplished using abrasive or water-blasting techniques. All laitance, dust, dirt, oil, curing compound, existing coatings, and any other matter that could interfere with the bond between the FRP system and concrete substrate should be removed.

When fibers are wrapped around corners, the corners should be rounded to a minimum 1/2 inch radius to prevent stress concentrations in the FRP system and voids between the FRP system and the concrete. Rough edges should also be smoothed by grinding or with putty prior to FRP application.

#### **CB4.1**

It is recommended that FRP applications be performed by a contractor trained in accordance with the installation procedures specified by the manufacturer. Comprehensive guidelines in this regard are provided in *NCHRP Report 609*, Recommended Construction Specifications and Process Control Manual for Repair and Retrofit of Concrete Structures Using Bonded FRP Composites

#### **CB4.2**

Bond behavior of the FRP system is highly dependent on a sound concrete substrate and can significantly influence the integrity of the FRP strengthening system. Proper preparation and profiling of the concrete substrate is necessary to achieve optimum bond strength. Improper surface preparation can lead to premature debonding or delamination.

#### **B4.3** Inspection, Evaluation, and Acceptance

Application of FRP systems should be inspected by a licensed engineer or qualified inspector knowledgeable in FRP systems and installation procedures. The following should be recorded at the time of installation:

- Date and time of installation
- Ambient temperature, relative humidity, and general weather observations and surface temperature of concrete
- Surface dryness, surface preparation methods and resulting profile using the ICRC-surface-profilechips
- Qualitative description of surface cleanliness
- Type of auxiliary heat source, if applicable
- Widths of cracks not injected with epoxy
- Fiber or pre-cured laminate batch number(s) and approximate locations in structure
- Batch numbers, mixture ratios, mixing times, and qualitative descriptions of the appearance of all mixed resins, including primers, putties, saturants, adhesives, and coatings mixed for the day
- Observations of progress of cure of resins
- Conformance with installation procedures
- Location and size of any delaminations or air voids
- General progress of work
- Level of curing of resin in accordance with ASTM D3418.
- Adhesion strength

#### **B5 MATERIAL PROPERTIES OF FRP**

The following mechanical properties should be obtained from manufacturers or coupon tests in accordance with ASTM D3039.

- $E_f$ : the modulus of elasticity of FRP
- $\varepsilon_{fu}$ : the ultimate strain of FRP.

Then, the nominal resistance,  $f_{fu}$ , can be determined assuming linear behavior of FRP stress-strain relationship up to failure as:

$$f_{fu} = E_f \varepsilon_{fu} \tag{B5-1}$$

#### **COMMENTARY**

#### **CB4.3**

When concrete and atmospheric temperatures exceed 90°F, difficulties may be experienced in application of the epoxy compound owing to acceleration of the reaction and hardening rates. If ambient temperatures above 90°F are anticipated, work should be scheduled when the temperature is lower, such as in the early morning hours. If it is necessary to apply epoxy compounds at temperatures exceeding 90 °F, the work should be supervised by a person experienced in applying epoxy at high temperatures. Epoxy systems formulated for elevated temperature are available (ACI 530R-93).

At temperatures below 40°F, difficulties may occur due to deceleration of the reaction rates. The presence of frost or ice crystals may also be detrimental to the bond between the FRP and the concrete.

Evaluate moisture content or outgassing of the concrete by determining if moisture will collect at bond lines between old concrete and epoxy adhesive before epoxy has cured. This may be accomplished by taping a 4 x 4 ft (1 x 1 m) polyethylene sheet to concrete surface. If moisture collects on underside of polyethylene sheet before epoxy would cure, then allow concrete to dry sufficiently to prevent the possibility of a moisture barrier between old concrete and new epoxy (ACI 530R-93).

During installation, sample cups of mixed resin should be prepared according to a predetermined sampling plan and retained for testing to determine level of curing in accordance with ASTM D3418. The relative cure of the resin can also be evaluated on the project site by physical observation of resin tackiness and hardness of work surfaces or hardness of retained resin samples.

For bond-critical applications, tension adhesion testing of cored samples should be conducted using the methods in ACI 530R or ASTM D 4541 or the method described by ISIS (1998). The sampling frequency should be specified. Tension adhesion strengths should exceed 200 psi and exhibit failure of the concrete substrate before failure of the adhesive (ACI 440.2R-08).

#### COMMENTARY

#### **B6 NOMINAL SHEAR RESISTANCE**

An interaction is known to exist between the shear contributions of concrete, transverse steel reinforcement, and FRP. However, this interaction mechanism is not yet fully understood and thus is not reflected in the design procedures. Therefore, following the current reinforced concrete design principals, the nominal shear resistance  $(V_n)$  is determined by adding the contribution of the FRP reinforcement to the contributions from concrete and internal transverse steel reinforcement:

$$V_n = V_c + V_s + V_f \tag{B6-1}$$

where,  $V_c$  is the contributions of concrete,  $V_s$  is the contribution of transverse steel reinforcement (stirrups), and  $V_f$  is the contribution of FRP. The contributions from the concrete ( $V_c$ ) and transverse steel reinforcement ( $V_s$ ) can be computed based on the current AASHTO LRFD Bridge Design Specifications. Calculation of the FRP contribution ( $V_f$ ) is presented in the following sections.

#### **B7 SHEAR CONTRIBUTION OF FRP**

#### **B7.1 Calculation of Contribution of FRP**

**CB7.1** 

The contribution of FRP  $(V_f)$  can be computed using the  $45^{\circ}$  truss model as:

$$V_{f} = \frac{A_{f} f_{fe} d_{f} (\sin \alpha_{f} + \cos \alpha_{f})}{s_{f}}$$

$$= \frac{A_{f} E_{f} \varepsilon_{fe} d_{f} (\sin \alpha_{f} + \cos \alpha_{f})}{s_{f}}$$

$$= \rho_{f} E_{f} \varepsilon_{fe} b_{v} d_{f} (\sin \alpha_{f} + \cos \alpha_{f})$$
(B7-1)

where,  $A_f$  is the area of FRP covering two sides of the beam and can be determined by  $2n_ft_fw_f$  ( $n_f$  is number of FRP plies,  $t_f$  is the FRP reinforcement thickness,  $w_f$  is the width of the strip),  $f_{fe}$  is the effective stress of FRP,  $d_f$  is the effective depth of FRP measured from the top of FRP reinforcement to the centroid of the longitudinal reinforcement,  $s_f$  is the center-to-center spacing of FRP,  $a_f$  is the angle of inclination of FRP with respect to the longitudinal axis of the member as shown in Figure B3.2,  $E_f$  is the modulus of elasticity of FRP,  $\epsilon_{fe}$  is the effective strain of FRP,  $\rho_f$  is the reinforcement ratio of FRP, and  $b_v$  is the effective web width taken as the minimum web width within the effective depth ( $d_f$ )

COMMENTARY

The FRP shear reinforcement ratio,  $\rho_f$ , is determined as:

For discrete strips

$$\rho_f = \frac{2n_f t_f w_f}{b_v s_f} \tag{B7-2}$$

For continuous sheets

$$\rho_f = \frac{2n_f t_f}{b_v} \tag{B7-3}$$

The effective strain ( $\varepsilon_{\it fe}$ ) represents the average strain experienced by the FRP at shear failure of the strengthened member and can be expressed as:

• For Full Anchorage (Rupture Failures Expected): Complete Wrap or U-Wrap with Anchors

$$\varepsilon_{fe} = R_f \varepsilon_{fu} \tag{B7-4}$$

where  $R_f = 0.088 \le 4(\rho_f E_f)^{-.67} \le 1.0$ 

 For Other Anchorage (Non-Rupture Failures more likely): Side bonding or U-Wrap

$$\varepsilon_{fe} = R_f \ \varepsilon_{fu} \le 0.012 \tag{B7-5}$$

where  $R_f = 0.066 \le 3(\rho_f E_f)^{-.67} \le 1.0$ 

The effective strain,  $\varepsilon_{fe}$ , is largely dependent on the failure modes as discussed in Appendix A - Sections A3 and A4. Therefore, the experimental database collected in this project was grouped by the failure mode of the test specimens, i.e., either as debonding or rupture of the FRP and then regression analyses were performed to obtain Eqn. B7-4 and B7-5.

The upper bound for the quantity  $\rho_f E_f$  in Eqs. B7-4 and B7-5 is 300 ksi. Substituting this value in these two equations results in the lower bound value of  $R_f$  shown in the two equations.

#### COMMENTARY

#### **B7.2 Limitations**

#### **B7.2.1** Shear span-to-depth ratio

The reduction factors  $(R_f)$  were developed from tests in which the loading was at a distance from the support sufficient to assume plane sections before deformation remain plane after deformation, i.e. shallow beam behavior. Thus, these provisions are only applicable to beams with a shear span-to-depth ratio greater than 2.5.

#### **B7.2.2 Maximum Amount of FRP Shear Reinforcement**

The amount of FRP should be determined so that the nominal shear strength calculated by Eq. B 6-1 should not exceed the nominal shear strength calculated by

$$V_n = 0.25 f_c b_\nu d_\nu + V_p$$
 (AASHTO 5.8.3.3-2)

#### **B.7.2.3 Maximum Spacing of FRP Shear Reinforcement**

The clear spacing between externally bonded FRP shear reinforcement shall not exceed the maximum permitted spacing ( $s_{\rm max}$ ) in accordance with the current AASHTO LRFD Bridge Design Specifications, expressed as:

If 
$$v_u < 0.125 f_c$$
 then  $s_{\max} = 0.8 d_v \le 24 \text{ in.}$  (AASHTO 5.8.2.7-1) If  $v_u \ge 0.125 f_c$  then  $s_{\max} = 0.4 d_v \le 12 \text{ in.}$  (AASHTO 5.8.2.7-2)

where  $v_u$  = the shear stress calculated in accordance with AASHTO LRFD – Article 5.8.2.9 (ksi) and  $d_v$  =effective shear depth as defined in AASHTO LRFD — Article 5.8.2.9 (in.)

#### **B7.3** Use of Anchorage Systems

Different types of anchorage systems are available for shear strengthening with FRP. Examples of mechanical anchorage systems consisting of FRP composite plates and concrete anchor bolts are available in the literature [NCHRP Report 12-75]. However, it should be noted that additional horizontal FRP strips cannot ensure FRP rupture failure. Thus, it is recommended that Equation B7-5 be used to calculate the FRP contribution, realizing that such approach will result in conservative estimates.

#### **CB7.2.2**

This provision is required to avoid web crushing failure of FRP strengthened beams due to excessive transverse shear reinforcement (both FRP and steel stirrups).

# APPENDIX

# **Design Examples**

The following six design examples are presented to illustrate use of the recommended guidelines:

- Example 1-1: RC T-beam without internal transverse steel reinforcement strengthened with FRP in U-wrap configuration without anchorage systems
- Example 1-2: RC T-beam without internal transverse steel reinforcement strengthened with FRP in U-wrap configuration with an anchorage system
- Example 2-1: RC T-beam with internal transverse steel reinforcement strengthened with FRP in U-wrap configuration without anchorage systems
- Example 2-2: RC T-Beam with internal transverse steel reinforcement strengthened with FRP in U-wrap configuration with an anchorage system
- Example 3-1: PC I-Beam with internal transverse steel reinforcement strengthened with FRP in U-wrap configuration without anchorage systems
- Example 3-2: PC I-Beam with internal transverse steel reinforcement strengthened with FRP in U-wrap configuration with an anchorage system

**DESIGN EXAMPLE 1-1:** RC T-Beam without Internal Transverse Steel Reinforcement Strengthened with FRP in U-wrap Configuration without Anchorage Systems

## 1. INTRODUCTION

This example demonstrates the design procedures for externally bonded FRP shear reinforcement of an older reinforced concrete (RC) bridge using a U-wrap configuration without anchorage. The bridge consists of simply supported T-beams spanning 42 feet and spaced at 4.5 feet on center. The T-beams contain no transverse steel reinforcement. Additional details of the T-beam are provided in Figures 1 and 2.

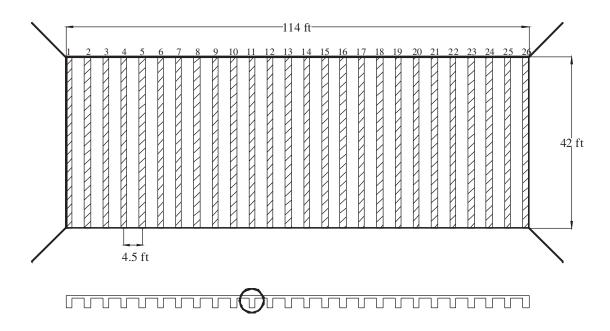


Figure 1. Bridge plan and transverse section.

#### 2. MATERIAL PROPERTIES

The following material properties have been chosen to represent those anticipated in an older bridge for which shear deficiencies might be expected.

#### 2.1. Concrete

Compressive strength  $f'_c := 3.0 \text{ ksi}$ 

Modulus of elasticity 
$$E_c := 33 \cdot (1.5)^{1.5} \sqrt{f'_c \cdot 1000}$$
 ksi 
$$E_c = 3321 \text{ ksi}$$

$$\beta_1 := \begin{bmatrix} 0.85 & \text{if} & f_c' \le 4 \\ 0.65 & \text{if} & f_c' \ge 8 \\ \\ \left[ 0.85 - 0.05 \cdot \left( f_c' - 4 \right) \right] & \text{otherwise} \end{bmatrix}$$

$$\beta_1 = 0.85$$

# 2.2. Longitudinal Reinforcement

Yield strength  $f_y := 60 \text{ ksi}$ Modulus of elasticity  $E_s := 29000 \text{ ksi}$ 

#### 2.3. FRP Reinforcement

Carbon Fiber Sheets are used in this example.

Thickness  $t_f := 0.0065$  in.

Failure strength  $f_{fu} := 550 \text{ ksi}$ 

Modulus of elasticity  $E_f := 33000 \text{ ksi}$ 

Failure strain 
$$\epsilon_{fu} \,:= \frac{f_{fu}}{E_f}$$
 
$$\epsilon_{fu} = 0.017 \text{ in/in}$$

#### 3. GEOMETRICAL PROPERTIES

Total Height  $h_T := 37$  in.

Flange Thickness  $h_f := 7$  in.

Width of the web  $b_v := 18$  in.

Effective Width of the Flange  $b_{eff} := 54$  in.

Tensile reinforcement =  $12#11 A_s := 18.72 in^2$ 

Internal shear reinforcement = Not provided  $A_v := 0.0 \text{ in}^2$ 

Distance from the extreme compression fiber to the center of the steel at the section d := 32.7 in.

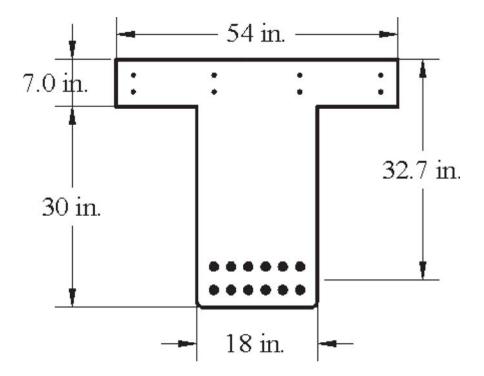


Figure 2. Cross-Section of an Intermediate Beam

# 4. CALCULATION OF THE FACTORED SHEAR FORCE AND NOMINAL SHEAR RESISTANCE

# 4.1 Factored Shear Force at the Critical Section

$$V_{u\_crit} := 100 \text{ kips}$$

# 4.2. Calculation of Nominal Shear Resistance

For this example, the simplified approach is followed.

$$\theta := 45 \text{ deg}$$
  $\beta := 2$ 

The nominal shear resistance provided by the concrete,  $V_c$ , is calculated in accordance with LRFD Eqn.5.8.3.3-3 as:

Assuming rectangular section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

$$c_{c1} := \frac{A_s \cdot f_y}{0.85 \cdot f'_c \cdot b_{eff} \cdot \beta_1}$$
  $c_{c1} = 9.6 \text{ in.}$ 

$$\begin{aligned} a_{c1} &:= \beta_1 \cdot c_{c1} & a_{c1} = 8.16 \text{ in.} \\ & \text{check\_} a_{c1} := \left\| \text{"Assumption is correct"} \quad \text{if } \left( a_{c1} \leq h_f \right) \right. \\ & \text{"Not behave as rectangular"} & \text{otherwise} \end{aligned}$$

check\_a<sub>c1</sub> = "Not behave as rectangular"

Assuming T-beam section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

$$\begin{split} c_{c2} &:= \frac{A_s \cdot f_y - 0.85 \cdot f'_c \cdot \left(b_{eff} - b_1\right) \cdot h_f}{0.85 \cdot f'_c \cdot b_v \cdot \beta_1} & c_{c2} = 12.32 \text{ in.} \\ a_{c2} &:= \beta_1 \cdot c_{c2} & a_{c2} = 10.47 \text{ in.} \\ check\_a_{c2} &:= \left\| \text{"Assumption is correct"} \right\| & \text{if } \left(a_{c2} \ge h_f\right) \\ & \text{"Not behave as rectangular"} & \text{otherwise} \end{split}$$

Therefore 
$$c_c := c_{c2}$$
  $c_c = 12.32 \text{ in.}$   $a_c := a_{c2}$   $a_c = 10.47 \text{ in.}$ 

The effective shear depth  $d_V$  is taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken less than the greater of  $0.9d_e$  or 0.72h (LRFD Article5.8.2.9)

check\_a<sub>c2</sub> = "Assumption is correct"

$$\begin{pmatrix} d_{v1} := d - \frac{a_c}{2} \\ d_{v2} := 0.9 \cdot d \end{pmatrix} \quad (d_{v3} := 0.72 \cdot h_T)$$

$$\begin{pmatrix} d_v := max(d_{v1}, d_{v2}, d_{v3}) \\ d_v \end{pmatrix} = 29.4 \text{ in.}$$

The nominal shear resistance provided by the concrete is:

$$v_c := 0.0316 \cdot \beta \cdot \sqrt{f'_c \cdot b_v \cdot d_v}$$
 (LRFD Eqn. 5.8.3.3-3)  
 $(v_c) = 58 \text{ kips}$ 

The nominal shear resistance provided by the internal steel reinforcement is:

$$v_s := 0$$

The nominal shear resistance provided by the vertical component of prestressing strands is:

$$\left(\mathbf{v}_{\mathbf{p}} := 0\right)$$

The nominal shear resistance of the member is:

$$v_n := v_c + v_s + v_p$$
 (LRFD Eqn. 5.8.3.3-1)  
 $v_n = 58 \text{ kips}$ 

#### 5. DESIGN OF FRP SHEAR REINFORCEMENT

## 5.1 Check if FRP Reinforcement is Necessary or Not

Strength reduction factor for shear ( $\phi := 0.9$ )

$$\label{eq:check_frp_needed} \begin{split} \text{Check\_FRP\_Needed} &:= \left| \text{"NOT need shear reinforcement"} \quad \text{if } \left( \phi \cdot V_n \geq V_{u\_crit} \right) \right. \\ \\ \text{"NEED shear reinforcement"} \quad \text{otherwise} \end{split}$$
 
$$\label{eq:check\_FRP\_Needed} \\ \text{Check\_FRP\_Needed} &= \text{"NEED shear reinforcement"} \end{split}$$

## 5.2 Computation of Required V<sub>f</sub>

$$V_{f\_req} := \frac{V_{u\_crit}}{\phi} - V_{n}$$

$$V_{f\_req} = 53.1 \text{ kips}$$

# 5.3 Selection of FRP Strengthening Scheme

U-wrap configuration is used without anchorage systems at the end of the sheets. The FRP sheets will be applied at 90 degree with respect to the longitudinal axis of the girder as shown in Figure 3. First, the spacing of FRP strips is chosen to meet the maximum spacing requirement. Then, the width of the FRP strips is selected to adjust the amount of FRP strips.

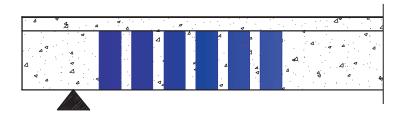


Figure 3 FRP strengthening scheme.

Use number of plies of FRP sheets

 $n_f := 1$ 

Use the width of FRP sheets

 $w_f := 8 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f := 15$  in.

Orientation of FRP sheets

 $\alpha_{\rm f} := 90 \deg$ 

Effective depth of FRP sheets  $d_f := d - h_f$ 

$$d_c = 25.7$$
 in.

Check if the selected spacing is acceptable or not

Shear stress on concrete is:

$$\left(v_{u} := \frac{V_{u\_crit} - \phi \cdot V_{p}}{\phi \cdot b_{v} \cdot d_{v}}\right)$$

$$\left(v_{u}\right) = 0.21 \text{ ksi}$$
(LRFD Eqn. 5.8.2.9-1)

The maximum spacing of the transverse reinforcement is:

$$s_{\text{max}} := \left| \begin{array}{ll} \min \left( 0.8 \cdot d_{\text{v}}, \, 24 \right) & \text{if } v_{\text{u}} < 0.125 \cdot f'_{\text{c}} \\ \min \left( 0.4 \cdot d_{\text{v}}, \, 12 \right) & \text{otherwise} \end{array} \right. \tag{LRFD Eqn. 5.8.2.7-1}$$

$$s_{max} = 23.5$$

# 5.4 Calculation of Shear Resistance of FRP, $V_f$

The FRP reinforcement ratio is:

$$\rho_{f} := \frac{2 \cdot n_{f} \cdot w_{f} \cdot t_{f}}{b_{v} \cdot s_{f}}$$

$$(Attachment A Eqn. 5.8.3.3-10)$$

$$(\rho_{f}) = 3.852 \times 10^{-4}$$

The FRP strain reduction factor is:

$$R_{f} := \min \left[ 3 \cdot \left( \rho_{f} \cdot E_{f} \right)^{-0.67}, 1.0 \right]$$
 (Attachment A Eqn. 5.8.3.3-9) 
$$R_{f} = 0.546$$

The effective strain of FRP is:

$$\varepsilon_{\rm fe} := \min \left( R_{\rm f} \cdot \varepsilon_{\rm fu}, \, 0.012 \right) \tag{Attachment A Eqn. 5.8.3.3-7}$$
 
$$\varepsilon_{\rm fe} = 9.103 \times 10^{-3} \text{ in./in.}$$

The effective stress of FRP is:

$$f_{fe} := \varepsilon_{fe} \cdot E_{f}$$
 (Attachment A Eqn. 5.8.3.3-6)  
 $\left(f_{fe}\right) = 300.4 \text{ ksi}$ 

The shear contribution of the FRP can be then calculated.

$$\begin{split} V_f &:= \rho_f \cdot E_f \cdot \epsilon_{fe} \cdot b_v \cdot d_f \cdot \left( \sin \left( \alpha_f \right) + \cos \left( \alpha_f \right) \right) & \text{(Attachment A Eqn. 5.8.3.3-5)} \\ \left( V_f \right) &= 53.5 \text{ kips} \\ V_{f\_check1} &:= \left\| \text{"Change FRP Strengthening Scheme"} \quad \text{if } \left( V_f < V_{f\_req} \right) \\ & \text{"Provided FRP Strength Large Enough"} \quad \text{otherwise} \\ V_{f\_check1} &= \text{"Provided FRP Strength Large Enough"} \\ V_{f\_check2} &:= \left\| \text{"Provided FRP amount is adequate"} \quad \text{if } \left( V_{f\_req} \leq V_f < 1.1 \cdot V_{f\_req} \right) \\ & \text{"Change the FRP amount slightly"} \quad \text{otherwise} \\ \left( V_{f\_check2} \right) &= \text{"Provided FRP amount is adequate"} \end{split}$$

## 5.5 Calculation of Design Shear Resistance of the Member

The design strength of the member is:

$$\phi V_{n\_total} := \phi \cdot \left( V_c + V_p + V_s + V_f \right)$$
 (Attachment A Eqn. 5.8.3.3-1) 
$$\left( \phi V_{n\_total} \right) = 100.4 \text{ kips}$$

$$\label{eq:web_crushing_limit} Web\_crushing\_limit := 0.25 \cdot f'_c \cdot b_v \cdot d_v + V_p \qquad (LRFD \ Eqn. \ 5.8.3.3-2)$$
 
$$Web\_crushing\_limit = 397.3 \ kips$$
 
$$Check\_web\_crushing\_limit := \left\| \text{"OK"} \qquad \text{if } \left( V_c + V_s + V_f + V_p \right) \le \text{Web\_crushing\_limit} \right.$$
 
$$\left\| \text{"No Good"} \qquad \text{otherwise} \right.$$
 
$$Check\_web\_crushing\_limit = \text{"OK"}$$

#### 6. SUMMARY

Externally bonded FRP sheets were designed in this example. The FRP sheets are applied at 90 degrees with respect to the longitudinal axis of the member with the U-wrap configuration and without anchorage systems as shown in Figure 4. The final design is summarized as:

Use number of plies of FRP sheets  $n_f = 1$ 

Use the width of FRP sheets  $w_f = 8 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f = 15$  in.

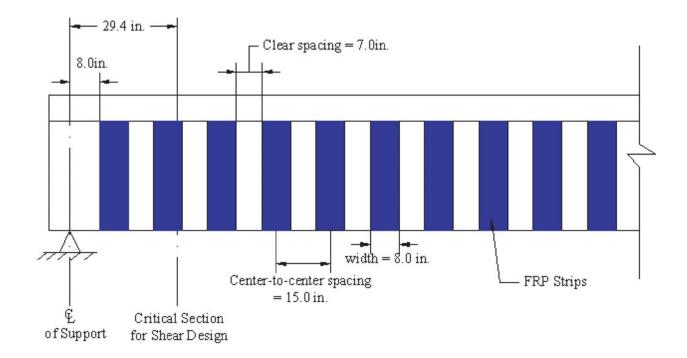


Figure 4. Final design of FRP strengthening.

**DESIGN EXAMPLE 1-2:** RC T-Beam without Internal Transverse Steel Reinforcement Strengthened with FRP in U-wrap Configuration with an Anchorage System

#### 1. INTRODUCTION

This example demonstrates the design procedures for externally bonded FRP shear reinforcement of an older reinforced concrete (RC) bridge using a U-wrap configuration with anchorage. The bridge consists of simply supported T-beams spanning 42 feet and spaced at 4.5 feet on center. The T-beams contain no transverse steel reinforcement. Additional details of the T-beam are provided in Figures 1 and 2.

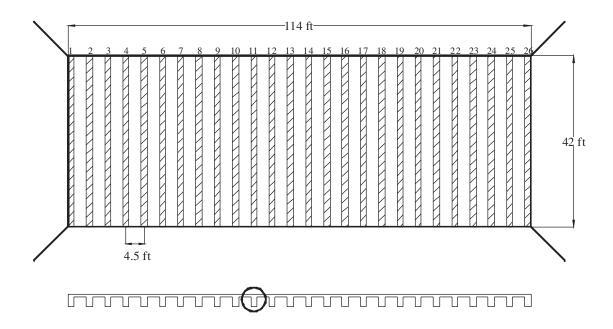


Figure 1. Bridge plan and transverse section.

#### 2. MATERIAL PROPERTIES

The following material properties have been chosen to represent those anticipated in an older bridge for which shear deficiencies might be expected.

#### 2.1. Concrete

Compressive strength 
$$(f_c := 3.0)$$
 ksi

Modulus of elasticity  $(E_c := 33 \cdot (1.5)^{1.5} \sqrt{f_c \cdot 1000})$  ksi

 $(E_c) = 3321$  ksi

$$\beta_{1} := \begin{bmatrix} 0.85 & \text{if } \mathbf{f}_{c} \leq 4 \\ 0.65 & \text{if } \mathbf{f}_{c} \geq 8 \\ \left[ 0.85 - 0.05 \cdot \left( \mathbf{f}_{c} - 4 \right) \right] & \text{otherwise} \end{bmatrix}$$

$$\beta_1 = 0.85$$

# 2.2. Longitudinal Reinforcement

Yield strength  $f_y := 60 \text{ ksi}$ Modulus of elasticity  $E_s := 29000 \text{ ksi}$ 

## 2.3. FRP Reinforcement

Carbon Fiber Sheets are used in this example.

Thickness  $t_f := 0.0065$  in.

Failure strength  $f_{fu} := 550 \text{ ksi}$ 

Modulus of elasticity  $E_f := 33000 \text{ ksi}$ 

Failure strain 
$$\ensuremath{\epsilon_{fu}} \coloneqq \frac{f_{fu}}{E_f}$$
 
$$\ensuremath{\epsilon_{fu}} = 0.017 \text{ in/in}$$

## 3. GEOMETRICAL PROPERTIES

Total Height  $h_T := 37$  in.

Flange Thickness  $h_f := 7$  in.

Width of the web  $b_v := 18$  in.

Effective Width of the Flange  $b_{eff} := 54$  in.

Tensile reinforcement =  $12#11 A_s := 18.72 in^2$ 

Internal shear reinforcement = Not provided  $(A_v := 0.0)$  in<sup>2</sup>

Distance from the extreme compression fiber to the center of the steel at the section d := 32.7 in.

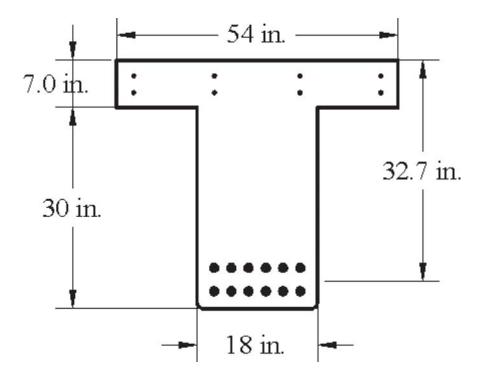


Figure 2. Cross-section of an intermediate beam.

# 4. CALCULATION OF THE FACTORED SHEAR FORCE AND NOMINAL SHEAR RESISTANCE

#### 4.1 Factored Shear Force at the Critical Section

$$V_{u\_crit} := 100 \text{ kips}$$

## 4.2. Calculation of Nominal Shear Resistance

For this example, the simplified approach is followed.

$$(\theta := 45 \text{ deg}) \qquad (\beta := 2)$$

The nominal shear resistance provided by the concrete,  $V_c$ , is calculated in accordance with LRFD Eqn.5.8.3.3-3 as:

Assuming rectangular section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

$$\begin{pmatrix}
c_{c1} := \frac{A_s \cdot f_y}{0.85 \cdot f_c \cdot b_{eff} \cdot \beta_1}
\end{pmatrix} \qquad \qquad (c_{c1}) = 9.6 \text{ in.}$$

$$\begin{pmatrix}
a_{c1} := \beta_1 \cdot c_{c1}
\end{pmatrix} \qquad \qquad (a_{c1}) = 8.16 \text{ in.}$$

Assuming T-beam section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

The effective shear depth  $d_v$  is taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken less than the greater of  $0.9d_o$  or 0.72h (LRFD Article5.8.2.9)

$$\begin{pmatrix} d_{v1} := d - \frac{a_c}{2} \end{pmatrix} \qquad (d_{v2} := 0.9 \cdot d) \qquad (d_{v3} := 0.72 \cdot h_T)$$

$$(d_v := \max(d_{v1}, d_{v2}, d_{v3}))$$

$$(d_v) = 29.4 \text{ in.}$$

The nominal shear resistance provided by the concrete is:

$$V_c := 0.0316 \cdot \beta \cdot \sqrt{f_c} \cdot b_v \cdot d_v \qquad \text{(LRFD Eqn. 5.8.3.3-3)}$$

$$\left(V_c\right) = 58 \text{ kips}$$

The nominal shear resistance provided by the internal steel reinforcement is:

$$V_s := 0$$

The nominal shear resistance provided by the vertical component of prestressing strands is:

$$(V_p := 0)$$

The nominal shear resistance of the member is:

$$V_n := V_c + V_s + V_p$$
 (LRFD Eqn. 5.8.3.3-1)  
 $V_n = 58 \text{ kips}$ 

#### 5. DESIGN OF FRP SHEAR REINFORCEMENT

# 5.1 Check if FRP Reinforcement is Necessary or Not

Strength reduction factor for shear ( $\phi := 0.9$ )

$$\label{eq:check_frp_needed} \mbox{Check\_FRP\_Needed} := \left| \begin{tabular}{ll} "NOT need shear reinforcement" & if $\left( \varphi \cdot V_n \geq V_{u\_crit} \right)$ \\ "NEED shear reinforcement" & otherwise \\ \end{tabular} \right.$$

Check\_FRP\_Needed = "NEED shear reinforcement"

# 5.2 Computation of Required $V_f$

$$V_{\underline{f}\_req} := \frac{V_{\underline{u}\_crit}}{\phi} - V_{\underline{n}}$$

$$V_{f_{req}} = 53.1 \text{ kips}$$

## 5.3 Selection of FRP Strengthening Scheme

U-wrap configuration is used with anchorage systems at the end of the sheets. The FRP sheets will be applied at 90 degrees with respect to the longitudinal axis of the girder as shown in the Figure 3 below. Anchorage systems will be installed at the top end portion of the FRP sheets to increase the effectiveness of FRP shear strengthening. First, the spacing of FRP strips is chosen to meet the maximum spacing requirement. Then, the width of the FRP strips is selected to adjust the amount of FRP strips.

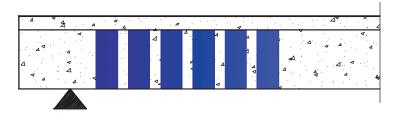


Figure 3. FRP strengthening scheme.

Use number of plies of FRP sheets

 $n_f := 1$ 

Use the width of FRP sheets

 $w_f := 5.5 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f := 18$  in.

Orientation of FRP sheets

 $\alpha_{\rm f} := 90 \deg$ 

Effective depth of FRP sheets  $d_f := d - h_f$ 

$$d_f = 25.7$$
 in.

Check if the selected spacing is acceptable or not

Shear stress on concrete is:

$$\left(v_{u} := \frac{V_{u\_crit} - \phi \cdot V_{p}}{\phi \cdot b_{v} \cdot d_{v}}\right)$$
 (LRFD Eqn. 5.8.2.9-1)

$$(v_{u}) = 0.21 \text{ ksi}$$

The maximum spacing of the transverse reinforcement is:

$$s_{max} := \begin{vmatrix} min(0.8 \cdot d_v, 24) & if v_u < 0.125 \cdot f_c \\ min(0.4 \cdot d_v, 12) & otherwise \end{vmatrix}$$
 (LRFD Eqn. 5.8.2.7-1)  
 $s_{max} = 23.5$ 

# 5.4 Calculation of Shear Resistance of FRP, $V_f$

The FRP reinforcement ratio is:

$$\rho_{f} := \frac{2 \cdot n_{f} \cdot w_{f} \cdot t_{f}}{b_{v} \cdot s_{f}}$$
(Attachment A Eqn. 5.8.3.3-10)
$$(\rho_{f}) = 2.207 \times 10^{-4}$$

The FRP strain reduction factor is:

$$R_f := \min \left[ 4 \cdot \left( \rho_f \cdot E_f \right)^{-0.67}, 1.0 \right]$$
 (Attachment A Eqn. 5.8.3.3-8) 
$$R_f = 1$$

The effective strain of FRP is:

$$\epsilon_{\rm fe}:=R_{\rm f}\cdot\epsilon_{\rm fu} \eqn. 5.8.3.3-7)$$
 
$$\epsilon_{\rm fe}=0.017 \ {\rm in./in.}$$

The effective stress of FRP is:

$$f_{fe} := \varepsilon_{fe} \cdot E_{f}$$
 (Attachment A Eqn. 5.8.3.3-6) 
$$(f_{fe}) = 550 \text{ ksi}$$

The shear contribution of the FRP can be then calculated.

$$\begin{split} \left(V_{f} \coloneqq \rho_{f} \cdot E_{f} \cdot \varepsilon_{fe} \cdot b_{v} \cdot d_{f} \cdot \left(\sin\left(\alpha_{f}\right) + \cos\left(\alpha_{f}\right)\right)\right) & \text{(Attachment A Eqn. 5.8.3.3-5)} \\ \left(V_{f}\right) = 56.1 \text{ kips} \\ V_{f\_{check1}} \coloneqq \left\| \text{"Change FRP Strengthening Scheme"} \quad \text{if } \left(V_{f} < V_{f\_{req}}\right) \\ \text{"Provided FRP Strength Large Enough"} \quad \text{otherwise} \\ V_{f\_{check1}} = \text{"Provided FRP Strength Large Enough"} \\ V_{f\_{check2}} \coloneqq \left\| \text{"Provided FRP amount is adequate"} \quad \text{if } \left(V_{f\_{req}} \le V_{f} < 1.1 \cdot V_{f\_{req}}\right) \\ \text{"Change the FRP amount slightly"} \quad \text{otherwise} \\ \left(V_{f\_{check2}}\right) = \text{"Provided FRP amount is adequate"} \end{split}$$

## 5.5 Calculation of Design Shear Resistance of the Member

The design strength of the member is:

$$\phi V_{n\_total} := \phi \cdot \left( V_c + V_p + V_s + V_f \right)$$

$$\left( \phi V_{n\_total} \right) = 102.722 \text{ kips}$$
(Attachment A Eqn. 5.8.3.3-1)

$$\phi V_{n\_check} := \left\| \text{"Not Good"} \quad \text{if } V_{u\_crit} > \phi V_{n\_total} \right\|$$

$$\text{"OK"} \quad \text{otherwise}$$

$$\left( \phi V_{n\_check} \right) = \text{"OK"}$$

$$Web\_crushing\_limit := 0.25 \cdot f'_c \cdot b_v \cdot d_v + V_p \qquad (LRFD \ Eqn \ 5.8.3.3-2)$$
 
$$Web\_crushing\_limit = 397.3 \ kips$$
 
$$Check\_web\_crushing\_limit := \left\| \text{"OK"} \quad \text{if } \left( V_c + V_s + V_f + V_p \right) \le Web\_crushing\_limit \right.$$
 
$$\left\| \text{"No Good"} \quad \text{otherwise} \right.$$
 
$$Check \ web \ crushing \ limit = \text{"OK"}$$

#### 6. SUMMARY

Externally bonded FRP sheets were designed in this example. The FRP sheets are applied at 90 degrees with respect to the longitudinal axis of the member with the U-wrap configuration as shown in Figure 4. In addition, an anchorage system is installed. The final design is summarized as:

Use number of plies of FRP sheets  $n_f = 1$ 

Use the width of FRP sheets  $w_f = 5.5$  in.

Use the center-to-center spacing of FRP sheets  $s_f = 18$  in.

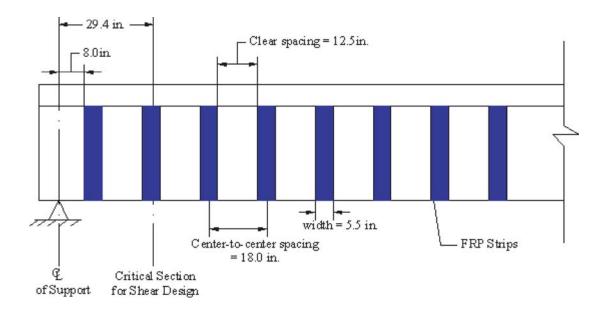


Figure 4. Final design of FRP strengthening.

**DESIGN EXAMPLE 2-1:** RC T-Beam with Internal Transverse Steel Reinforcement Strengthened with FRP in U-wrap Configuration without Anchorage Systems

#### 1. INTRODUCTION

This example demonstrates the design procedures for externally bonded FRP shear reinforcement of an older reinforced concrete (RC) bridge using a U-wrap configuration without anchorage. The bridge consists of simply supported T-beams spanning 42 feet and spaced at 4.5 feet on center. The T-beams contain transverse steel reinforcement spaced at 12 inches on center. Additional details of the T-beam are provided in Figures 1 and 2.

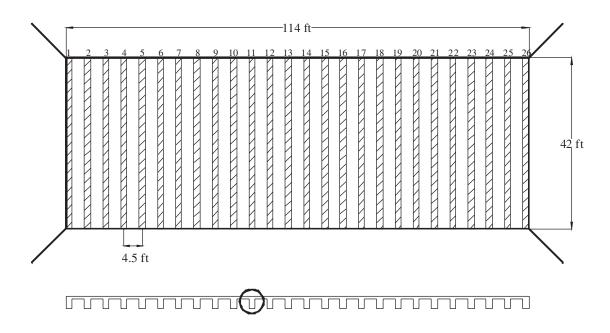


Figure 1. Bridge plan and transverse section.

#### 2. MATERIAL PROPERTIES

The following material properties have been chosen to represent those anticipated in an older bridge for which shear deficiencies might be expected.

#### 2.1. Concrete

Compressive strength  $f'_c := 3.0 \text{ ksi}$ 

Modulus of elasticity 
$$\left(E_c:=33\cdot(1.5)^{1.5}\sqrt{f'_c\cdot 1000}\right)$$
 ksi 
$$\left(E_c\right)=3321 \text{ ksi}$$

$$\beta_{1} := \begin{bmatrix} 0.85 \text{ if } f'_{c} \le 4 \\ \\ 0.65 \text{ if } f'_{c} \ge 8 \\ \\ \left[ 0.85 - 0.05 \cdot \left( f'_{c} - 4 \right) \right] \text{ otherwise} \end{bmatrix}$$

$$\beta_1 = 0.85$$

# 2.2. Longitudinal Reinforcement

Yield strength  $f_y := 60 \text{ ksi}$ Modulus of elasticity  $E_s := 29000 \text{ ksi}$ 

#### 2.3. Internal Steel Shear Reinforcement

Yield strength 
$$f_{yt} := 60 \text{ ksi}$$

## 2.4. FRP Reinforcement

Carbon Fiber Sheets are used in this example.

Thickness  $t_f := 0.0065$  in.

Failure strength  $f_{fu} := 550 \text{ ksi}$ 

Modulus of elasticity  $E_f := 33000 \text{ ksi}$ 

Failure strain 
$$\epsilon_{fu} := \frac{f_{fu}}{E_f}$$
 
$$\epsilon_{fu} = 0.017 \text{ in./in.}$$

## 3. GEOMETRICAL PROPERTIES

Total Height  $h_T := 37$  in.

Flange Thickness  $h_f := 7$  in.

Width of the web  $b_v := 18$  in.

Effective width of the flange  $b_{eff} := 54$  in.

Tensile reinforcement =  $12#11 A_s := 18.72 in.^2$ 

Internal shear reinforcement = #3 at 12 in. spacing

$$A_v := 0.22 \text{ in.}^2$$
  $s_v := 12 \text{ in.}$   $\alpha := 90 \cdot \text{deg}$ 

Distance from the extreme compression fiber to the center of the steel at the section d := 32.7 in.

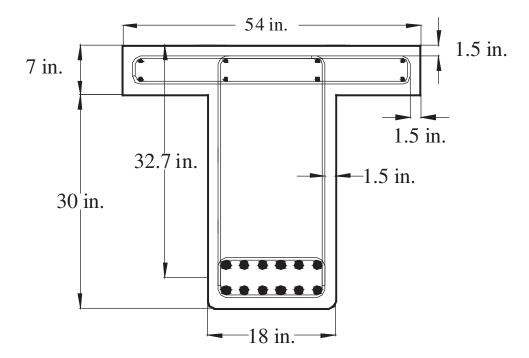


Figure 2. Cross-section of an intermediate beam.

# 4. CALCULATION OF THE FACTORED SHEAR FORCE AND NOMINAL SHEAR RESISTANCE

## 4.1 Factored Shear Force at the Critical Section

$$V_{u \text{ crit}} := 120 \text{ kips}$$

#### 4.2. Calculation of Nominal Shear Resistance

For this example, the simplified approach is followed.

$$(\theta := 45 \text{ deg})$$
  $(\beta := 2)$ 

The nominal shear resistance provided by the concrete,  $V_c$ , is calculated in accordance with LRFD Eqn.5.8.3.3-3 as:

Assuming rectangular section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

$$\begin{pmatrix} c_{c1} \coloneqq \frac{A_s \cdot f_y}{0.85 \cdot f'_c \cdot b_{eff} \cdot \beta_1} \end{pmatrix}$$
 
$$\begin{pmatrix} c_{c1} \end{pmatrix} = 9.6 \text{ in.}$$
 
$$\begin{pmatrix} a_{c1} \coloneqq \beta_1 \cdot c_{c1} \end{pmatrix}$$
 
$$\begin{pmatrix} a_{c1} \end{pmatrix} = 8.16 \text{ in.}$$

Assuming T-beam section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

The effective shear depth  $d_v$  is taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken less than the greater of  $0.9d_e$  or 0.72h (LRFD Article5.8.2.9)

$$\begin{pmatrix} d_{v1} := d - \frac{a_c}{2} \\ d_{v2} := 0.9 \cdot d \end{pmatrix} \begin{pmatrix} d_{v3} := 0.72 \cdot h_T \end{pmatrix}$$

$$\begin{pmatrix} d_v := \max (d_{v1}, d_{v2}, d_{v3}) \\ d_v = 29.43 \text{ in.} \end{pmatrix}$$

The nominal shear resistance provided by the concrete is:

$$V_c := 0.0316 \cdot \beta \cdot \sqrt{f'_c} \cdot b_v \cdot d_v$$
 (LRFD Eqn. 5.8.3.3-3)  
$$\left(V_c\right) = 57.988 \text{ kips}$$

The nominal shear resistance provided by the internal steel reinforcement is:

$$V_{s} := \frac{A_{v} \cdot f_{yt} \cdot d_{v} \cdot (\cot(\theta) + \cot(\alpha)) \sin(\alpha)}{s_{v}}$$

$$V_{s} = 32.373 \text{ kips}$$
(LRFD Eqn. 5.8.3.3-4)

The nominal shear resistance provided by the vertical component of prestressing strands is:

$$(V_p := 0)$$

The nominal shear resistance of the member is:

$$V_n := V_c + V_s + V_p$$
 (LRFD Eqn. 5.8.3.3-1)  
 $V_n = 90.36 \text{ kips}$ 

#### 5. DESIGN OF FRP SHEAR REINFORCEMENT

# 5.1 Check if FRP Reinforcement is Necessary or Not

Strength reduction factor for shear ( $\phi := 0.9$ )

Check\_FRP\_Needed := 
$$\begin{subarray}{ll} "NOT need shear reinforcement" & if  $\begin{subarray}{ll} $\phi \cdot V_n \geq V_{u\_crit} \end{subarray} \begin{subarray}{ll} "NEED shear reinforcement" & otherwise \end{subarray}$ 

$$\begin{subarray}{ll} Check\_FRP\_Needed = "NEED shear reinforcement" & otherwise \end{subarray}$$$$

# 5.2 Computation of Required $V_f$

$$V_{f\_req} := \frac{V_{u\_crit}}{\phi} - V_{n}$$

$$V_{f\_req} = 43 \text{ kips}$$

## 5.3 Selection of FRP Strengthening Scheme

U-wrap configuration is used with anchorage systems at the end of the sheets. The FRP sheets will be applied at 90 degrees with respect to the longitudinal axis of the girder as shown in the Figure 3 below. First, the spacing of FRP strips is chosen to meet the maximum spacing requirement. Then, the width of the FRP strips is selected to adjust the amount of FRP strips.

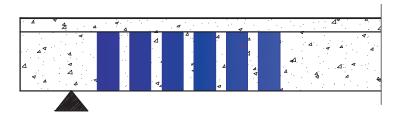


Figure 3. FRP strengthening scheme.

Use number of plies of FRP sheets

 $n_f := 1$ 

Use the width of FRP sheets

 $w_c := 4 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f := 12$  in.

Orientation of FRP sheets

 $\alpha_{\rm f} := 90 \deg$ 

Effective depth of FRP sheets  $d_f := d - h_f$ 

$$d_f = 25.7$$
 in.

Check if the selected spacing is acceptable

Shear stress on concrete is:

$$\left(v_{u} := \frac{V_{u\_crit} - \phi \cdot V_{p}}{\phi \cdot b_{v} \cdot d_{v}}\right)$$

$$\left(v_{u}\right) = 0.252 \text{ ksi}$$
(LRFD Eqn. 5.8.2.9-1)

The maximum spacing of the transverse reinforcement is:

$$\mathbf{s}_{\text{max}} \coloneqq \left| \begin{array}{l} \min \left( 0.8 \cdot \mathbf{d}_{\text{v}}, \, 24 \right) \text{ if } \mathbf{v}_{\text{u}} < 0.125 \cdot \mathbf{f'}_{\text{c}} \\ \min \left( 0.4 \cdot \mathbf{d}_{\text{v}}, \, 12 \right) \text{ otherwise} \end{array} \right. \tag{LRFD Eqn. 5.8.2.7-1}$$

$$s_{max} = 23.5$$

# 5.4 Calculation of Shear Resistance of FRP, $V_{\rm f}$

The FRP reinforcement ratio is:

$$\rho_{f} := \frac{2 \cdot n_{f} \cdot w_{f} \cdot t_{f}}{b_{v} \cdot s_{f}}$$
(Attachment A Eqn. 5.8.3.3-10)
$$\left(\rho_{f}\right) = 2.407 \times 10^{-4}$$

The FRP strain reduction factor is:

$$R_{f} := \min \left[ 3 \cdot \left( \rho_{f} \cdot E_{f} \right)^{-0.67}, 1.0 \right]$$
 (Attachment A Eqn. 5.8.3.3-9) 
$$R_{f} = 0.748$$

The effective strain of FRP is:

$$\epsilon_{\rm fe} := \min \left( R_{\rm f} \cdot \epsilon_{\rm fu}, \, 0.012 \right) \tag{Attachment A Eqn. 5.8.3.3-7}$$
 
$$\epsilon_{\rm fe} = 0.012 \text{ in./in.}$$

The effective stress of FRP is:

$$f_{fe} := \varepsilon_{fe} \cdot E_f$$
 (Attachment A Eqn. 5.8.3.3-6)  
 $\left(f_{fe}\right) = 396 \text{ ksi}$ 

The shear contribution of the FRP can be then calculated.

$$\begin{split} V_f &:= \rho_f \cdot E_f \cdot \epsilon_{fe} \cdot b_v \cdot d_f \cdot \left( \sin \left( \alpha_f \right) + \cos \left( \alpha_f \right) \right) & \text{(Attachment A Eqn. 5.8.3.3-5)} \\ \left( V_f \right) &= 44.1 \text{ kips} \\ V_{f\_check1} &:= \left\| \text{"Change FRP Strengthening Scheme"} \quad \text{if } \left( V_f < V_{f\_req} \right) \\ & \text{"Provided FRP Strength Large Enough"} \quad \text{otherwise} \\ V_{f\_check1} &= \text{"Provided FRP Strength Large Enough"} \\ V_{f\_check2} &:= \left\| \text{"Provided FRP amount is adequate"} \quad \text{if } \left( V_{f\_req} \leq V_f < 1.1 \cdot V_{f\_req} \right) \\ & \text{"Change the FRP amount slightly"} \quad \text{otherwise} \\ & \left( V_{f\_check2} \right) = \text{"Provided FRP amount is adequate"} \end{split}$$

# **5.5** Calculation of Design Shear Resistance of the Member

The design strength of the member is:

$$\phi V_{n\_total} := \phi \cdot \left( V_c + V_p + V_s + V_f \right)$$
 (Attachment A Eqn. 5.8.3.3-1) 
$$\left( \phi V_{n\_total} \right) = 121.02 \text{ kips}$$

$$\begin{split} \phi V_{n\_check} &:= \left\| \text{"Not Good"} & \text{if } V_{u\_crit} > \phi V_{n\_total} \right. \\ & \left( \phi V_{n\_total} \right) = \text{"OK"} \\ \\ & \left( \phi V_{n\_total} \right) = \text{"OK"} \\ \\ & \text{Web\_crushing\_limit} := 0.25 \cdot \text{f'}_c \cdot \text{b}_v \cdot \text{d}_v + V_p \quad \text{(LRFD Eqn. 5.8.3.3-2)} \\ & \text{Web\_crushing\_limit} = 397.3 \text{ kips} \\ & \text{Check\_web\_crushing\_limit} := \left\| \text{"OK"} \quad \text{if } \left( V_c + V_s + V_f + V_p \right) \leq \text{Web\_crushing\_limit} \right. \\ & \left\| \text{"No Good"} \quad \text{otherwise} \right. \\ & \text{Check\_web\_crushing\_limit} = \text{"OK"} \end{split}$$

#### 6. SUMMARY

Externally bonded FRP sheets were designed in this example. The FRP sheets are applied at 90 degrees with respect to the longitudinal axis of the member with the U-wrap configuration and without anchorage systems as shown in Figure 4. The final design is summarized as:

Use number of plies of FRP sheets  $n_f = 1$ 

Use the width of FRP sheets  $w_f = 4 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f = 12$  in.

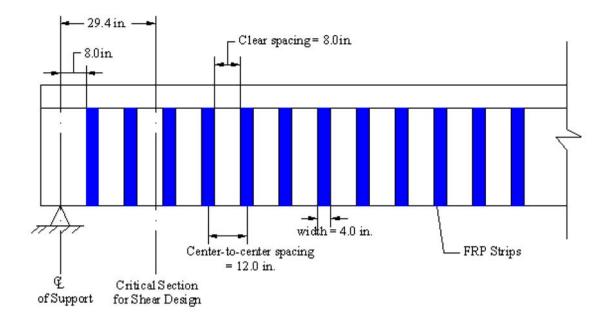


Figure 4. Final design of FRP strengthening.

**DESIGN EXAMPLE 2-2:** RC T-Beam with Internal Transverse Steel Reinforcement Strengthened with FRP in U-wrap Configuration with an Anchorage System

## 1. INTRODUCTION

This example demonstrates the design procedures for externally bonded FRP shear reinforcement of an older reinforced concrete (RC) bridge using a U-wrap configuration with anchorage. The bridge consists of simply supported T-beams spanning 42 feet and spaced at 4.5 feet on center. The T-beams contain transverse steel reinforcement spaced at 12 inches on center. Additional details of the T-beam are provided in Figures 1 and 2.

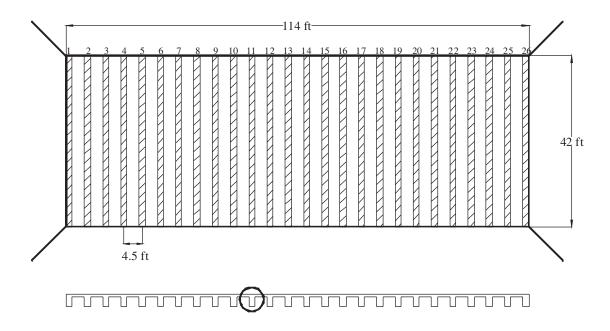


Figure 1. Bridge plan and transverse section.

#### 2. MATERIAL PROPERTIES

The following material properties have been chosen to represent those anticipated in an older bridge for which shear deficiencies might be expected.

#### 2.1. Concrete

Compressive strength  $f_c := 3.0 \text{ ksi}$ 

Modulus of elasticity 
$$\left(E_c:=33\cdot(1.5)^{1.5}\sqrt{f_c'\cdot1000}\right)$$
 ksi 
$$\left(E_c\right)=3321 \text{ ksi}$$

$$\beta_1 := \begin{bmatrix} 0.85 \text{ if } f_c \le 4 \\ \\ 0.65 \text{ if } f_c \ge 8 \\ \\ \left[ 0.85 - 0.05 \cdot \left( f_c - 4 \right) \right] \text{ otherwise} \end{bmatrix}$$

$$\beta_1 = 0.85$$

# 2.2. Longitudinal Reinforcement

Yield strength  $f_y := 60 \text{ ksi}$ Modulus of elasticity  $E_s := 29000 \text{ ksi}$ 

#### 2.3. Internal Steel Shear Reinforcement

Yield strength  $f_{yt} := 60 \text{ ksi}$ 

### 2.4. FRP Reinforcement

Carbon Fiber Sheets are used in this example.

Thickness  $t_f := 0.0065$  in. Failure strength  $f_{fu} := 550$  ksi

Modulus of elasticity  $E_f := 33000 \text{ ksi}$ 

Failure strain 
$$\epsilon_{fu}^{}:=\frac{f_{fu}^{}}{E_{f}^{}}$$
 
$$\epsilon_{fu}^{}=0.017 \text{ in./in.}$$

#### 3. GEOMETRICAL PROPERTIES

Total Height  $h_T := 37$  in.

Flange Thickness  $h_f := 7$  in.

Width of the web  $b_y := 18$  in.

Effective Width of the Flange  $b_{eff} := 54$  in.

Tensile reinforcement =  $12#11 A_s := 18.72 \text{ in.}^2$ 

Internal shear reinforcement = #3 at 12 in. spacing

$$A_v := 0.22 \text{ in}^2$$
  $s_v := 12 \text{ in.}$   $\alpha := 90 \text{ deg}$ 

Distance from the extreme compression fiber to the center of the steel at the section d := 32.7 in.

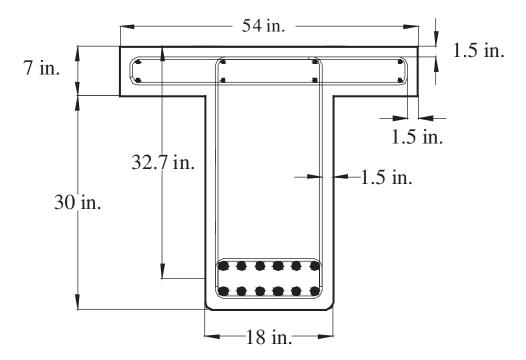


Figure 2. Cross-section of an intermediate beam.

# 4. CALCULATION OF THE FACTORED SHEAR FORCE AND NOMINAL SHEAR RESISTANCE

#### 4.1 Factored Shear Force at the Critical Section

$$V_{u\_crit} := 120 \text{ kips}$$

## 4.2. Calculation of Nominal Shear Resistance

For this example, the simplified approach is followed.

$$(\theta := 45 \text{ deg}) \qquad (\beta := 2)$$

The nominal shear resistance provided by the concrete,  $V_c$ , is calculated in accordance with LRFD Eqn.5.8.3.3-3 as:

Assuming rectangular section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

Assuming T-beam section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

The effective shear depth  $d_v$  is taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken less than the greater of  $0.9d_e$  or 0.72h (LRFD Article5.8.2.9)

$$\begin{pmatrix} d_{v1} := d - \frac{a_c}{2} \\ d_{v2} := 0.9 \cdot d \end{pmatrix} \begin{pmatrix} d_{v3} := 0.72 \cdot h_T \end{pmatrix}$$

$$\begin{pmatrix} d_v := \max (d_{v1}, d_{v2}, d_{v3}) \\ d_v \end{pmatrix} = 29.4 \text{ in.}$$

The nominal shear resistance provided by the concrete is:

$$V_c := 0.0316 \cdot \beta \cdot \sqrt{f'_c} \cdot b_v \cdot d_v$$
 (LRFD Eqn. 5.8.3.3-3) 
$$\left(V_c\right) = 58 \text{ kips}$$

The nominal shear resistance provided by the internal steel reinforcement is:

$$V_s := \frac{A_v \cdot f_{yt} \cdot d_v \cdot (\cot(\theta) + \cot(\alpha)) \sin(\alpha)}{s_v}$$
 (LRFD Eqn. 5.8.3.3-4)  
$$V_s = 32.4 \text{ kips}$$

The nominal shear resistance provided by the vertical component of prestressing strands is:

$$\left(V_{p} := 0\right)$$

The nominal shear resistance of the member is:

$$V_n := V_c + V_s + V_p$$
 (LRFD Eqn. 5.8.3.3-1)  
 $V_n = 90.4 \text{ kips}$ 

#### 5. DESIGN OF FRP SHEAR REINFORCEMENT

# 5.1 Check if FRP Reinforcement is Necessary or Not

Strength reduction factor for shear ( $\phi := 0.9$ )

# 5.2 Computation of Required $V_f$

$$V_{f\_req} := \frac{V_{u\_crit}}{\phi} - V_{n}$$

$$V_{f\_req} = 43 \text{ kips}$$

#### **5.3** Selection of FRP Strengthening Scheme

U-wrap configuration is used with anchorage systems at the end of the sheets. The FRP sheets will be applied at 90 degrees with respect to the longitudinal axis of the girder as shown in the Figure 3 below. Anchorage systems will be installed at the top end portion of the FRP sheets to increase the effectiveness of FRP shear strengthening. First, the spacing of FRP strips is chosen to meet the maximum spacing requirement. Then, the width of the FRP strips is selected to adjust the amount of FRP strips.

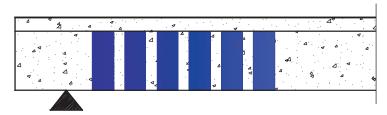


Figure 3. FRP strengthening scheme.

Use number of plies of FRP sheets

 $n_f := 1$ 

Use the width of FRP sheets

 $W_{\epsilon} := 4 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f := 16$  in.

Orientation of FRP sheets

 $\alpha_{\rm f} := 90 \deg$ 

Effective depth of FRP sheets  $d_f := d - h_f$ 

$$d_f = 25.7$$
 in.

Check if the selected spacing is acceptable or not

Shear stress on concrete is:

$$\left(v_{u} := \frac{V_{u\_crit} - \phi \cdot V_{p}}{\phi \cdot b_{v} \cdot d_{v}}\right)$$

$$\left(v_{u}\right) = 0.252 \text{ ksi}$$
(LRFD Eqn. 5.8.2.9-1)

The maximum spacing of the transverse reinforcement is:

$$s_{\text{max}} := \left| \begin{array}{ll} \min \! \left( 0.8 \cdot d_{_{\text{\tiny V}}}, \, 24 \right) & \text{if } v_{_{\text{\tiny U}}} < 0.125 \cdot f'_{_{\text{\tiny C}}} \\ \min \! \left( 0.4 \cdot d_{_{\text{\tiny V}}}, \, 12 \right) & \text{otherwise} \end{array} \right. \tag{LRFD Eqn. 5.8.2.7-1}$$

$$s_{\text{max}} = 23.5$$

# 5.4 Calculation of Shear Resistance of FRP, $V_{\rm f}$

The FRP reinforcement ratio is:

$$\rho_{f} := \frac{2 \cdot n_{f} \cdot w_{f} \cdot t_{f}}{b_{v} \cdot s_{f}}$$

$$(Attachment A Eqn. 5.8.3.3-10)$$

$$(\rho_{f}) = 1.806 \times 10^{-4}$$

The FRP strain reduction factor is:

$$R_f := \min \left[ 4 \cdot \left( \rho_f \cdot E_f \right)^{-0.67}, \ 1.0 \right] \qquad \text{(Attachment A Eqn. 5.8.3.3-8)}$$
 
$$R_f = 1$$

The effective strain of FRP is:

$$\epsilon_{\rm fe} := R_{\rm f} \cdot \epsilon_{\rm fu} \qquad \qquad ({\rm Attachment~A~Eqn.~5.8.3.3-7})$$
 
$$\epsilon_{\rm fe} = 0.017~{\rm in./in.}$$

The effective stress of FRP is:

$$f_{fe} := \varepsilon_{fe} \cdot E_{f}$$
 (Attachment A Eqn. 5.8.3.3-6) 
$$\left(f_{fe}\right) = 550 \text{ ksi}$$

The shear contribution of the FRP can be then calculated.

$$\begin{split} \left(V_f \coloneqq \rho_f \cdot E_f \cdot \epsilon_{fe} \cdot b_v \cdot d_f \cdot \left(\sin\left(\alpha_f\right) + \cos\left(\alpha_f\right)\right)\right) & \quad \text{(Attachment A Eqn. 5.8.3.3-5)} \\ \left(V_f\right) = 45.9 \text{ kips} \\ V_{f\_check1} \coloneqq \left\| \text{"Change FRP Strengthening Scheme"} \quad \text{if } \left(V_f < V_{f\_req}\right) \\ \text{"Provided FRP Strength Large Enough"} \quad \text{otherwise} \\ V_{f\_check1} = \text{"Provided FRP Strength Large Enough"} \\ V_{f\_check2} \coloneqq \left\| \text{"Provided FRP amount is adequate"} \quad \text{if } \left(V_{f\_req} \le V_f < 1.1 \cdot V_{f\_req}\right) \\ \text{"Change the FRP amount slightly"} \quad \text{otherwise} \\ \left(V_{f\_check2}\right) = \text{"Provided FRP amount is adequate"} \end{split}$$

# 5.5 Calculation of Design Shear Resistance of the Member

The design strength of the member is:

$$\begin{split} \phi V_{n\_total} &:= \phi \cdot \left( V_c + V_p + V_s + V_f \right) & \text{(Attachment A Eqn. 5.8.3.3-1)} \\ & \left( \phi V_{n\_total} \right) = 122.7 \text{ kips} \\ & \phi V_{n\_check} := \left\| \text{"Not Good"} \quad \text{if } V_{u\_crit} > \phi V_{n\_total} \right. \\ & \left. \text{"OK"} \quad \text{otherwise} \right. \\ & \left( \phi V_{n\_check} \right) = \text{"OK"} \end{split}$$

 $\label{eq:web_crushing_limit} Web\_crushing\_limit := 0.25 \cdot f'_c \cdot b_v \cdot d_v + V_p \qquad (LRFD \ Eqn. \ 5.8.3.3-2)$   $Web\_crushing\_limit = 397.3 \ kips$   $Check\_web\_crushing\_limit := \left\| \ "OK" \qquad if \left( V_c + V_s + V_f + V_p \right) \le Web\_crushing\_limit \right.$   $\left\| \ "No \ Good" \qquad otherwise \right.$   $Check\_web\_crushing\_limit = "OK"$ 

## 6. SUMMARY

Externally bonded FRP sheets were designed in this example. The FRP sheets are applied at 90 degrees with respect to the longitudinal axis of the member with the U-wrap configuration as shown in Figure 4. In addition, an anchorage system is installed. The final design is summarized as:

Use number of plies of FRP sheets  $n_f = 1$ 

Use the width of FRP sheets  $w_f = 4 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f = 16$  in.

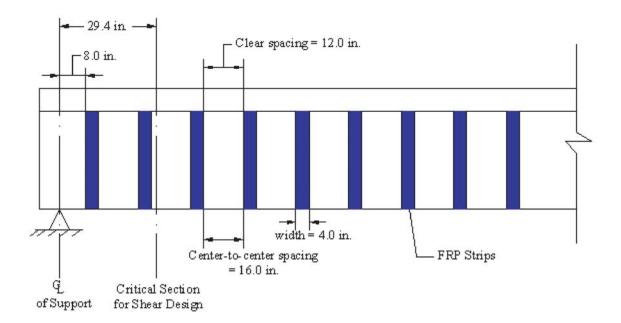
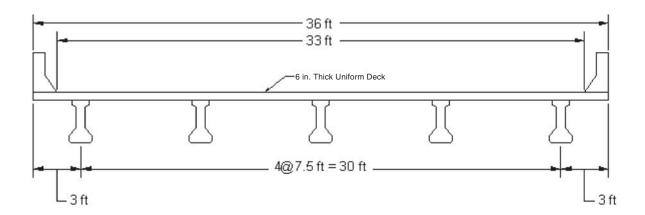


Figure 4. Final design of FRP strengthening.

**DESIGN EXAMPLE 3-1:** PC I-Beam with Internal Transverse Steel Reinforcement Strengthened with FRP in U-wrap Configuration without Anchorage Systems

# 1. INTRODUCTION

This example demonstrates the design procedures for externally bonded FRP shear reinforcement of a prestressed I-beam bridge using a U-wrap configuration without anchorage. The bridge consists of five simply supported pretensioned I-beams spanning 42 feet and spaced at 7.5 feet on center. The I-beams are lightly reinforced with transverse steel reinforcement. Additional details of the bulb-tees are provided in Figures 1 and 2.



# (a) Prestressed I-Beam Bridge Deck Cross-Section

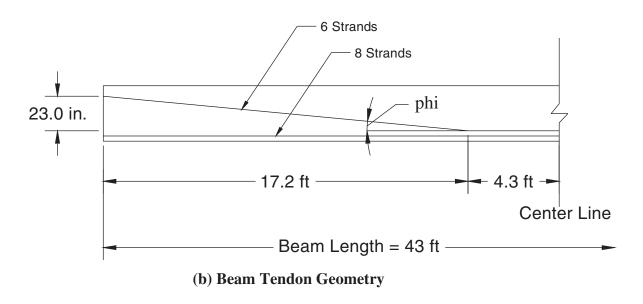


Figure 1. AASHTO bulb-tee bridge deck bridge (Ref. PCI Bridge Design Manual).

## 2. MATERIAL PROPERTIES

## 2.1. Concrete

# **2.1.1 Deck**

Compressive strength  $f'_{cd} := 4.0 \text{ ksi}$ 

Modulus of elasticity 
$$E_{cd} := 33 \cdot (1.5)^{1.5} \sqrt{f'_{cd} \cdot 1000}$$
 ksi

$$E_{cd} = 3834 \text{ ksi}$$

$$\beta_{1d} := \begin{bmatrix} 0.85 \text{ if } f'_{cd} \le 4 \\ \\ 0.65 \text{ if } f'_{cd} \ge 8 \\ \\ \left[ 0.85 - 0.05 \cdot \left( f'_{cd} - 4 \right) \right] \text{ otherwise} \end{bmatrix}$$

$$\beta_{1d} = 0.85$$

## 2.1.1 I-Beam

Compressive strength  $f'_{cb} := 7.0 \text{ ksi}$ 

Modulus of elasticity 
$$E_{cb} := 33 \cdot (1.5)^{1.5} \sqrt{f'_{cb} \cdot 1000}$$
 ksi

$$E_{cb} = 5072 \text{ ksi}$$

$$\beta_{1b} := \begin{bmatrix} 0.85 \text{ if } f'_{cb} \le 4 \\ \\ 0.65 \text{ if } f'_{cb} \ge 8 \\ \\ \left[ 0.85 - 0.05 \cdot \left( f'_{cb} - 4 \right) \right] \text{ otherwise} \end{bmatrix}$$

$$\beta_{1b} = 0.7$$

## 2.2. Prestressing Strands

Specified tensile strength  $f_{pu} := 270 \text{ ksi}$ 

Yield strength  $f_{pv} := 243 \text{ ksi}$ 

Modulus of elasticity  $E_{ps} := 28500 \text{ ksi}$ 

Diameter = 0.5 in.

Total Area of the 14 strands  $A_{ps} := 2.142 \text{ in.}^2$ 

k := 0.28 for low-relaxation steel

## 2.3. Internal Steel Shear Reinforcement

Yield strength  $f_{vt} := 60 \text{ ksi}$ 

#### 2.4. FRP Reinforcement

Carbon Fiber Sheets are used in this example.

Thickness  $t_f := 0.0065$  in.

Failure strength  $f_{fu} := 550 \text{ ksi}$ 

Modulus of elasticity  $E_f := 33000 \text{ ksi}$ 

Failure strain 
$$\epsilon_{fu} \coloneqq \frac{f_{fu}}{E_f}$$

$$\varepsilon_{\text{fu}} = 0.017$$
 in./in.

# 3. GEOMETRICAL PROPERTIES

Total height including deck slab  $h_T := 38$  in.

Flange thickness  $h_f := 6$  in.

Width of the web  $b_v := 7$  in.

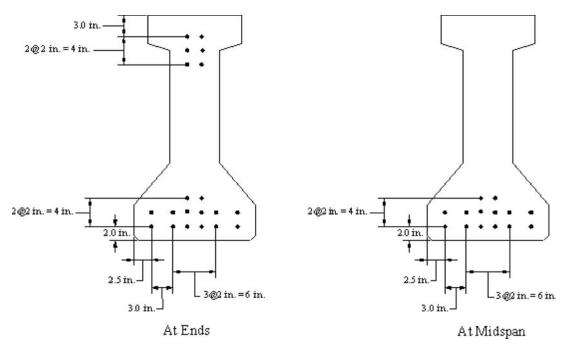
Effective width of the Flange  $b_{eff} := 79.0$  in.

Internal shear reinforcement = #3 at 12 in. spacing

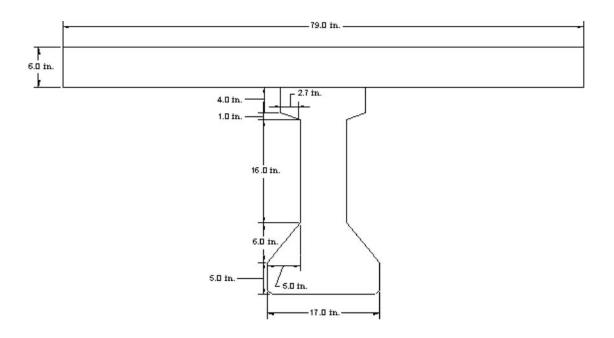
$$A_v := 0.22 \text{ in.}^2$$
  $s_v := 12 \text{ in.}$   $\alpha := 90 \cdot \text{deg}$ 

$$s_v := 12 \text{ in}$$

$$\alpha := 90 \cdot \deg$$



(a) I-Beam Prestressing Pattern.



(b) Cross-Section of an Intermediate Beam

Figure 2. Cross-section of an intermediate beam.

# 4. CALCULATION OF THE FACTORED SHEAR FORCE AND NOMINAL SHEAR RESISTANCE

#### 4.1 Factored Shear Force at the Critical Section

$$V_{u \text{ crit}} := 100 \text{ kips}$$

#### 4.2. Calculation of Nominal Shear Resistance

For this example, the simplified approach is followed.

$$\theta := 45 \cdot \deg \quad \beta := 2$$

The nominal shear resistance provided by the concrete,  $V_c$ , is calculated in accordance with LRFD Eqn.5.8.3.3-3 as:

The distance from the extreme compression fiber to the center of gravity of the strands at the midspan:

$$d_p := 34.6 \text{ in.}$$

Assuming rectangular section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

$$c_{c} := \frac{A_{ps} \cdot f_{pu}}{0.85 \cdot f'_{cd} \cdot b_{eff} \cdot \beta_{1d} + k \cdot A_{ps} \cdot \frac{f_{pu}}{d_{p}}}$$

$$\left(c_{c}\right) = 2.482 \text{ in.}$$

$$a_{c} := \beta_{1d} \cdot c_{c}$$

$$\left(a_{c}\right) = 2.11 \text{ in.}$$

$$\left(\text{check}\_a_{c} := \left\|\text{"Assumption is correct"} \quad \text{if } \left(a_{c} \ge h_{f}\right)\right\|$$
"Not behave as rectangular" otherwise 
$$\left(\text{check}\_a_{c}\right) = \text{"Assumption is correct"}$$

The effective shear depth  $d_v$  is taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken to be less than the greater of  $0.9d_e$  or 0.72h (LRFD Article5.8.2.9).

Since some of the strands are harped, the effective depth varies point-to-point. However, the effective depth must be calculated at the critical section in shear, which is not yet determined; therefore, an iterative procedure is required. For this example, only the final cycle of the iteration is shown.

Assume  $d_v d_v trial := 27.36 in.$ 

Calculate the distance from the extreme compression face to the center of gravity of the strand,  $d_e$  at the location,  $d_g$  away from the centerline of the support.

$$\mathbf{e}_{\mathrm{tr}} \coloneqq \frac{2 \cdot 4 + 4 \cdot 4 + \left[\frac{23}{206.4} \left(206.4 - \mathbf{d}_{\mathbf{v}\_\mathrm{trial}}\right) + 2\right] \cdot 2 + \left[\frac{23}{206.4} \left(206.4 - \mathbf{d}_{\mathbf{v}\_\mathrm{trial}}\right) + 4\right] \cdot 2 + \left[\frac{23}{206.4} \left(206.4 - \mathbf{d}_{\mathbf{v}\_\mathrm{trial}}\right) + 6\right] \cdot 2}{6 + 6 + 2}$$

$$d_e := h_T - e_{tr}$$

$$d_{a} = 26.021$$
 in.

Determine 
$$d_v \ d_{v1} := d_e - \frac{a_c}{2}$$
  $d_{v2} := 0.9 \cdot d_e$   $\left(d_{v3} := 0.72 \cdot h_T\right)$ 

$$\left(d_{v_{-}max} := \max\left(d_{v1}, d_{v2}, d_{v3}\right)\right)$$

$$\left(d_{v_{-}} := \max\left(d_{v_{-} \max}, 0.5 \cdot d_{v_{-} \max} \cdot \cot(\theta)\right)\right)$$

Final  $d_{v}$   $(d_{v}) = 27.36 \text{ in.}$ 

Check\_dv1 := 
$$|"OK" ext{ if } 0.995 \le \frac{d_{v_trial}}{d_v} \le 1.005$$
  
"Try Again" otherwise

$$Check_dv1 = "OK"$$

$$Check\_dv2 := \left| \begin{array}{ll} "OK" & \text{if } \frac{d_v}{b_v} \leq 4 \\ \\ "NOT \ GOOD" & \text{otherwise} \end{array} \right|$$

$$Check_dv2 = "OK"$$

The nominal shear resistance provided by the concrete is:

$$V_c := 0.0316 \cdot \beta \cdot \sqrt{f'_c} \cdot b_v \cdot d_v$$
 (LRFD Eqn. 5.8.3.3-3) 
$$(V_c) = 32 \text{ kips}$$

The nominal shear resistance provided by the internal steel reinforcement is:

$$V_{s} := \frac{A_{v} \cdot f_{yt} \cdot d_{v} \cdot (\cot(\theta) + \cot(\alpha)) \sin(\alpha)}{s_{v}}$$

$$V_{s} = 30.1 \text{ kips}$$
(LRFD Eqn. 5.8.3.3-4)

Harped tendon force = 6 x 0.153 x 149.0 = 136.8 kips (assuming  $f_{pe}$  = 149 ksi) slope of the tendons  $\psi$  := 0.111

$$V_p := 136.8 \cdot \psi$$
  $V_p = 15.2 \text{ kips}$ 

The nominal shear resistance of the member is:

$$V_n := V_c + V_s + V_p$$
 (LRFD Eqn. 5.8.3.3-1)  
 $V_p = 77.3 \text{ kips}$ 

#### 5. DESIGN OF FRP SHEAR REINFORCEMENT

### 5.1 Check if FRP Reinforcement is Necessary or Not

Strength reduction factor for shear ( $\phi := 0.9$ )

$$\label{eq:check_frp_needed} \mbox{Check\_FRP\_Needed} := \begin{bmatrix} "NOT \ need \ shear \ reinforcement" & if \left( \varphi \cdot V_n \geq V_{u\_crit} \right) \\ "NEED \ shear \ reinforcement" & otherwise \\ \end{bmatrix}$$

Check FRP Needed = "NEED shear reinforcement"

# 5.2 Computation of Required $V_f$

$$V_{f\_req} := \frac{V_{u\_crit}}{\phi} - V_n$$

$$V_{f_{req}} = 33.8 \text{ kips}$$

### 5.3 Selection of FRP Strengthening Scheme

U-wrap configuration is used with anchorage systems at the end of the sheets. The FRP sheets will be applied at 90 degrees with respect to the longitudinal axis of the girder as shown in the Figure 3 below. First, the spacing of FRP strips is chosen to meet the maximum spacing requirement. Then, the width of the FRP strips is selected to adjust the amount of FRP strips.

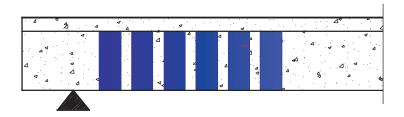


Figure 3. FRP strengthening scheme.

 $\begin{aligned} &\text{Use number of plies of FRP sheets} & &n_f := 1 \\ &\text{Use the width of FRP sheets} & &w_f := 8 \text{ in.} \end{aligned}$ 

Use the center-to-center spacing of FRP sheets  $s_f := 12$  in.

Orientation of FRP sheets  $\alpha_f := 90 \text{ deg}$ 

Effective depth of FRP sheets  $d_f := d_p - h_f$  $d_f = 28.6 \text{ in.}$ 

Check if the selected spacing is acceptable or not

Shear stress on concrete is:

$$\left(v_{u} := \frac{V_{u\_crit} - \phi \cdot V_{p}}{\phi \cdot b_{v} \cdot d_{v}}\right)$$

$$\left(v_{u}\right) = 0.501 \text{ ksi}$$
(LRFD Eqn. 5.8.2.9-1)

The maximum spacing of the transverse reinforcement is:

$$s_{\text{max}} := \left| \begin{array}{l} \min \left( 0.8 \cdot d_{\text{v}}, \, 24 \right) \text{ if } v_{\text{u}} < 0.125 \cdot f'_{\text{cb}} \\ \min \left( 0.4 \cdot d_{\text{v}}, \, 12 \right) \text{ otherwise} \end{array} \right. \tag{LRFD Eqn. 5.8.2.7-1}$$
 
$$s_{\text{max}} = 21.9$$

$$\label{eq:Check_Spacing} \mbox{Check\_Spacing} := \left\| \mbox{"Acceptable"} & \mbox{if } s_f \leq s_{max} \right. \\ \mbox{"NOT\_Acceptable\_Change\_the\_Spacing"} & \mbox{otherwise} \\ \mbox{Check\_Spacing} = \mbox{"Acceptable"} \\ \mbox{}$$

# 5.4 Calculation of Shear Resistance of FRP, $V_{\rm f}$

The FRP reinforcement ratio is:

$$\begin{split} \rho_f &\coloneqq \frac{2 \cdot n_f \cdot w_f \cdot t_f}{b_v \cdot s_f} \\ \left( \rho_f \right) &= 1.238 \times 10^{-3} \end{split} \tag{Attachment A Eqn. 5.8.3.3-10}$$

The FRP strain reduction factor is:

$$R_f := \min \left[ 3 \cdot \left( \rho_f \cdot E_f \right)^{-0.67}, 1.0 \right]$$
 (Attachment A Eqn. 5.8.3.3-9) 
$$R_f = 0.25$$

The effective strain of FRP is:

$$\begin{split} \epsilon_{fe} &:= min\left(R_{f} \cdot \epsilon_{fu}, \, 0.012\right) & \text{(Attachment A Eqn. 5.8.3.3-7)} \\ \epsilon_{fe} &= 4.163 \times 10^{-3} \text{ in./in.} \end{split}$$

The effective stress of FRP is:

$$f_{fe} := \varepsilon_{fe} \cdot E_{f}$$
 (Attachment A Eqn. 5.8.3.3-6)  
 $\left(f_{fe}\right) = 137.4 \text{ ksi}$ 

The shear contribution of the FRP can be then calculated.

$$\begin{split} \left(V_f \coloneqq \rho_f \cdot E_f \cdot \epsilon_{fe} \cdot b_v \cdot d_f \cdot \left(\sin\left(\alpha_f\right) + \cos\left(\alpha_f\right)\right)\right) & \text{(Attachment A Eqn. 5.8.3.3-5)} \\ \left(V_f\right) = 34.1 \text{ kips} \\ V_{f\_check1} \coloneqq \left\| \text{"Change FRP Strengthening Scheme"} \quad \text{if } \left(V_f < V_{f\_req}\right) \\ \text{"Provided FRP Strength Large Enough"} & \text{otherwise} \\ V_{f\_check1} = \text{"Provided FRP Strength Large Enough"} \end{split}$$

$$V_{f\_check2} := \| \text{"Provided FRP amount is adequate"} \quad \text{if } \left( V_{f\_req} \leq V_f < 1.1 \cdot V_{f\_req} \right) \\ \| \text{"Change the FRP amount slightly"} \quad \text{otherwise} \\ \\ \left( V_{f\_check2} \right) = \text{"Provided FRP amount is adequate"} \\ \| V_{f\_check2} - V_f \|_{L^2(\mathbb{R}^2)} \leq V_f < 1.1 \cdot V_{f\_req} - V_f <$$

## 5.5 Calculation of Design Shear Resistance of the Member

The design strength of the member is:

$$\begin{split} \phi V_{n\_total} &:= \phi \cdot \left( V_c + V_p + V_s + V_f \right) & \text{(Attachment A Eqn. 5.8.3.3-1)} \\ \left( \phi V_{n\_total} \right) &= 100.2 \text{ kips} \\ \\ \phi V_{n\_check} &:= \left\| \text{"Not Good"} \quad \text{if } V_{u\_crit} > \phi V_{n\_total} \right. \\ \left\| \text{"OK"} \quad \text{otherwise} \right. \\ \left( \phi V_{n\_check} \right) &= \text{"OK"} \\ \\ Web\_crushing\_limit &:= 0.25 \cdot f'_{cb} \cdot b_v \cdot d_v \cdot V_p \quad \text{(LRFD Eqn. 5.8.3.3-2)} \\ Web\_crushing\_limit &= 350.3 \text{ kips} \\ Check\_web\_crushing\_limit &:= \left\| \text{"OK"} \quad \text{if } \left( V_c + V_s + V_f + V_p \right) \le \text{Web\_crushing\_limit} \\ \left\| \text{"No Good"} \quad \text{otherwise} \right. \end{split}$$

# Check\_web\_crushing\_limit = "OK"

#### 6. SUMMARY

Externally bonded FRP sheets were designed in this example. The FRP sheets are applied at 90 degrees with respect to the longitudinal axis of the member with the U-wrap configuration and without anchorage systems as shown in Figure 4. The final design is summarized as:

Use number of plies of FRP sheets  $n_f = 1$  Use the width of FRP sheets  $w_f = 8 \text{ in.}$ 

Use the center-to-center spacing of FRP sheets  $s_f = 12$  in.

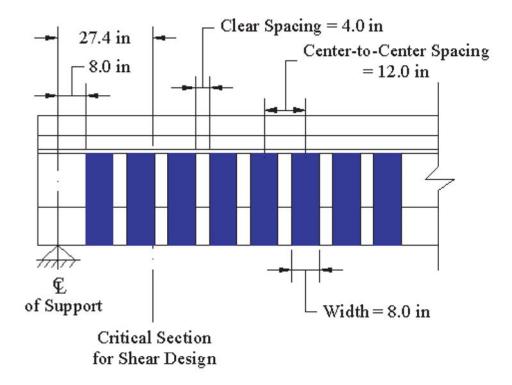
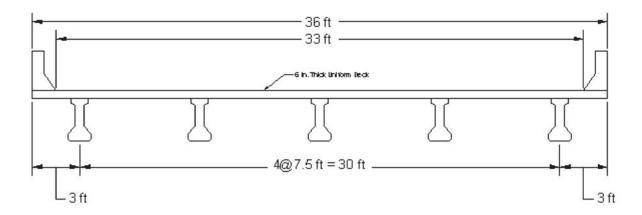


Figure 4. Final design of FRP strengthening.

**DESIGN EXAMPLE 3-2:** PC I-Beam with Internal Transverse Steel Reinforcement Strengthened with FRP in U-wrap Configuration with an Anchorage System

### 1. INTRODUCTION

This example demonstrates the design procedures for externally bonded FRP shear reinforcement of a prestressed I-beam bridge using a U-wrap configuration with anchorage. The bridge consists of five simply supported prestensioned I-beams spanning 42 feet and spaced at 7.5 feet on center. The I-beams are lightly reinforced with transverse steel reinforcement. Additional details of the bulb-tees are provided in Figures 1 and 2.



## (a) Prestressed I-Beam Bridge Deck Cross-Section

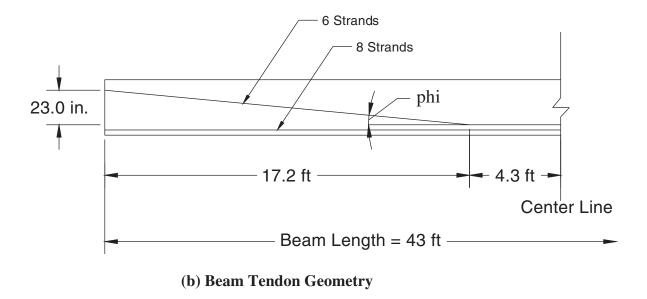


Figure 1. AASHTO bulb-tee bridge deck bridge (Ref. PCI Bridge Design Manual).

#### 2. MATERIAL PROPERTIES

#### 2.1. Concrete

#### 2.1.1 Deck

Compressive strength  $f'_{cd} := 4.0 \text{ ksi}$ 

Modulus of elasticity 
$$E_{cd} := 33 \cdot (1.5)^{1.5} \sqrt{f_{cd} \cdot 1000}$$
 ksi

$$E_{cd} = 3834 \text{ ksi}$$

$$\beta_{1d} := \begin{bmatrix} 0.85 \text{ if } f'_{cd} \le 4 \\ 0.65 \text{ if } f'_{cd} \ge 8 \\ \left[ 0.85 - 0.05 \cdot \left( f'_{cd} - 4 \right) \right] \text{ otherwise} \end{bmatrix}$$

$$\beta_{1d} = 0.85$$

## 2.1.1 I-Beam

Compressive strength  $f'_{cb} := 7.0 \text{ ksi}$ 

Modulus of elasticity  $E_{cb} := 33 \cdot (1.5)^{1.5} \sqrt{f_{cb} \cdot 1000} \text{ ksi}$ 

$$E_{cb} = 5072 \text{ ksi}$$

$$\beta_{1b} := \begin{bmatrix} 0.85 \text{ if } f_{cb} \leq 4 \\ 0.65 \text{ if } f_{cb} \geq 8 \\ \left[ 0.85 - 0.05 \cdot \left( f_{cb} - 4 \right) \right] \text{ otherwise} \end{bmatrix}$$

$$\beta_{1b} = 0.7$$

$$\beta_{1b} = 0.7$$

# 2.2. Prestressing Strands

Specified tensile strength  $f_{pu} := 270 \text{ ksi}$ 

Yield strength  $f_{py} := 243 \text{ ksi}$ 

Modulus of elasticity  $E_{ps} := 28500 \text{ ksi}$ 

Diameter = 0.5 in.

Total Area of the 14 strands  $A_{ps} := 2.142 \text{ in}^2$ 

k := 0.28 for low-relaxation steel

### 2.3. Internal Steel Shear Reinforcement

Yield strength  $f_{yt} := 60 \text{ ksi}$ 

#### 2.4. FRP Reinforcement

Carbon-Fiber Sheets are used in this example.

Thickness  $t_f := 0.0065$  in.

Failure strength  $f_{fu} := 550 \text{ ksi}$ 

Modulus of elasticity  $E_f := 33000 \text{ ksi}$ 

Failure strain 
$$\epsilon_{fu}^{}:=\frac{f_{fu}^{}}{E_f^{}}$$
 
$$\epsilon_{fu}^{}=0.017~in./in.$$

### 3. GEOMETRICAL PROPERTIES

Total height including deck slab  $h_T := 38$  in.

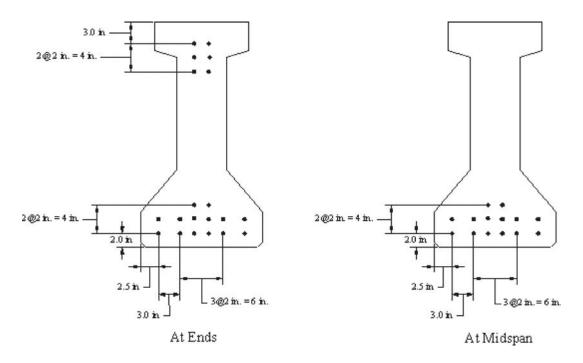
Flange thickness  $h_f := 6$  in.

Width of the web  $b_v := 7$  in.

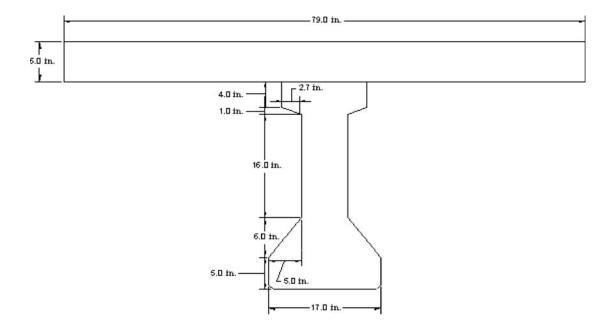
Effective width of the flange  $b_{eff} := 79.0$  in.

Internal shear reinforcement = #3 at 12 in. spacing

$$A_{v} := 0.22 \text{ in}^{2}$$
  $s_{v} := 12 \text{ in.}$   $\alpha := 90 \cdot \text{deg}$ 



## (a) I-Beam Prestressing Pattern



## (b) Cross-Section of an Intermediate Beam

Figure 2. Cross-section of an intermediate beam.

# 4. CALCULATION OF THE FACTORED SHEAR FORCE AND NOMINAL SHEAR RESISTANCE

### 4.1 Factored Shear Force at the Critical Section

$$V_{u\_crit} := 100 \text{ kips}$$

## 4.2. Calculation of Nominal Shear Resistance

For this example, the simplified approach is followed.

$$\theta := 45 \cdot \deg \quad \beta := 2$$

The nominal shear resistance provided by the concrete,  $V_c$ , is calculated in accordance with LRFD Eqn.5.8.3.3-3 as:

The distance from the extreme compression fiber to the center of gravity of the strands at the midspan:

$$d_p := 34.6 \text{ in.}$$

Assuming rectangular section behavior with no compression steel, the distance from the extreme compression fiber to the neutral axis,  $c_c$ , may be calculated as:

$$c_{c} := \frac{A_{ps} \cdot f_{pu}}{0.85 \cdot f'_{cd} \cdot b_{eff} \cdot \beta_{1d} + k \cdot A_{ps} \cdot \frac{f_{pu}}{d_{p}}}$$

$$\left(c_{c}\right) = 2.482 \text{ in.}$$

$$a_{c} := \beta_{1d} \cdot c_{c}$$

$$\left(a_{c}\right) = 2.11 \text{ in.}$$

$$\left(\text{check}\_a_{c} := \left\| \text{"Assumption is correct"} \right\| \text{ if } \left(a_{c} \ge h_{f}\right)$$

$$\| \text{"Not behave as rectangular"} \quad \text{otherwise} \right)$$

$$\left(\text{check}\_a_{c}\right) = \text{"Assumption is correct"}$$

The effective shear depth  $d_v$  is taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken to be less than the greater of  $0.9d_a$  or 0.72h (LRFD Article5.8.2.9).

Since some of the strands are harped, the effective depth varies point-to-point. However, the effective depth must be calculated at the critical section in shear, which is not yet determined; therefore, an iterative procedure is required. For this example, only the final cycle of the iteration is shown.

Assume 
$$d_v d_{v\_trial} := 27.36 \text{ in.}$$

Calculate the distance from the extreme compression face to the center of gravity of the strand,  $d_e$  at the location,  $d_v$  away from the centerline of the support.

$$\mathbf{e}_{\mathrm{tr}} \coloneqq \frac{2 \cdot 4 + 4 \cdot 4 + \left[\frac{23}{206.4} \left(206.4 - \mathbf{d}_{\mathbf{v}\_\mathrm{trial}}\right) + 2\right] \cdot 2 + \left[\frac{23}{206.4} \left(206.4 - \mathbf{d}_{\mathbf{v}\_\mathrm{trial}}\right) + 4\right] \cdot 2 + \left[\frac{23}{206.4} \left(206.4 - \mathbf{d}_{\mathbf{v}\_\mathrm{trial}}\right) + 6\right] \cdot 2}{6 + 6 + 2}$$

$$d_e := h_T - e_{tr}$$
  
 $d_e = 26.021 \text{ in.}$ 

Determine 
$$d_v d_{v1} := d_e - \frac{a_c}{2}$$
  $d_{v2} := 0.9 \cdot d_e$   $\left(d_{v3} := 0.72 \cdot h_T\right)$  
$$\left(d_{v\_max} := \max\left(d_{v1}, d_{v2}, d_{v3}\right)\right)$$
 
$$\left(d_v := \max\left(d_{v\_max}, 0.5 \cdot d_{v\_max} \cdot \cot(\theta)\right)\right)$$
 Final  $d_v d_v = 27.36$  in.

Check\_dv1 := 
$$|"OK" ext{ if } 0.995 \le \frac{d_{v_{trial}}}{d_{v}} \le 1.005$$
  
"Try Again" otherwise

$$Check_dv1 = "OK"$$

Check\_dv2 := 
$$\left| \text{"OK"} \right|$$
 if  $\frac{d_v}{b_v} \le 4$  "NOT GOOD" otherwise

Check 
$$dv2 = "OK"$$

The nominal shear resistance provided by the concrete is:

$$V_{c} := 0.0316 \cdot \beta \cdot \sqrt{f'_{cb}} \cdot b_{v} \cdot d_{v}$$
 (LRFD Eqn. 5.8.3.3-3) 
$$\left(V_{c}\right) = 32 \text{ kips}$$

The nominal shear resistance provided by the internal steel reinforcement is:

$$V_{s} := \frac{A_{v} \cdot f_{yt} \cdot d_{v} \cdot (\cot(\theta) + \cot(\alpha)) \sin(\alpha)}{s_{v}}$$

$$V_{s} = 30.1 \text{ kips}$$
(LRFD Eqn. 5.8.3.3-4)

Harped tendon force =  $6 \times 0.153 \times 149.0 = 136.8$  kips (assuming  $f_{pe} = 149$  ksi) slope of the tendons  $\psi := 0.111$ 

$$V_p := 136.8 \cdot \psi$$
  $V_p = 15.2 \text{ kips}$ 

The nominal shear resistance of the member is:

$$V_n := V_c + V_s + V_p$$
 (LRFD Eqn. 5.8.3.3-1)  
 $V_p = 77.3 \text{ kips}$ 

#### 5. DESIGN OF FRP SHEAR REINFORCEMENT

### 5.1 Check if FRP Reinforcement is Necessary

Strength reduction factor for shear ( $\phi := 0.9$ )

$$\label{eq:check_frp_needed} \mbox{Check_FRP_Needed} := \left| \begin{tabular}{ll} "NOT need shear reinforcement" & if $\left( \varphi \cdot V_n \geq V_{u\_crit} \right)$ \\ "NEED shear reinforcement" & otherwise \\ \end{tabular} \right.$$

Check\_FRP\_Needed = "NEED shear reinforcement"

# 5.2 Computation of Required $V_f$

$$V_{f\_req} := \frac{V_{u\_crit}}{\phi} - V_{n}$$

$$V_{f\_req} = 33.8 \text{ kips}$$

## **5.3 Selection of FRP Strengthening Scheme**

U-wrap configuration is used with anchorage systems at the end of the sheets. The FRP sheets will be applied at 90 degrees with respect to the longitudinal axis of the girder as shown in the Figure 3 below. First, the spacing of FRP strips is chosen to meet the maximum spacing requirement. Then, the width of the FRP strips is selected to adjust the amount of FRP strips.

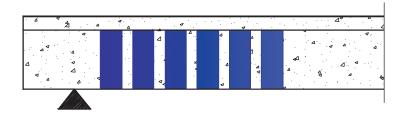


Figure 3. FRP strengthening scheme.

Use number of plies of FRP sheets  $n_f := 1$ Use the width of FRP sheets  $w_f := 4$  in.

Use the center-to-center spacing of FRP sheets  $s_f := 12$  in.

Orientation of FRP sheets

$$\alpha_f := 90 \deg$$

Effective depth of FRP sheets  $d_f := d_p - h_f$ 

$$d_f = 28.6 \text{ in.}$$

Check if the selected spacing is acceptable or not

Shear stress on concrete is:

$$\left(v_{u} := \frac{V_{u\_crit} - \phi \cdot V_{p}}{\phi \cdot b_{v} \cdot d_{v}}\right)$$

$$\left(v_{u}\right) = 0.501 \text{ ksi}$$
(LRFD Eqn. 5.8.2.9-1)

The maximum spacing of the transverse reinforcement is:

$$\begin{split} s_{max} &:= \left| \begin{array}{ll} \min \! \left( 0.8 \cdot d_v, \, 24 \right) \text{ if } v_u < 0.125 \cdot f'_{cb} & \text{(LRFD Eqn. 5.8.2.7-1)} \\ \min \! \left( 0.4 \cdot d_v, \, 12 \right) \text{ otherwise} & \text{(LRFD Eqn. 5.8.2.7-2)} \\ s_{max} &= 21.9 & \\ \text{Check\_Spacing} &:= \left| \begin{array}{ll} \text{"Acceptable"} & \text{if } s_f \leq s_{max} \\ \text{"NOT\_Acceptable\_Change\_the\_Spacing"} & \text{otherwise} \\ \end{array} \right. \end{split}$$

Check\_Spacing = "Acceptable"

# 5.4 Calculation of Shear Resistance of FRP, $V_f$

The FRP reinforcement ratio is:

$$\rho_f := \frac{2 \cdot n_f \cdot w_f \cdot t_f}{b_v \cdot s_f}$$
 (Attachment A Eqn. 5.8.3.3-10) 
$$\left(\rho_f\right) = 6.19 \times 10^{-4}$$

The FRP strain reduction factor is:

$$R_f := \min \left[ 4 \cdot \left( \rho_f \cdot E_f \right)^{-0.67}, 1.0 \right]$$
 (Attachment A Eqn. 5.8.3.3-8) 
$$R_f = 0.53$$

The effective strain of FRP is:

$$\epsilon_{\rm fe}:=R_{\rm f}\cdot\epsilon_{\rm fu} \qquad \qquad ({\rm Attachment\ A\ Eqn.\ 5.8.3.3-7})$$
 
$$\epsilon_{\rm fe}=8.832\times 10^{-3}\ {\rm in./in.}$$

The effective stress of FRP is:

$$f_{fe} := \varepsilon_{fe} \cdot E_{f}$$
 (Attachment A Eqn. 5.8.3.3-6)  
 $\left(f_{fe}\right) = 291.4 \text{ ksi}$ 

The shear contribution of the FRP can be then calculated.

$$\begin{split} \left(V_f \coloneqq \rho_f \cdot E_f \cdot \epsilon_{fe} \cdot b_v \cdot d_f \cdot \left(\sin\left(\alpha_f\right) + \cos\left(\alpha_f\right)\right)\right) & \text{(Attachment A Eqn. 5.8.3.3-5)} \\ \left(V_f\right) &= 36.1 \text{ kips} \\ V_{f\_check1} \coloneqq \left\| \text{"Change FRP Strengthening Scheme"} \quad \text{if } \left(V_f < V_{f\_req}\right) \\ \quad \text{"Provided FRP Strength Large Enough"} \quad \text{otherwise} \\ V_{f\_check1} &= \text{"Provided FRP Strength Large Enough"} \\ V_{f\_check2} \coloneqq \left\| \text{"Provided FRP amount is adequate"} \quad \text{if } \left(V_{f\_req} \le V_f < 1.1 \cdot V_{f\_req}\right) \\ \quad \text{"Change the FRP amount slightly"} \quad \text{otherwise} \end{split}$$

 $V_{f \text{ check2}}$  = "Provided FRP amount is adequate"

# 5.5 Calculation of Design Shear Resistance of the Member

The design strength of the member is:

$$\begin{split} \phi V_{n\_total} &:= \varphi \cdot \left( V_c + V_p + V_s + V_f \right) & \text{(Attachment A Eqn. 5.8.3.3-1)} \\ \left( \phi V_{n\_total} \right) &= 102.1 \text{ kips} \\ \\ \phi V_{n\_check} &:= \left\| \text{"Not Good"} \quad \text{if } V_{u\_crit} > \phi V_{n\_total} \right. \\ \left. \left( \phi V_{n\_check} \right) = \text{"OK"} \right. \\ \\ \left( \phi V_{n\_check} \right) &= \text{"OK"} \\ \\ Web\_crushing\_limit &:= 0.25 \cdot f'_{cb} \cdot b_v \cdot d_v \cdot V_p \quad \text{(LRFD Eqn. 5.8.3.3-2)} \\ Web\_crushing\_limit &= 350.3 \text{ kips} \\ Check\_web\_crushing\_limit &:= \left\| \text{"OK"} \quad \text{if } \left( V_c + V_s + V_f + V_p \right) \leq \text{Web\_crushing\_limit} \\ &= \left\| \text{"No Good"} \quad \text{otherwise} \right. \end{split}$$

Check\_web\_crushing\_limit = "OK"

### 6. SUMMARY

Externally bonded FRP sheets were designed in this example. The FRP sheets are applied at 90 degrees with respect to the longitudinal axis of the member with the U-wrap configuration and without anchorage systems as shown in Figure 4. The final design is summarized as:

Use number of plies of FRP sheets  $n_f = 1$ 

Use the width of FRP sheets  $W_f = 4$  in.

Use the center-to-center spacing of FRP sheets  $s_f = 12$  in.

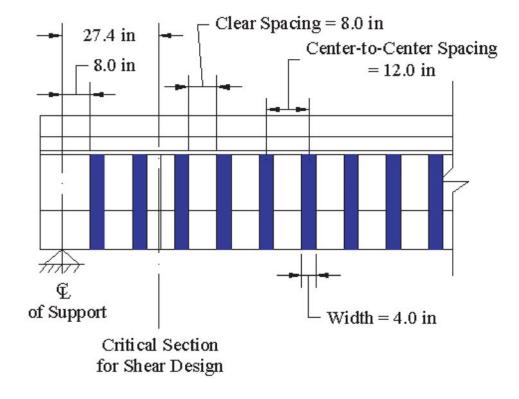


Figure 4. Final design of FRP strengthening.

Abbreviations and acronyms used without definitions in TRB publications:

AAAE American Association of Airport Executives
AASHO American Association of State Highway Officials

AASHTO American Association of State Highway and Transportation Officials

ACI–NA Airports Council International–North America ACRP Airport Cooperative Research Program

ADA Americans with Disabilities Act

APTA American Public Transportation Association
ASCE American Society of Civil Engineers
ASME American Society of Mechanical Engineers
ASTM American Society for Testing and Materials

ATA Air Transport Association
ATA American Trucking Associations

CTAA Community Transportation Association of America
CTBSSP Commercial Truck and Bus Safety Synthesis Program

DHS Department of Homeland Security

DOE Department of Energy

EPA Environmental Protection Agency FAA Federal Aviation Administration FHWA Federal Highway Administration

FMCSA Federal Motor Carrier Safety Administration

FRA Federal Railroad Administration FTA Federal Transit Administration

HMCRP Hazardous Materials Cooperative Research Program
IEEE Institute of Electrical and Electronics Engineers
ISTEA Intermodal Surface Transportation Efficiency Act of 1991

ITE Institute of Transportation Engineers

NASA National Aeronautics and Space Administration
NASAO National Association of State Aviation Officials
NCFRP National Cooperative Freight Research Program
NCHRP National Cooperative Highway Research Program
NHTSA National Highway Traffic Safety Administration

NTSB National Transportation Safety Board

PHMSA Pipeline and Hazardous Materials Safety Administration RITA Research and Innovative Technology Administration

SAE Society of Automotive Engineers

SAFETEA-LU Safe, Accountable, Flexible, Efficient Transportation Equity Act:

A Legacy for Users (2005)

TCRP Transit Cooperative Research Program

TEA-21 Transportation Equity Act for the 21st Century (1998)

TRB Transportation Research Board
TSA Transportation Security Administration
U.S.DOT United States Department of Transportation